

Visualizing Social and Neural Connectivity in Autism: Insights from Clustering and Stochastic Models

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Abstract

Autism spectrum disorder (ASD) is characterized by diverse patterns of social interaction, communication, and behavior. This study explores the application of clustering and stochastic migration models to visualize and understand the social and neural connectivity patterns associated with autism. The clustering model, with its strong internal connections and limited external connections, mirrors the tight-knit social groups and communication barriers often observed in individuals with autism. In contrast, the stochastic model, characterized by more dispersed connections and greater adaptability, represents the variability and flexibility seen in social interactions across typical individuals. By comparing these models, we can gain deeper insights into the unique challenges and strengths of individuals with autism, highlighting the importance of personalized interventions. Additionally, these models provide a visual framework for understanding the differences in brain connectivity patterns observed in autism, with implications for both behavioral and neural correlates. This study underscores the value of computational models in advancing our understanding of autism and guiding effective support strategies.

Keywords: Autism, Neural Connectivity, Clustering, Computational Model

1. Introduction

Autism spectrum disorder (ASD) is a complex neurodevelopmental condition characterized by a wide range of symptoms including difficulties in social interaction, communication challenges, and repetitive behaviors. The heterogeneity of autism makes it imperative to explore diverse models that can encapsulate the various behavioral and neural patterns associated with the disorder. Computational models provide a powerful tool to visualize and analyze these patterns, offering insights that can inform both scientific understanding and practical interventions [1,2].

In this study, we employ two distinct computational models to represent and understand the connectivity patterns in individuals with autism: the clustering migration model and the stochastic migration model. The clustering migration model is designed to mimic the formation of tight-knit social groups, a phenomenon frequently observed in individuals with autism [3]. This model features strong internal connections within clusters and weak connections between clusters, reflecting the tendency of individuals with autism to form strong bonds with specific people while experiencing challenges in establishing connections outside their immediate social circle [4]. This model

also incorporates reverberating signals within clusters with limited exits, symbolizing the repetitive behaviors and restricted interest's characteristic of autism [5].

Conversely, the stochastic migration model represents a more dispersed and variable pattern of connections. This model, characterized by medium-strength connections and multiple exits, encapsulates the variability in social interactions observed across the typical individual [6]. Some individuals with autism, though, exhibit greater adaptability and have a wider range of social connections, which this model effectively captures. The stochastic model's representation of multiple exits suggests a higher degree of flexibility in communication and social behavior, contrasting with the more rigid patterns depicted in the clustering model [7].

Recent advancements in understanding synaptic variability and quantum effects have furthered our knowledge of neural dynamics in ASD. For example, the use of perovskite quantum dots in optoelectronic synaptic devices illustrates the impact of quantum effects on synaptic function and variability, highlighting the importance of integrating quantum mechanics into our understanding of neural processes [8,9].

By comparing these two models, we aim to highlight the diverse social and neural connectivity patterns present in individuals with autism. The clustering model can be seen as a representation of overconnectivity within certain neural networks, while the stochastic model may reflect a more balanced or varied connectivity pattern [10]. These differences in connectivity have significant implications for understanding the neural basis of autism and for developing tailored interventions [11].

Understanding these patterns is crucial for designing effective interventions and support systems. For individuals exhibiting behaviors similar to those in the clustering model, interventions might focus on gradually increasing exposure to new social situations and strengthening weak connections, enhancing communication skills and providing support to navigate varied social interactions could be also beneficial [12,13].

This study underscores the value of computational models in visualizing and understanding the complex patterns of social and neural connectivity in autism. By providing a visual and conceptual framework, these models can guide more effective and personalized strategies for supporting individuals with autism, ultimately contributing to better outcomes and quality of life.

Methodology

This study utilizes computational models to explore the social and neural connectivity patterns associated with autism spectrum disorder (ASD). The methodology involves the implementation of three distinct models, each representing different aspects of connectivity and migration behavior in a simulated neural network. The models include clustering migration, stochastic migration, and detailed simulations of reverberating signals within neural circuits. These models are described by a series of mathematical equations and visualized using Python libraries. Below, we detail the methodological steps and equations used for each model.

3.1. Models

Model 1. Clustering Migration (Graph 1.)

The clustering migration model simulates the formation of tight-knit social groups with strong internal connections and weak connections between clusters.

1. Initial Positions: Cells are uniformly distributed along the x -axis:

$$x_i = -200 + \frac{400i}{N-1} \text{ for } i = 0,1,2, \dots, N-1$$

2. Migration to Semicircle: Cells migrate to form a semicircle of radius 8, with clustering effects introduced by adding Gaussian noise:

$$\begin{aligned} 1) \theta_{1i} &= \frac{i\pi}{N-1} \text{ for } i = 0,1,2, \dots, N-1 \\ 2) x'_{1i} &= r \cos(\theta_{1i}) + \mathcal{N}(0, \sigma^2) \text{ where } \mathcal{N}(0, \sigma^2) \sim \mathcal{N}(0, 0.2^2) \\ 3) y'_{1i} &= r \sin(\theta_{1i}) \end{aligned}$$

3. Connectivity: Strong connections are established within clusters and weak connections between clusters:

$$\begin{aligned} (1) &= w_{\text{strong}} \text{ for } i, j \in C_k \text{ and } i \neq j \\ (2) &w_{i,j} = w_{\text{weak}} \text{ for } i \in C_m, j \in C_n \text{ and } i \neq j \text{ and } m \neq n \end{aligned}$$

Model 2. Stochastic Migration

The stochastic migration model represents more variable connectivity patterns, highlighting the diversity within the autism spectrum.

1. Initial Positions: Similar to Model 1, cells are uniformly distributed along the x -axis.
2. Stochastic Migration: Cells migrate to a semicircle of radius 8, with stochastic variations in their angles:

$$\begin{aligned} \theta_{2i} &= \text{clip} \left(\frac{i\pi}{N-1} + \mathcal{N}(0, \tau^2), 0, \pi \right) \text{ where } \mathcal{N}(0, \tau^2) \sim \mathcal{N}(0, 0.1) \\ x'_{2i} &= r \cos(\theta_{2i}) \\ y'_{2i} &= r \sin(\theta_{2i}) \end{aligned}$$

3. Connectivity Patterns: Various geometric patterns are defined (triangles, squares, hexagons, etc.), with connections established accordingly:

$$\begin{aligned} \text{Triangle: } &w_{i,(i+1) \bmod 3} = w_{i,(i+2) \bmod 3} = 1 \text{ for } i \in \{0,1,2\} \\ \text{Square: } &w_{i,(i+1) \bmod 4} = w_{i,(i+2) \bmod 4} = 1 \text{ for even } i \in \{3,4,5,6\} \\ \text{Hexagon: } &w_{i,(i+1) \bmod 6} = w_{i,(i+2) \bmod 6} = 1 \text{ for } i \in \{7,8,9,10,11,12\} \\ \text{Pentagon: } &w_{i,(i+1) \bmod 5} = 1 \text{ for } i \in \{13,14,15,16,17\} \\ \text{Heptagon: } &w_{i,(i+1) \bmod 7} = 1 \text{ for } i \in \{18,19,20,21,22,23,24\} \end{aligned}$$

4. Medium Strength Random Connections: Additional connections are added with medium strength:
 $w_{i,j} = \text{Uniform}(0.5, 1.5)$ for $i \neq j$ and $(i, j) \notin$ existing edges

Model 3. Detailed Simulations of Reverberating Signals

The detailed simulations involve modeling reverberating signals within neural circuits, highlighting the differences in connectivity and signal propagation.

1. Circle Graph with Exits: A circle graph with 20 nodes is created, with nodes connected in a circular manner and specific exit nodes:

$$\begin{aligned} x_i &= \cos \left(\frac{2\pi i}{N} \right) \text{ for } i = 0,1,2, \dots, N-1 \\ y_i &= \sin \left(\frac{2\pi i}{N} \right) \text{ for } i = 0,1,2, \dots, N-1 \end{aligned}$$

The detailed simulations involve modeling reverberating signals within neural circuits, highlighting the differences in connectivity and signal propagation.

2. Reverberating Signals: Signals propagate with added noise, representing the dynamic nature of neural communication:

$$\begin{aligned} x'_i &= x_i + \mathcal{N}(0, \sigma^2) \\ y'_i &= y_i + \mathcal{N}(0, \sigma^2) \end{aligned}$$

3. Escape Probability: The escape probability at exits is defined by a Bernoulli trial:

$$P_{\text{escape}} = \begin{cases} 1 & \text{if the signal escapes through the exit} \\ 0 & \text{otherwise} \end{cases}$$

4. Number of Reverberations: The number of reverberations is controlled by the number of iterations:

$$\text{Reverberations} = R$$

3.2. Visualization

The models are visualized using Python's Matplotlib library. For each model, the initial and migrated positions of the cells are plotted, with connections indicated by lines. The clustering and stochastic models are shown side-by-side for comparison, highlighting the differences in connectivity patterns.

By applying these models, we aim to capture and analyze the diverse connectivity patterns observed in individuals with autism, providing insights into the social and neural dynamics that characterize the autism spectrum.

4. Results

In this section, we present and interpret the results of the three computational models used to visualize the social and neural connectivity patterns in individuals with autism spectrum disorder (ASD). The models include the clustering migration model, the stochastic migration model, and the detailed simulations of reverberating signals within neural circuits.

Graph 1: Clustering Migration Model

The first graph depicts the clustering migration model, where cells initially distributed along the x axis migrate to form a semicircle with a radius of 8. This model incorporates a clustering effect by adding Gaussian noise to the positions of the cells.

$$\theta_{1i} = \frac{i\pi}{N-1} \text{ for } i = 0, 1, 2, \dots, N-1$$

$$x'_{1i} = r \cos(\theta_{1i}) + \mathcal{N}(0, \sigma^2) \text{ where } \mathcal{N}(0, \sigma^2) \sim \mathcal{N}(0, 0.2^2)$$

$$y'_{1i} = r \sin(\theta_{1i})$$

Observations:

- Cells form distinct clusters with strong internal connections.
- Weak connections are observed between clusters, representing limited interaction outside immediate social groups.
- The clustering effect introduces slight positional perturbations, emphasizing the tendency of individuals with autism to form tight-knit social groups and experience challenges in connecting outside these groups.

This graph effectively models the social dynamics in autism, where strong bonds are formed within specific groups, but communication with external groups is limited [3,4].

Graph 2: Stochastic Migration Model

The second graph illustrates the stochastic migration model, where cells migrate to form a parabola with height of 8,

incorporating stochastic variations in their angles.

This model represents more variable and dispersed connectivity patterns.

$$\theta_{2i} = \text{clip}\left(\frac{i\pi}{N-1} + \mathcal{N}(0, \tau^2), 0, \pi\right) \text{ where } \mathcal{N}(0, \tau^2) \sim \mathcal{N}(0, 0.3^2)$$

$$x'_{2i} = r \cos(\theta_{2i})$$

$$y'_{2i} = r \sin(\theta_{2i})$$

Observations:

- Cells are more evenly dispersed along the semicircle, reflecting greater variability in social interactions.
- The presence of medium-strength random connections between nodes suggests flexibility and adaptability in communication.

This model captures the diversity within the autism spectrum, highlighting individuals who exhibit a wider range of social connections and greater adaptability [7,6].

Graph 3: Reverberating Signals in Neural Circuits

The third graph simulates reverberating signals within neural circuits, highlighting differences in connectivity and signal propagation. Two scenarios are modeled: one with 2 exits and another with 5 exits.

Scenario 1: Circle graph with 20 nodes and 2 exits.

$$x_i = \cos\left(\frac{2\pi i}{N}\right), y_i = \sin\left(\frac{2\pi i}{N}\right)$$

Observations:

- Signals reverberate 20 times within the circle before exiting, representing difficulty in breaking out of behavior loops.
- Limited exits symbolize challenges in transitioning between tasks or environments, akin to the repetitive behaviors seen in autism.

Scenario 2: Circle graph with 20 nodes and 5 exits.

$$x_i = \cos\left(\frac{2\pi i}{N}\right), y_i = \sin\left(\frac{2\pi i}{N}\right)$$

Observations:

- Signals reverberate 5 times within the circle before exiting, indicating greater ease in transitioning between states.
- Multiple exits represent higher flexibility and adaptability in neural communication, akin to individuals with more fluid social interactions.

Reverberating Signals:

$$x'_i = x_i + \mathcal{N}(0, \sigma^2)$$

$$y'_i = y_i + \mathcal{N}(0, \sigma^2)$$

Escape Probability:

$$P_{\text{escape}} = \begin{cases} 1 & \text{if the signal escapes through the exit} \\ 0 & \text{otherwise} \end{cases}$$

These simulations provide insights into the neural dynamics underlying autism. The difficulty in breaking out of behavior loops (as seen in the first scenario) parallels the repetitive behaviors and restricted interests in autism. The preference for continuous movements, such as watching wheels rolling, can be attributed to the brain's need for predictability and order [14].

Conclusion

The results of these computational models highlight the complex social and neural connectivity patterns in individuals with autism. By visualizing these patterns, we can better understand the unique challenges and strengths of individuals on the autism spectrum, ultimately guiding more effective and personalized intervention strategies.

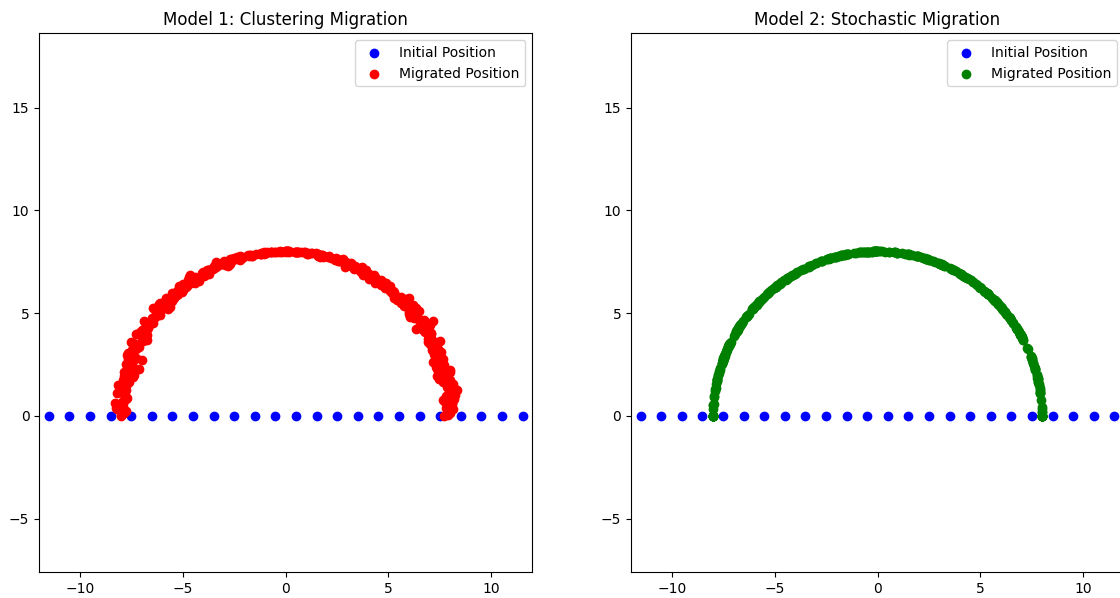
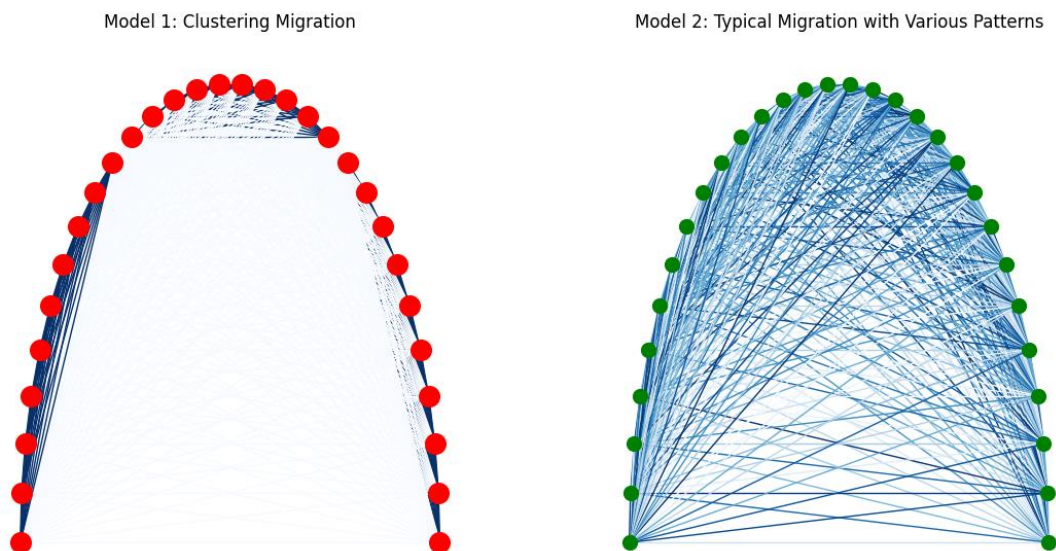
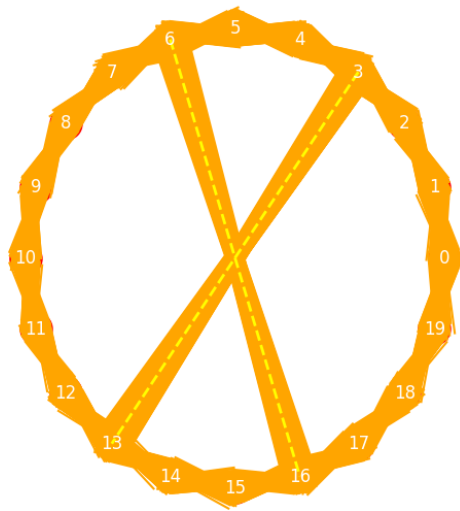


Figure 1: The protoneurons migrate from the midline (simulated as the ventricular wall) to the semicircle line (cortex). Note the formation of clusters in the first graph, representative of autism and the fluid second graph representative of a typical individual.

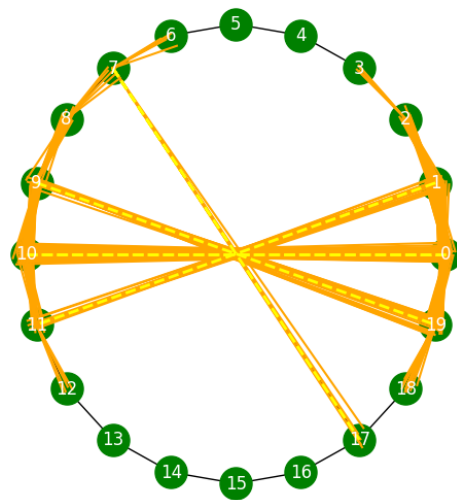


Graph 2: Cells are restricted to its clusters and have poor communications with other clusters, characteristic of autism. On the right graph Cells are more evenly along the parabola, reflecting greater variability in social interactions. The presence of medium-strength random connections between nodes suggests flexibility and adaptability in communication in the right graph

Model 1: Reverberating Circle with 2 Exits



Model 2: Circle with 5 Exits



Graph 3: These simulations provide insights into the neural dynamics underlying autism. The difficulty in breaking out of behavior loops (as seen in the first scenario) parallels the repetitive behaviors and restricted interests in autism (left graph). The preference for continuous movements, such as watching wheels rolling, can be attributed to the brain's need for predictability and order [14]. Right graph represents a typical circuit.

5. Discussion

The computational models employed in this study provide a visual and conceptual framework to understand the diverse social and neural connectivity patterns observed in individuals with autism spectrum disorder (ASD). By comparing the clustering and stochastic migration models, we gain insights into the characteristic behaviors and neural dynamics associated with autism, which have significant implications for intervention and support strategies.

5.1. Clustering Migration Model

The clustering migration model highlights the tendency of individuals with autism to form tight-knit social groups with strong internal connections and weak connections between clusters. This pattern can be interpreted as a reflection of the social dynamics often observed in individuals with autism, who may form strong bonds with specific individuals or groups while experiencing challenges in establishing and maintaining connections outside their immediate social circle [3,4]. The reverberating signals within clusters, with limited exits, symbolize the repetitive behaviors and restricted interest's characteristic of autism [5].

One of the key challenges faced by individuals with autism is difficulty in breaking out of behavior loops. The clustering model's limited exits represent the challenges in transitioning between tasks or environments, which is a common characteristic in autism. Repetitive behaviors and restricted interests, often described as "stimming," provide a sense of predictability and comfort to individuals with autism. These behaviors can be seen as a coping mechanism to deal with overwhelming sensory input or to self-regulate emotions [15]. The model underscores the importance of interventions that gradually introduce new social situations and strengthen weak connections, thereby facilitating

greater social flexibility and adaptability [12].

5.2. Stochastic Migration Model

The stochastic migration model, characterized by more variable and dispersed connections, represents the variability in social interactions observed across the autism spectrum [6]. The model captures the diversity within the autism spectrum, highlighting individuals who exhibit a wider range of social connections and greater adaptability. Interventions for these individuals might focus on enhancing communication skills and providing support to navigate varied social interactions [13].

Recent research on synaptic loss and cognitive deficits in neurological conditions further emphasizes the importance of understanding synaptic variability and its impact on neural connectivity and behavior [16]. Additionally, advancements in quantum biology highlight the potential influence of quantum effects on synaptic function, which could provide new insights into the neural mechanisms underlying ASD [17].

The stochastic migration model, characterized by more variable and dispersed connections, represents the variability in social interactions observed across the autism spectrum and typical individual [6]. Some individuals with autism exhibit greater adaptability and have a wider range of social connections. The stochastic model's multiple exits suggest a higher degree of flexibility in communication and social behavior, which contrasts with the more rigid patterns depicted in the clustering model [7].

5.3. Neural Connectivity and Behavioral Correlates

The observed differences in connectivity in the models have parallels in neural connectivity patterns in individuals with autism. Research has shown that individuals with autism

may exhibit overconnectivity within certain brain regions and underconnectivity between regions, leading to difficulties in integrating information across different neural networks [10,11]. The clustering model can be seen as a representation of overconnectivity within specific neural networks, while the stochastic model may reflect a more balanced or varied connectivity pattern.

These neural connectivity patterns can explain some of the behavioral characteristics of autism. For example, the preference for continuous movements and repetitive actions, such as watching wheels rolling, can be understood as a manifestation of the brain's need for predictability and order. Continuous and repetitive actions provide a sense of stability and control, which can be comforting for individuals with autism who might otherwise experience sensory overload or difficulty in processing complex stimuli [14].

5.4. Implications for Intervention

Understanding these connectivity patterns is crucial for designing effective interventions and support systems for individuals with autism. For those exhibiting behaviors similar to those in the clustering model, interventions might focus on gradually

6. Attachments

Python Code Graph 1.

```
import numpy as np

import matplotlib.pyplot as plt

# Parameters

num_cells = 400

radius = 8

x_positions = np.linspace(-200, 200, num_cells)

# Model 1: Clustering Migration

theta_1 = np.linspace(0, np.pi, num_cells)

x_migrated_1 = radius * np.cos(theta_1)

y_migrated_1 = radius * np.sin(theta_1)

# Adding some clustering effect by perturbing positions

cluster_effect = np.random.normal(0, 0.2, num_cells)
```

increasing exposure to new social situations and strengthening weak connections. This approach can help individuals develop the skills needed to navigate more complex social environments and reduce the reliance on repetitive behaviors [12].

For individuals resembling the stochastic model, interventions might focus on enhancing communication skills and providing support to navigate varied social interactions. These interventions can leverage the existing flexibility and adaptability observed in these individuals, helping them to build more robust social networks and improve their overall social functioning [13].

Conclusion

The computational models presented in this study provide valuable insights into the diverse social and neural connectivity patterns observed in individuals with autism. By visualizing these patterns, we can better understand the unique challenges and strengths of individuals on the autism spectrum, ultimately guiding more effective and personalized support strategies. These models underscore the importance of a nuanced approach to autism intervention, one that recognizes the variability within the spectrum and addresses the specific needs of each individual [18-33].

```

x_migrated_1 += cluster_effect
# Model 2: Stochastic Migration

np.random.seed(42)

theta_2 = np.linspace(0, np.pi, num_cells) + np.random.normal(0, 0.3, num_cells)
theta_2 = np.clip(theta_2, 0, np.pi) # Ensure theta_2 is within [0, pi] to stay above x-axis

x_migrated_2 = radius * np.cos(theta_2)
y_migrated_2 = radius * np.sin(theta_2)

# Plotting the results

fig, ax = plt.subplots(1, 2, figsize=(14, 7))

# Plot for Model 1

ax[0].scatter(x_positions, np.zeros(num_cells), color='blue', label='Initial Position')
ax[0].scatter(x_migrated_1, y_migrated_1, color='red', label='Migrated Position')
ax[0].set_title('Model 1: Clustering Migration')
ax[0].legend()
ax[0].axis('equal')
ax[0].set_xlim([-radius*1.5, radius*1.5])
ax[0].set_ylim([-1, radius*1.5])

nx.draw(G2, nx.get_node_attributes(G2, 'pos'), ax=ax[1], with_labels=True,
node_color='green', edge_color='black', node_size=500, font_color='white')

draw_reverberation(ax[1], G2, exits2, num_reverberations_model2,
escape_ratio_model2, noise_multiplier_model2)

ax[1].set_title('Model 2: Circle with 5 Exits')

```

Python code Graph 2.

```
import numpy as np
```

```
import matplotlib.pyplot as plt

import networkx as nx

import matplotlib.animation as animation

# Function to create a circle graph with exits

def create_circle_graph(num_nodes, num_exits, strong_weight=2, weak_weight=0.1):

    G = nx.Graph()

    nodes = range(num_nodes)

    for i in nodes:

        G.add_node(i, pos=(np.cos(2 * np.pi * i / num_nodes), np.sin(2 * np.pi * i /
num_nodes)))

        G.add_edge(i, (i + 1) % num_nodes, weight=strong_weight)

    exits = np.random.choice(nodes, num_exits, replace=False)

    for exit in exits:

        G.add_edge(exit, (exit + num_nodes // 2) % num_nodes, weight=weak_weight)

    return G, exits

# Parameters

num_nodes = 20

num_exits_model1 = 2

num_exits_model2 = 5

num_reverberations_model1 = 20

num_reverberations_model2 = 5

escape_ratio_model1 = 0.2

escape_ratio_model2 = 0.5

# Create graphs for both models
```

```

G1, exits1 = create_circle_graph(num_nodes, num_exits_model1)
G2, exits2 = create_circle_graph(num_nodes, num_exits_model2)

# Function to draw reverberating signals
def draw_reverberation(ax, G, exits, num_reverberations, escape_ratio):
    pos = nx.get_node_attributes(G, 'pos')
    nodes = list(G.nodes)
    signals = [0] # Start at node 0
    for _ in range(num_reverberations):
        new_signals = []
        for signal in signals:
            neighbors = list(G.neighbors(signal))
            for neighbor in neighbors:
                if np.random.rand() > escape_ratio or neighbor in exits:
                    new_signals.append(neighbor)
                    ax.plot([pos[signal][0], pos[neighbor][0]], [pos[signal][1],
pos[neighbor][1]], color='yellow')
            signals = new_signals

# Plot settings
fig, ax = plt.subplots(1, 2, figsize=(14, 7))

# Plot for Model 1
nx.draw(G1, nx.get_node_attributes(G1, 'pos'), ax=ax[0], with_labels=True,
node_color='red', edge_color='black', node_size=500, font_color='white')

draw_reverberation(ax[0], G1, exits1, num_reverberations_model1,
escape_ratio_model1)

```

```
ax[0].set_title('Model 1: Reverberating Circle with 2 Exits')
```

```
# Plot for Model 2
```

```
nx.draw(G2, nx.get_node_attributes(G2, 'pos'), ax=ax[1], with_labels=True,  
node_color='green', edge_color='black', node_size=500, font_color='white')
```

```
draw_reverberation(ax[1], G2, exits2, num_reverberations_model2,  
escape_ratio_model2)
```

```
ax[1].set_title('Model 2: Circle with 5 Exits')
```

```
plt.show()
```

```
plt.show()
```

```
# Plot for Model 2
```

```
ax[1].scatter(x_positions, np.zeros(num_cells), color='blue', label='Initial Position')
```

```
ax[1].scatter(x_migrated_2, y_migrated_2, color='green', label='Migrated Position')
```

```
ax[1].set_title('Model 2: Stochastic Migration')
```

```
ax[1].legend()
```

```
ax[1].axis('equal')
```

```
ax[1].set_xlim([-radius*1.5, radius*1.5])
```

```
ax[1].set_ylim([-1, radius*1.5])
```

```
plt.show()
```

Python codes

Graph 3.

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
import networkx as nx
```

```
# Function to create a circle graph with exits
```

```
def create_circle_graph(num_nodes, num_exits, strong_weight=2, weak_weight=0.1):
```

```
    G = nx.Graph()
```

```
    nodes = range(num_nodes)
```

```
    for i in nodes:
```

```
        G.add_node(i, pos=(np.cos(2 * np.pi * i / num_nodes), np.sin(2 * np.pi * i /  
num_nodes)))
```

```
        G.add_edge(i, (i + 1) % num_nodes, weight=strong_weight)
```

```
    exits = np.random.choice(nodes, num_exits, replace=False)
```

```
    for exit in exits:
```

```
        G.add_edge(exit, (exit + num_nodes // 2) % num_nodes, weight=weak_weight)
```

```
    return G, exits
```

```
# Parameters
```

```
num_nodes = 20
```

```
num_exits_model1 = 2
```

```
num_exits_model2 = 5
```

```
num_reverberations_model1 = 20
```

```
num_reverberations_model2 = 5
```

```
escape_ratio_model1 = 0.2
```

```
escape_ratio_model2 = 0.5
```

```
noise_multiplier_model1 = 10
```

```
noise_multiplier_model2 = 5
```

```
# Create graphs for both models
```

```
G1, exits1 = create_circle_graph(num_nodes, num_exits_model1)
```

```
G2, exits2 = create_circle_graph(num_nodes, num_exits_model2)
```

```
# Function to draw reverberating signals with noise and exits
```

```
def draw_reverberation(ax, G, exits, num_reverberations, escape_ratio,  
noise_multiplier):
```

```
    pos = nx.get_node_attributes(G, 'pos')
```

```
    nodes = list(G.nodes)
```

```
    signals = [0] # Start at node 0
```

```
    for _ in range(num_reverberations):
```

```
        new_signals = []
```

```
        for signal in signals:
```

```
            neighbors = list(G.neighbors(signal))
```

```
            for neighbor in neighbors:
```

```
                if np.random.rand() > escape_ratio or neighbor in exits:
```

```
                    new_signals.append(neighbor)
```

```
                    for _ in range(noise_multiplier):
```

```
                        noise_x = np.random.normal(0, 0.02)
```

```
                        noise_y = np.random.normal(0, 0.02)
```

```
                        ax.plot([pos[signal][0], pos[neighbor][0] + noise_x], [pos[signal][1],  
pos[neighbor][1] + noise_y], color='orange')
```

```
                    signals = new_signals
```

```
                    for exit in exits:
```

```
ax.plot([pos[exit][0], pos[(exit + num_nodes // 2) % num_nodes][0]],  
        [pos[exit][1], pos[(exit + num_nodes // 2) % num_nodes][1]],  
        color='yellow', linewidth=2, linestyle='dashed')
```

```
# Plot settings
```

```
fig, ax = plt.subplots(1, 2, figsize=(14, 7))
```

```
# Plot for Model 1
```

```
nx.draw(G1, nx.get_node_attributes(G1, 'pos'), ax=ax[0], with_labels=True,  
        node_color='red', edge_color='black', node_size=500, font_color='white')
```

```
draw_reverberation(ax[0], G1, exits1, num_reverberations_model1,  
escape_ratio_model1, noise_multiplier_model1)
```

```
ax[0].set_title('Model 1: Reverberating Circle with 2 Exits')
```

```
# Plot for Model 2
```

Python code graph 3.

Conflict of Interest

The author declares no conflict of interest.

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