# The Equality of the Values of the Area and Perimeter of a Number of TwoDimensional Figures, Volume and Area - Three-Dimensional 

Andrey V. Voron*

*Corresponding Author
Andrey V. Voron, Russia.
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#### Abstract

Annotation Possible variants of the equality of the values of the area and perimeter of a number of two-dimensional figures (square, circle, rectangular, obtuse and equilateral triangles), volume and area - three-dimensional (Platonic bodies, cone, cylinder, pyramid and sphere) are considered.


Keywords: Equality of Values, Two-Dimensional Shapes, Three-Dimensional Shapes, Parameters of Geometric Shapes, Perimeter, Volume, Area

## 1. Introduction

In one of his publications, possible cases of equality (numerical equality) of a number of two-dimensional and three-dimensional geometric shapes were considered [1]. As the research material accumulated, the number of such figures increased. And it can still increase by the efforts of geometry lovers. In this regard, it is hoped that by significantly replenishing the "register" of such geometric shapes, a very beautiful theorem can be formulated.

## 2. The Main Part

Calculations of the parameters of a number of two-dimensional and three-dimensional figures were performed using the online calculator "Geleot". Calculations requiring accuracy of more than three decimal places were performed independently on the basis of appropriate formulas, using a calculator.

According to the results of calculations, the following numerical equalities of the area and perimeter of a number of twodimensional figures were revealed:

- of a square, when the side is 4 (the area and length of the perimeter, respectively, will be equal to the value 16), the radius of the inscribed circle is 2 , and the described one is equal to the value 8 , the diagonal of the square is equal to 32 ;
- a circle, when the equality of the area and the length of the
circle is observed at a value of $12.566 \ldots$ or $4 \pi$ (the radius of the inscribed circle is 2 );
- right-angled triangles with an irrational value of the area and perimeter, when the area and length of the perimeter of the first is equal to $27,416324 \ldots \equiv(\sqrt{5}+3) 2$ ( where the smaller cathet is $5,236 \ldots$ will be equal to $\sqrt{ } 27,416324 \ldots$, and the larger one is double the value of the smaller one $-10,472 \ldots$ ) and the second one, when the cathets are $6,8285 \ldots \equiv(\sqrt{ } 2+2) \times 2$ - with an area and perimeter value of $23.314 \ldots \equiv(\sqrt{ } 8+2) 2$. The radius of the circle inscribed in the triangle is 2 ;
- Heron triangles with sides: $(5,12,13$ and $6,8,10$ are rightangled triangles) when the area and perimeter of the first is equal to the value of 30 , and the second $-24 ; 6,25,29 ; 7,15,20 ; 9$, $10,17 \ldots$ ( obtuse triangles with an area of and the perimeter are equal to $60,42,36$, respectively), the radius of the circle inscribed in the named triangles is 2;
- an equilateral right triangle, with an area value of $20.7846 \ldots$ or $=\sqrt{ } 3 \times 12$ (while the side length is $6.928 \ldots \equiv \sqrt{48}$ or $=\sqrt{ } 3 \times 4$ ), the radius of the inscribed circle is 2 .

The equality of the values of the area and perimeter of a number of two-dimensional shapes, volume and area - threedimensional, image No. 1


Figure 1: Visual representation of four different possible right-angled triangles satisfying the equality $\mathbf{S}=\mathbf{P}$

According to the results of calculations, the following numerical equalities of volume and area of a number of three-dimensional figures were revealed:

- a cube with a face equal to the value of $\sqrt{ } 8$, the volume and surface area of the cube is 216 , the radius of the inscribed sphere is 3 ;
- spheres (equality of volume and surface area) equal to the value $113.097335526 \ldots$ or $36 \pi$ (in this case, the diameter of the sphere is 6 , and its circumference is $18.85 \ldots \equiv 6 \pi$ ), the radius of the inscribed sphere is 3 ;
- tetrahedron (equality of area and volume) equal to $374,123 \ldots$ $\equiv 216 \times \sqrt{ } 3$ (whiletheedgelengthis $14.669693845669907 \ldots \equiv \sqrt{216}$ ), the radius of the inscribed sphere is 3 ;
- octahedron (equality of area and volume) equal to the value $187.061 \ldots \equiv 108 \times \sqrt{ } 3$ (while the edge length is $7.348669228349534 \ldots \equiv \sqrt{ } 54$ ), the radius of the inscribed sphere is 3 ;
- icosahedron (equality of area and volume) equal to the value $136.4595 \ldots$ (while the edge length is $3.9695 \ldots$..), the radius of the inscribed sphere is 3 ;
- dodecahedron (equality of area and volume) equal to the value 149.8578... (while the edge length is $2.694168 \ldots$...) the radius of the inscribed sphere is 3 ;

The equality of the values of the area and perimeter of a number of two-dimensional figures, volume and area - threedimensional, image No. 2


Figure 2: Platonic solids (without dodecahedron) having linear dimensions based on the size of a sphere inscribed in them with a radius of 3 conventional units

- cylinder (equality of area and volume) equal to the value $54 \pi \approx 169.646 \ldots$ (in this case, the radius is 3 , and the height is double the value of the radius -6 ). The area of the side surface is $113.097 \ldots$ (volume and area of the sphere inscribed in the figure) or $36 \pi$, and the area of one of the two bases is $9 \pi$, the radius of the inscribed The volume of the cylinder is equal to 3 . The volume of the cylinder is exactly 1.5 times greater than the volume of the sphere inscribed in it (where there is equality of area and volume values);
- a cone (equality of area and volume) equal to the value $96 \pi \approx$ 301.593... (in this case, the radius of the base is 6 , the forming area is 10 , and the height of the figure is 8 ). The area of the base (circle) is $113.097 \ldots$ (volume and area of the sphere inscribed in the figure) or $36 \pi$, the area of the lateral surface, respectively, $60 \pi$, the radius of the inscribed sphere is 3 ;
- a triangular pyramid (equality of area and volume of a tetrahedron) at a height of 12 , the side of the base is $14.66969384567 \ldots \equiv \sqrt{ } 216$ and is equal to the value $374.123 \ldots$, the radius of the inscribed sphere is 3 ;
- a four-sided pyramid (equality of area and volume) with a height of 12 , the side of the base is $8.485281374 \ldots \equiv \sqrt{ } 72$ and is
equal to 288 . The ratio of height to the side of the base is $\sqrt{ } 2$. At the same time, the area of the side surface of the pyramid is three times the area of the base (216 and 72), the radius of the inscribed sphere is 3 ;
- a hexagonal pyramid with a height of 12 , the side of the base is $4,898979485 \ldots \equiv \sqrt{ } 24$ and is equal to $249.415 \ldots$, the radius of the inscribed sphere is 3 .


## 3. Based on the Calculations Carried out, the Conclusion is

 Formulated- in two-dimensional figures: square, circle, rectangular, obtuse and equilateral triangles, the radius of the inscribed circle with equal values of area and perimeter is 2 ;
- in three-dimensional figures, tetrahedron, cube, octahedron, icosahedron, dodecahedron, cone, cylinder, 3-4-6-sided pyramid and sphere, the radius of the inscribed circle with equal values of area and volume is 3 .


## References

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