

# The Concise Proof Method of the Fermat Conjecture Under the Prime Number Convention

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## Abstract

The 16<sup>th</sup> century French amateur mathematician Fermat declared that he had proved himself but could not prove the proof process in the book, which later became Fermat's Great Theorem. For more than three hundred years, the proof of Fermat's theorem has attracted a large number of mathematicians, and also produced a lot of unintentional results. In 1995, the British mathematician Wiles used a variety of complex modern mathematical methods to prove Fermat's theorem, which became a legend in the history of mathematics. However, people still expect to find the concise proof method claimed by Fermat. This paper proposes a concise proof method of Fermat's great theorem. This method can realize the concise proof of Fermat's great theorem under the condition of prime number convention.

**Keywords:** Fermat's Great Theorem, Concise Proof, Symmetry Exchange Method, Antithesis Method

## 1. Foreword

The French man Fermat is a legend in the history of science, He was a lawyer by profession, But he is well known for his mathematical studies, In 1637, When he was reading the Latin translation of the ancient Greek mathematician Diophantine's book arithmetic, Next to volume 11, proposition 8: " Break a cubic number into the sum of two cubic numbers, Or decompose a fourth power into the sum of two fourth exponents; Or the general decomposition of a power higher than a quadratic into the sum of two equal exponents, This is not possible, About this, I am certain that a wonderful method of proof has been discovered, Unfortunately, the blank space here is too small, Can't write it"

Fermat means that for  $x^n + y^n = z^n$  When  $n > 2$  no positive integer solution, this is the famous Fermat guess, in 1667, his son of the books to this paragraph and published, from then on, Fermat guess attracted countless mathematics lovers, however, since 1667 to the 1990s, no mathematician successfully proved the guess, including famous mathematicians such as Euler and Gauss, so that the conjecture has been rated as the most difficult mathematical problems.

Evidence of Fermat theorem stimulated the development of analytic number theory in the nineteenth century and the twentieth century modular form theorem, during which appeared many proofs for

specific  $n$  value, Fermat himself proved the case of  $n = 4$  in the equation without integer solution, but until the 1990s, has not been able to get the complete proof of Fermat conjecture.

In 1995, the British mathematician Wiles used a variety of complex modern mathematical methods to prove Fermat's great theorem, which became a legend in mathematical history. But one still expects to find the concise method of proof that Fermat claims.

## 2. Main Body

In this paper, we propose a concise proof of Fermat theorem under the prime convention, which adopts the combination of symmetry exchange method and the concise proof of Fermat theorem under the prime convention. This paper plans, proving that the equation  $x^n + y^n = z^n$ , When  $n$  is an odd number greater than equal to 3 and when  $z$  is 3, there is no integer solution, because the equation is an even number equal to 6, the equation can be converted into the corresponding equation with an odd power, because Fermat himself has proved that the equation has no integer solution for  $n = 4$ , as long as the equation  $x^n + y^n = z^n$ , When  $n$  is an odd number greater than or equal to 3, the equation has no integer solution, we can fully prove that Fermat's great theorem holds if the integer is the power of the integer and the integer is greater than or equal to 3

The specific certification process is as follows:

First take  $n = 3$  as an example for the equation  $x^n + y^n = z^n$ ,  $z$  is a prime number greater than or equal to 3, then  $x, y$  must be one odd and one even, first assume a positive integer solution when  $n=3$ , because obviously  $x$  cannot be equal to  $y$ ,  $x + y > z$ , here first assume  $x > y$ , on both sides of the equation simultaneously multiplied by 23, Then obtain equation 2:  $(2x)^3 + (2y)^3 = (2z)^3$ , Next, the symmetry element replacement method is adopted, making  $2x = a + b$ ,  $2y = a - b$ ,  $c = z$ , and substituting equation 2 to obtain equation 3 as follows:

$$(2a)^3 + (a^2 + 3b^2) = (2c)^3,$$

2	$2^2$	$2^3$
c	$1c^2$	$c^3$
2c	$2c^2$	$2c^3$
$2^2c$	$2^2c^2$	$2^2c^3$
$2^3c$	$2^3c^2$	$2^3c^3$

**Table 1: From equation 3, 2a must be used  $(2c)^3$  The product factor,**

When  $2a=2$  can introduce  $a=1$ , the condition of  $a > 3$  in condition 2 is violated

When  $2a=2^2c$  can launch  $a=2$ , violating the condition that a in condition 1 is odd

When  $2a=2^3c$  can launch  $a=4$ , violating the condition that a in condition 1 is odd

When  $2a=c$ , violate the condition in condition 1 where both a and c are odd

When  $2a=c^2$ , in violation of condition 1 where both a and c are odd

When  $2a=c^3$ , in violation of condition 1 where both a and c are odd

When  $2a=2c$  can launch  $a=c$ , violate the condition of  $a > c$  in condition 1

When  $2a=2^2c^2$  can launch  $a=c^2$ , since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a=2^3c^3$  can launch  $a=c^3$ , since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a=4c$  can derive  $a=2c$ , the condition of  $a < 2c$  in condition 2 and the parity of a are violated

When  $2a=4^2c^2$  can launch  $a=2^2c^2$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=4^3c^3$  can launch  $a=2^3c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=8c$  can derive  $a=4c$ , the condition of  $a < 2c$  in condition 2 and the parity of a are violated

When  $2a=8^2c^2$  can launch  $a=4^2c^2$ , Against condition and  $a < 2c$  in

According to equations 2 and 3 and the preset conditions, we can conclude that equations 2 and 3 have positive integer solutions as follows:

Condition 1: because  $2x = a + b$ ,  $2y = a - b$ ,  $a = x + y$ ,  $b = x - y$ , because the previous preset  $x, y$  is odd and even, and  $x > y$ , then a must be odd, and  $a > c$ ;

Condition 2: According to equation 3 and before,  $3 = < c < a < 2c$  Since c is a prime number, according to the permutation combination,  $(2c)^3$  There are only several product factors listed below, which are listed below

condition 2 because  $c > =3$

When  $2a=8^3c^3$  can launch  $a=4^3c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

Since inconsistent conclusions can be derived for each product factor, it can be shown that for  $n=3$ ,  $z$  is prime or equal to  $3^n + y^n = z^n$  No positive integer solution.

However, we should take  $n=5$  as an example for the equation  $x^n + y^n = z^n$ ,  $z$  is a prime number greater than or equal to 3, then  $x, y$  must be odd and even, first assume that there is a positive integer solution when  $n=5$ , because there still must be  $x$  cannot be equal to  $y$ ,  $y + y > z$ , here first assume  $x > y$ , on both sides of the equation multiplied by 25, You can get equation 4:  $(2x)^5 + (2y)^5 = (2z)^5$ ,

Next, the symmetric element replacement method is still adopted, by substituting  $2x=a + b$ ,  $2y=a - b$ ,  $c=z$  into equation 4. Equation 5 is as follows:  $(2a)^5 + (a^4 + 10a^2b^2 + 5b^4) = (2c)^5$ ,

According to equations 4 and 5 and the preset conditions, several conditions that equations 4 and 5 have the positive integer solutions are as follows:

Condition 3: because  $2x=a + b$ ,  $2y=a - b$ , can push  $+ y$  a,  $x, b=x - y$ , because  $x$  is preset,  $y$  is odd and even, and  $x > y$ , then a and b must be odd, and  $a > c$ ,  $b > =1$ ;

Condition 4: According to equation 5 and before,  $3 = < c < a < 2c, 0.5a < c < a$ ,

Since c is a prime number, according to the permutation combination,  $(2c)^5$  There are only several product factors listed below, which are listed below

2	$2^2$	$2^3$	$2^4$	$2^5$
c	$1c^2$	$c^3$	$1c^4$	$1c^5$
2c	$2c^2$	$2c^3$	$2c^4$	$2c^5$
$2^2c$	$2^2c^2$	$2^2c^3$	$2^2c^4$	$2^2c^5$
$2^3c$	$2^3c^2$	$2^3c^3$	$2^3c^4$	$2^3c^5$

$2^4c$	$2^4c^2$	$2^4c^3$	$2^4c^4$	$2^4c^5$
$2^5c$	$2^5c^2$	$2^5c^3$	$2^5c^4$	$2^5c^5$

**Table 2: From equation 5, 2a must be used (2c)<sup>5</sup>The product factor,**

When  $2a=2$  can introduce  $a=1$ , the condition of  $a > 3$  in condition 2 is violated

When  $2a=2^2$  Can launch  $a=2$ , violating the condition that a in condition 1 is odd

When  $2a=2^3$  Can launch  $a=4$ , violating the condition that a in condition 1 is odd

When  $2a=2^4$  Can derive  $a=8$ , violating the condition that a in condition 1 is odd

When  $2a=2^5$  Can derive  $a=16$ , violating the condition that a in condition 1 is odd

When  $2a=c$ , violate the condition in condition 1 where both a and c are odd

When  $2a=c^2$ , In violation of condition 1 where both a and c are odd

When  $2a=c^3$ , In violation of condition 1 where both a and c are odd

When  $2a=c^4$ , In violation of condition 1 where both a and c are odd

When  $2a=c^5$ , In violation of condition 1 where both a and c are odd

When  $2a = 2c$  can launch  $a = c$ , violate the condition of  $a > c$  in condition 1

When  $2a = 2c^2$  Can launch  $a=c^2$ , Since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a = 2c^3$  Can launch  $a=c^3$ , Since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a = 2c^4$  Can launch  $a=c^4$ , Since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a = 2c^5$  Can launch  $a=c^5$ , Since  $c >$ , violating the condition  $a < 2c$  in condition 2 =3

When  $2a = 4c$  can introduce  $a=2c$ , the condition of  $a < 2c$  in condition 2 is violated

When  $2a = 4c^2$  Can launch  $a=2c^2$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a = 4c^3$  Can launch  $a=2c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a = 4c^4$  Can launch  $a=2c^4$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a = 4c^5$  Can launch  $a=2c^5$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a = 8c$  can derive  $a=4c$ , the condition of  $a < 2c$  in condition 2 and the parity of a are violated

When  $2a = 8c^2$  Can launch  $a=4c^2$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a = 8c^3$  Can launch  $a=4c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=8c^4$  Can launch  $a=4c^4$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=8c^5$  Can launch  $a=4c^5$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=16c$  can derive  $a=8c$ , the condition of  $a < 2c$  in condition 2 and the parity of a are violated

When  $2a=16c^2$  Can be launched with  $a=8c^2$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=16c^3$  Can be launched with  $a=8c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=16c^4$  Can be launched with  $a=8c^4$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=16c^5$  Can be launched with  $a=8c^5$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=32c$  can introduce  $a=16c$ ,  $a < 2c$  in condition 2 is violated

When  $2a=32c^2$  Can be launched with  $a=16c^2$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=32c^3$  Can be launched with  $a=16c^3$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=32c^4$  Can be launched with  $a=16c^4$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

When  $2a=32c^5$  Can be launched with  $a=16c^5$ , Against condition and  $a < 2c$  in condition 2 because  $c > =3$

Since inconsistent conclusions can be derived for each product factor, it can be shown that equation  $x^n + y^n = z^n$  for  $n=5$  and  $z$  is a prime more than or equal to  $3^{n+1}y^n=z^n$  No positive integer solution.

Using the above method, we can sequentially prove that, for the equation  $x^n + y^n = z^n$ , when  $n$  is an odd number equal to 3 (3,5,7,9,...), And when  $z$  is a prime number greater than or equal to 3, the contradiction can be introduced, so the equation has no integer solution, and because when  $n$  is an even number greater than or equal to 6, the equation can be transformed into the corresponding equation whose power is odd, the proof method and the proof method when  $n$  is odd are basically the same. The proof process is as follows:

**Next, we take the case of  $n = 6$  as an example**

**When  $n=6$ , and  $z$  is more than 3, the equation  $x^n + y^n = z^n$  No positive integer solution.**

For equation  $x^6 + y^6 = z^6$ ,  $z$  is a prime number greater than or equal to 3, then  $x, y$  must be one odd and one even, first assume that there is a positive integer solution when  $n=6$ , because obviously  $x$  cannot be equal to  $y, y + y > z$ , here first assume  $x > y$ , make  $u = x^2, v = y^2, w = z^2$ , You can get equation 6:  $(u)^3 + (v)^3 = (w)^3$ , According to the preset condition, for equation 6 should satisfy  $u >$

v, u and v should be one odd and one even, and w should be one equal to  $z^2$  The odd number of

For equation 6, both sides are simultaneously multiplied by 23, Then obtain equation 7:  $(2u)^3 + (2v)^3 = (2w)^3$ ,

Next, the symmetry element replacement method is adopted, making  $2u = a + b$ ,  $2v = a - b$ ,  $c = w$ , and substituting equation 2 to obtain equation 8 as follows:

$$(2a)^3 + (a^2 + 3b^2) = (2c)^3,$$

According to equations 6,7 and 8, and preset conditions, we follow that equations 6,7 and 8 have positive integer solutions:

2	$2^2$	$2^3$			
z	$1z^2$	$z^3$	$1z^4$	$1z^5$	$1z^6$
2z	$2z^2$	$2z^3$	$2z^4$	$2z^5$	$2z^6$
$2^2z$	$2^2z^2$	$2^2z^3$	$2^2z^4$	$2^2z^5$	$2^2z^6$
$2^3z$	$2^3z^2$	$2^3z^3$	$2^3z^4$	$2^3z^5$	$2^3z^6$

**Table 3: From equation 9, we know that 2a must be  $2^3z^6$  The product factor,**

When  $2a=2$  can introduce  $a=1$ , the condition of  $a > 3$  in condition 6 is violated

When  $2a=2^2$  Can launch  $a=2$ , violating the condition that a in condition 5 is odd

When  $2a=2^3$  Can derive  $a=4$ , violating the condition that a in condition 5 is odd

When  $2a=z$ , violate the condition where both a and z in condition 5 are odd

When  $2a = z^2$ , The condition where both a and z in condition 5 are odd

When  $2a = z^3$ , The condition where both a and z in condition 5 are odd

When  $2a = z^4$ , The condition where both a and z in condition 5 are odd

When  $2a = z^5$ , The condition where both a and z in condition 5 are odd

When  $2a = z^6$ , The condition where both a and z in condition 5 are odd

When  $2a = 2z$  can launch  $a = z < c$ , violate the condition  $a > c$  in condition 5, condition

When  $2a = 2z^2$  Can be introduced with  $a = z^2 = c$ , condition of  $a > c$  in condition 5

When  $2a = 2z^3$  Can be introduced with  $a = z^3 > 2z^2 = 2c$ , violating the condition with  $a < 2c$  in condition 5

When  $2a = 2z^4$  Can be introduced with  $a = z^4 > 2z^2 = 2c$ , violating the condition with  $a < 2c$  in condition 5

When  $2a = 2z^5$  Can be introduced with  $a = z^5 > 2z^2 = 2c$ , violating the condition with  $a < 2c$  in condition 5

When  $2a = 2z^6$  Can be introduced with  $a = z^6 > 2z^2 = 2c$ , violating the condition with  $a < 2c$  in condition 5

When  $2a = 4z$  can derive  $a = 2z < c$ , the condition of  $a > c$  and the parity of a in condition 5 are violated

When  $2a=4z^2$  Can be introduced with  $a = 2z^2 = 2c$ , violating the

Condition 5: because  $2u = a + b$ ,  $2v = a - b$ ,  $a = u + v$  can be introduced,  $b = u - v$ , because u is preset, v is one odd and one even, and  $u > v$ , then a must be odd, and  $a > c$ ;

Condition 6: According to equation 8 and before,  $3 = c < a < 2c$  support  $c = w = z^2$  In equation 9, equation 9:  $(2a)^3 + (a^2 + 3b^2) = (2z^2)^3 = 2^3z^6$ ,

Since z is a prime number, combined according to the permutation,  $2^3z^6$  There are only several product factors listed below, which are listed below

parity of condition a with  $a < 2c$  in condition 6

When  $2a=4z^3$  Can be introduced with  $a = 2z^3 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=4z^4$  Can be introduced with  $a = 2z^4 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=4z^5$  Can be introduced with  $a = 2z^5 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=4z^6$  Can be introduced with  $a = 2z^6 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=8z$  can introduce  $a=4z$ , violating the parity of a in condition 5

When  $2a=8z^2$  Can be introduced with  $a=4z^2=4c$ , and the condition of  $a < 2c$  in violation condition 6, and the parity of a

When  $2a=8z^3$  Can be introduced with  $a = 4z^3 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=8z^4$  Can be introduced with  $a = 4z^4 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=8z^5$  Can be introduced with  $a = 4z^5 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

When  $2a=8z^6$  Can be introduced with  $a = 4z^6 > 2c$ , violating the condition of  $a < 2c$  in condition 6, and the parity of a

Since inconsistent conclusions can be derived for each product factor, it can be shown that for  $n = 6$ , z is prime or equal to  $3^n + y^n = z^n$  No positive integer solution.

It is next shown with the case at  $n = 10$

When  $n = 10$  and z is more than 3, equation  $x^n + y^n = z^n$  No positive integer solution.

For equation  $x^{10} + y^{10} = z^{10}$ , z is a prime number greater than or equal to 3, then x, y must be one odd and one even, first assume a positive integer solution when  $n=10$ , because obviously x cannot be equal to y,  $y + y > z$ , here first assume  $x > y$ , make  $u = x^2$ ,  $v = y^2$ ,  $w = z^2$ , Then obtain equation 10:  $(u)^5 + (v)^5 = (w)^5$ ,

According to the preset condition, for equation 10 should satisfy  $u > v$ , u and v should be one odd and one even, and w should be one

equal to  $z^2$  The odd number of

For equation 6, both sides are simultaneously multiplied by 25, Then obtain equation 11:  $(2u)^5 + (2v)^5 = (2w)^5$ ,

Next, the symmetry element replacement method is adopted, making  $2u = a + b$ ,  $2v = a - b$ ,  $c = w$ , and substituting equation 2 to obtain equation 12 as follows:

$$(2a)^5(a^4 + 10a^2b^2 + 5b^4) = (2c)^5,$$

According to equation 10, equation 11 and equation 12 and preset conditions, several conditions that equation 10,11 and equation 12 have positive integer solutions are as follows:

Condition 7: because  $2u = a + b$ ,  $2v = a - b$ , can launch  $a = u + v$ ,  $b = u - v$ , because the previous preset  $u, v$  is one odd and one even, and  $u > v$ , then  $a$  must be odd, and  $a > c$ ;

Condition 8: According to equation 12 and before,  $3 = c < a < 2c$  can be introduced

support  $c = w = z^2$  Enter Equation 12 to obtain Equation 13:  $(2a)^5(a^4 + 10a^2b^2 + 5b^4) = (2c)^5 = 2^5z^{10}$

Since  $z$  is a prime number, combined according to the permutation,  $2^5z^{10}$  There are only several product factors listed below, which are listed below

2	$2^2$	$2^3$	$2^4$	$2^5$					
$z$	$1z^2$	$z^3$	$1z^4$	$1z^5$	$1z^6$	$1z^7$	$1z^8$	$1z^9$	$1z^{10}$
$2z$	$2z^2$	$2z^3$	$2z^4$	$2z^5$	$2z^6$	$2z^7$	$2z^8$	$2z^9$	$2z^{10}$
$2^2z$	$2^2z^2$	$2^2z^3$	$2^2z^4$	$2^2z^5$	$2^2z^6$	$2^2z^7$	$2^2z^8$	$2^2z^9$	$2^2z^{10}$
$2^3z$	$2^3z^2$	$2^3z^3$	$2^3z^4$	$2^3z^5$	$2^3z^6$	$2^3z^7$	$2^3z^8$	$2^3z^9$	$2^3z^{10}$
$2^4z$	$2^4z^2$	$2^4z^3$	$2^4z^4$	$2^4z^5$	$2^4z^6$	$2^4z^7$	$2^4z^8$	$2^4z^9$	$2^4z^{10}$
$2^5z$	$2^5z^2$	$2^5z^3$	$2^5z^4$	$2^5z^5$	$2^5z^6$	$2^5z^7$	$2^5z^8$	$2^5z^9$	$2^5z^{10}$

**Table 4: From equation 13 shows that  $2a$  must be  $2^5z^{10}$  The product factor,**

When  $2a = 2$  can introduce  $a = 1$ , the condition of  $a > 3$  in condition 8 is violated

When  $2a = 2^2$  Can be able  $a = 2$ , violating the condition 7 where  $a$  is odd

When  $2a = 2^3$  Can be able  $a = 4$ , violating the condition 7 where  $a$  is odd

When  $2a = 2^4$  Can derive  $a = 8$ , violating the condition that  $a$  in condition 7 is odd

When  $2a = 2^5$  Can launch  $a = 16$ , violating the condition that  $a$  in condition 7 is odd

When  $2a = z$ , violate the condition where both  $a$  and  $z$  in condition 7 are odd

When  $2a = z^2$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^3$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^4$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^5$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^6$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^7$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^8$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^9$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = z^{10}$ , Conditions where both  $a$  and  $z$  in the violation condition 7 are odd

When  $2a = 2z$  can derive  $a = z < c$ , violate the condition of  $a > c$ , in condition 7

When  $2a = 2z^2$  Can be introduced with  $a = z^2 = c$ , condition of  $a > c$

in condition 7

When  $2a = 2z^3$  Can be introduced with  $a = z^3 > 2z^2 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^4$  Can be introduced with  $a = z^4 > 2z^3 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^5$  Can be introduced with  $a = z^5 > 2z^4 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^6$  Can be introduced with  $a = z^6 > 2z^5 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^7$  Can be introduced with  $a = z^7 > 2z^6 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^8$  Can be introduced with  $a = z^8 > 2z^7 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^9$  Can be introduced with  $a = z^9 > 2z^8 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 2z^{10}$  Can be introduced with  $a = z^{10} > 2z^9 = 2c$ , violating the condition of  $a < 2c$  in condition 8

When  $2a = 4z$  can derive  $a = 2z < c$ , the condition of  $a > c$  and the parity of  $a$  in condition 7 are violated

When  $2a = 4z^2$  Can be introduced with  $a = 2z^2 = 2c$ , violating the parity of condition  $a$  with  $a < 2c$  in condition 8

When  $2a = 4z^3$  Can be introduced with  $a = 2z^3 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^4$  Can be introduced with  $a = 2z^4 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^5$  Can be introduced with  $a = 2z^5 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^6$  Can be introduced with  $a = 2z^6 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^7$  Can be introduced with  $a = 2z^7 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^8$  Can be introduced with  $a = 2z^8 > 2c$ , the condition of  $a < 2c$  in violation condition 8, and the parity of  $a$

When  $2a = 4z^9$  Can be introduced with  $a = 2z^9 > 2c$ , the condition of

a  $<2c$  in violation condition 8, and the parity of a  
When  $2a=4z^{10}$  Can be introduced with  $a=2z^{10}>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z$  can launch  $a=4z$ , violating the parity of a in condition  
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When  $2a=8z^2$  Can be introduced with  $a=4z^2=4c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^3$  Can be introduced with  $a=4z^3>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^4$  Can be introduced with  $a=4z^4>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^5$  Can be introduced with  $a=4z^5>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^6$  Can be introduced with  $a=4z^6>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^7$  Can be introduced with  $a=4z^7>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^8$  Can be introduced with  $a=4z^8>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^9$  Can be introduced with  $a=4z^9>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=8z^{10}$  Can be introduced with  $a=4z^{10}>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z$  can launch  $a=8z$ , violating the parity of a in  
condition 7

When  $2a=16z^2$  Can be introduced with  $a=8z^2=8c$ , condition of a  
 $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^3$  Can be introduced with  $a=8z^3>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^4$  Can be introduced with  $a=8z^4>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^5$  Can be introduced with  $a=8z^5>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^6$  Can be introduced with  $a=8z^6>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^7$  Can be introduced with  $a=8z^7>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^8$  Can be introduced with  $a=8z^8>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^9$  Can be introduced with  $a=8z^9>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=16z^{10}$  Can be introduced with  $a=8z^{10}>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z$  can introduce  $a=16z$ , violating the parity of a in

condition 7

When  $2a=32z^2$  Can be launched with  $a=16z^2=16c$ , condition of a  
 $<2c$  in violation condition 8, and parity of a

When  $2a=32z^3$  Can be launched with  $a=16z^3>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^4$  Can be launched with  $a=16z^4>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^5$  Can be launched with  $a=16z^5>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^6$  Can be launched with  $a=16z^6>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^7$  Can be launched with  $a=16z^7>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^8$  Can be launched with  $a=16z^8>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^9$  Can be launched with  $a=16z^9>2c$ , the condition of  
a  $<2c$  in violation condition 8, and the parity of a

When  $2a=32z^{10}$  Can be launched with  $a=16z^{10}>2c$ , the condition  
of a  $<2c$  in violation condition 8, and the parity of a

Since inconsistent conclusions can be derived for each product  
factor, it can also be shown that for  $n=10$ ,  $z$  is prime greater than or  
equal to  $3^n + y^n = z^n$  No positive integer solution.

Using the above method, we can successively prove that, for the  
equation  $x^n + y^n = z^n$ , When  $n$  is an even number of 4 greater than or  
equal to 3 (6,10,14,18,...) And when  $z$  is a prime number greater  
than or equal to 3, a contradiction can be introduced, so there is no  
integer solution in this case, because Fermat himself has shown  
that the equation has no integer solution in the case of  $n=4$ , it can  
be proved for  $x^n + y^n = z^n$  when  $n > 2$ , there is no positive integer  
solution under the condition that the integer  $Z$  is prime, so the  
complete proof holds under the condition that the integer is prime  
and the power of the integer is greater than or equal to 3

### 3. Conclusion

In conclusion, this paper uses the symmetry replacement method,  
the enumeration method and the antithesis method to give a concise  
proof of the condition that the integer is prime, and the power of  
the integer is greater than or equal to 3. Since prime numbers are  
the basic composition of composite numbers, the authors also  
believe that the method will help to finally find the concise method  
of proof claimed by Fermat [1].

### Reference

1. Cao Zexian, an excellent proof in the history of Mathematics,  
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