

# Dark Matter-Dark Energy as Massive Bosons a Quantum Multi-Entanglement System with Dark Matter or Dark Energy as Some Massive Bosons-String Particles of Spin 2

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**Submitted:** 2024, Aug 22; **Accepted:** 2024, Sep 13; **Published:** 2024, Sep 18

**Citation:** Kpotogbey, R. D. (2024). Dark Matter-Dark Energy as Massive Bosons a Quantum Multi-Entanglement System with Dark Matter or Dark Energy as Some Massive Bosons-String Particles of Spin 2. *Ann Comp Phy Material Sci*, 1(3), 01-119.

## Abstract

*A quantum multi-entanglement system with Dark matter or dark energy as some massive bosons-string particles of spin 2. Dark matter or dark energy are some particles of spin 2 instead of near spin 0 ones.*

*Example 1:  $dE = 4\sqrt{(gM^2)/\sqrt{2}} \sim 125.5673374143954990316092809188 \text{ GeV}$  ( $(gM^2) = 1393.6328858707575005182839547884 \text{ GeV}^2$ ) the particle at exactly some 125 GeV and spin 1+1+1-1=2 (As a frequent Space-Time reflect.) or 1-1+1-1=0. The Source of massive bosons that are dark matter-dark energy simulators is probably the extreme side of black hole's core where the magnetic field stopping matter is getting strongest. Magnetic Field [B] = kg/(s<sup>2</sup>.A), ([E] = m<sup>2</sup>.kg/s<sup>2</sup>), [E].(1/(m<sup>2</sup>.A)) = [B], A↗, d↘ → E↖ ([d] = m), M↗ → q.A↗, d↘ → E↗ ([M] = kg)*

$$\frac{1}{m_{massive\,boson}^2} \propto q$$

*We strive to prevent the emission of massive gravitons into the central black hole, considering that a Modified Newtonian dynamics would require measurement of its effects starting from the sun and its  $(4.152 \pm 0.014) \cdot 10^6 M_{\text{sun}} \rightarrow L \sim 2.5 \text{ kpc} = 7.7142 \cdot 10^{19} \text{ m}$  new gravitational field:*

$IM_{\text{sun}} \rightarrow 0.602119460500963 \cdot 10^6 \text{ kpc}$  ( $1.857947976878612 \cdot 10^{13} \text{ m} = 124.1960537090558 \text{ UA} > 40 \text{ UA}$ : And have, from certain constant effects, effects on the closest star to the Sun, a Cen C (Proxima Centauri), is 1.316 parsec (4.28 light years) away [1]. Or  $(4.152 \pm 0.014) \cdot 10^6 M_{\text{sun}} \rightarrow (L \sim 2.5 \text{ kpc} = 7.7142 \cdot 10^{19} \text{ m})^2$

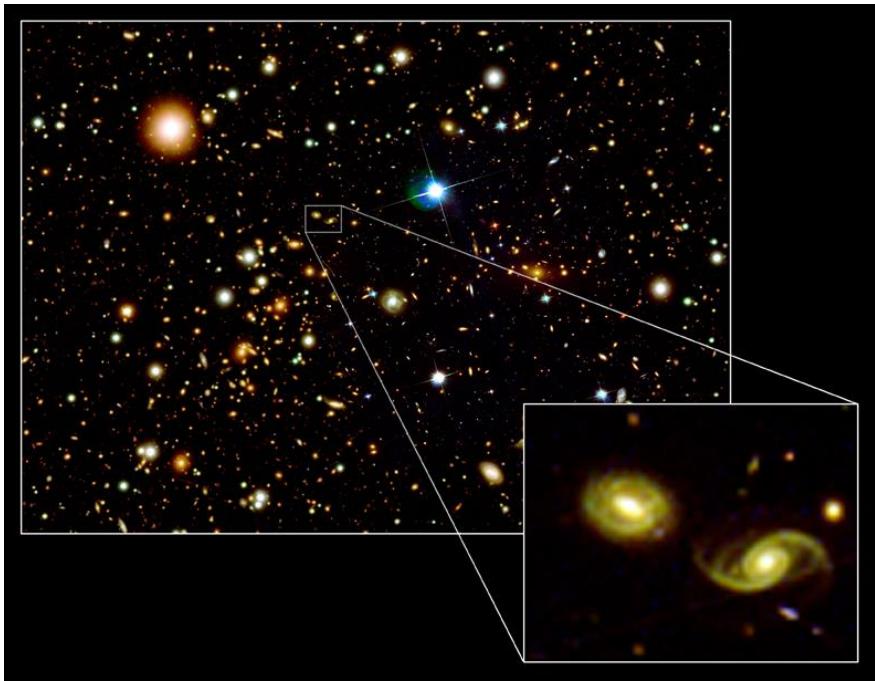
$$IM_{\text{sun}} \rightarrow 1.505298651252408 \cdot 10^{-6} \text{ kpc}^2 \rightarrow 0.001226906129763972 \text{ kpc} (3.785839706490093 \cdot 10^{16} \text{ m})$$

$= 253067.5548359765 \text{ UA}$  To affect the closest star to the Sun, a Cen C (Proxima Centauri), is 1.316 parsec (4.28 light years) away. Dark Matter-Effects evolve with the quantity of black holes and black holes-cores like another row of other hypothetical phenomena [2].

## 1. Introduction

### 1.1. The Galaxy Cluster 1E 0657-56, also known as the "Bullet Cluster"

The bullet cluster is marked by a unique combination of massive spin +2 and spin -2 boson effects [3]. These massive bosons are generated from the MAD of the matter rotating around each black hole. The spin +2 bosons are then generated in these cases in the opposite direction of the massive spin -2 bosons and somehow jump over a black hole and decelerate matter towards the global collision point.



**Figure 1: Galaxy Cluster in Perspective [4]**

This optical image from Hubble and Magellan shows a close-up (inset) of one of the galaxies, a spiral galaxy approximately the same size as the Milky Way, within the galaxy cluster known as 1E 0657-56. The full-field view shows over a thousand galaxies in this cluster. These immense objects are among the largest structures in the Universe.

[View Motion Graphic](#)

Scale: Full-field image is 7.5 x 5.4 arcmin

(Credit: NASA/STScI; Magellan/U. Arizona/D. Clowe et al.)

The structure of the surrounding matter of each black hole undergoes changes that are directly proportional to changes in each black hole's MAD system. The effect of massive bosons with spin +2 rather than -2 or the effect of dark energy appears from 2000000 light years around a central black hole, i.e. 40 units further than the radius of a galaxy [5].

## 1.2. Asymmetric Entanglement Processes Observed from Graphs

We have (1)  $dE_{k3} = 4\sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2 \cdot k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2}))}$  (4dprocess);

(1 – 1)  $dE_{k3} = 4\sqrt{(1393.6328858707575005182839547884 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2 \cdot k3)})^{\frac{1}{2}}}{-\frac{2^3}{2+2 \cdot k3} + 2^2}))}$

### 1.2.1. Case#1

{gM:  $\sqrt{1393.6328858707575005182839547884}$ }

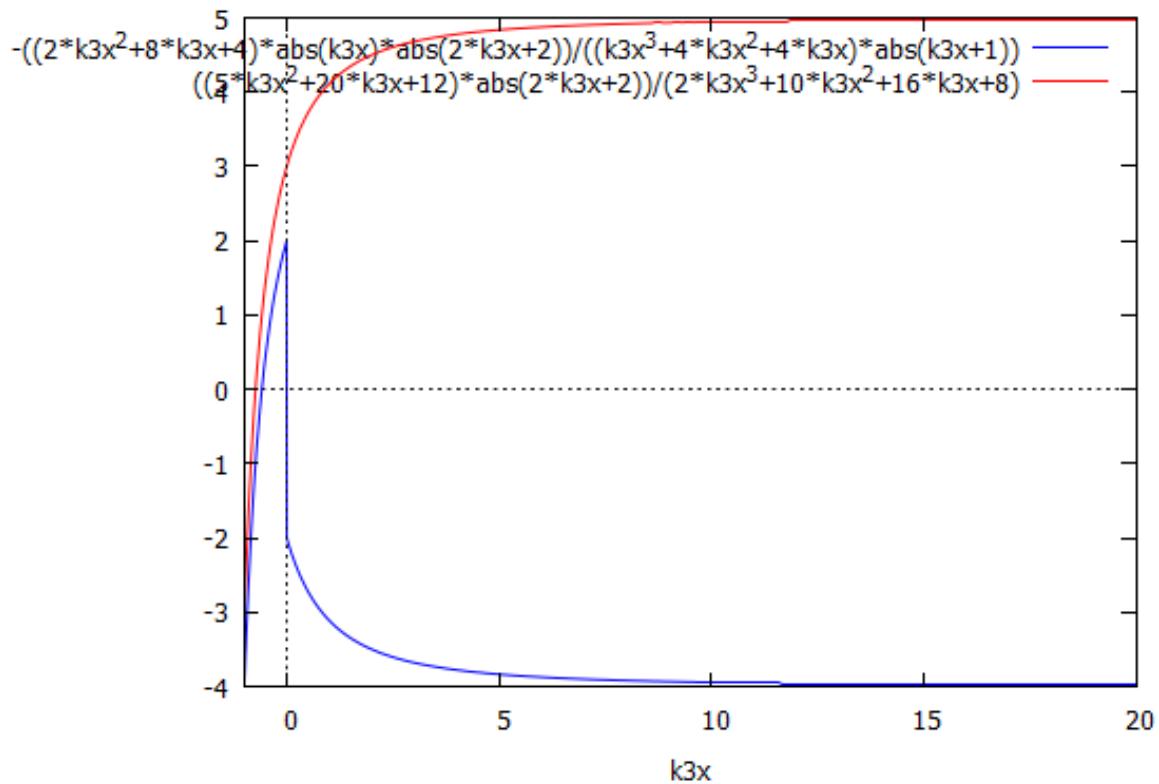
{if  $k3x! = 0$  and  $k3x! = -1$  and  $k3x! = -2$  then  $(dEd(2^{7/4}) * gM * \sqrt{abs(k3x+1)}) / (\sqrt{abs(k3x)} * abs(2 * k3x + 2)^{1/4})$ }

f1Ek3x=-((2^(11/4)\*gM\*k3x^2+2^(19/4)\*gM\*k3x+2^(15/4)\*gM)\*sqrt(abs(k3x))\*abs(2\*k3x+2)^(3/4))/((k3x^3+4\*k3x^2+4\*k3x)\*sqrt(abs(k3x+1)))

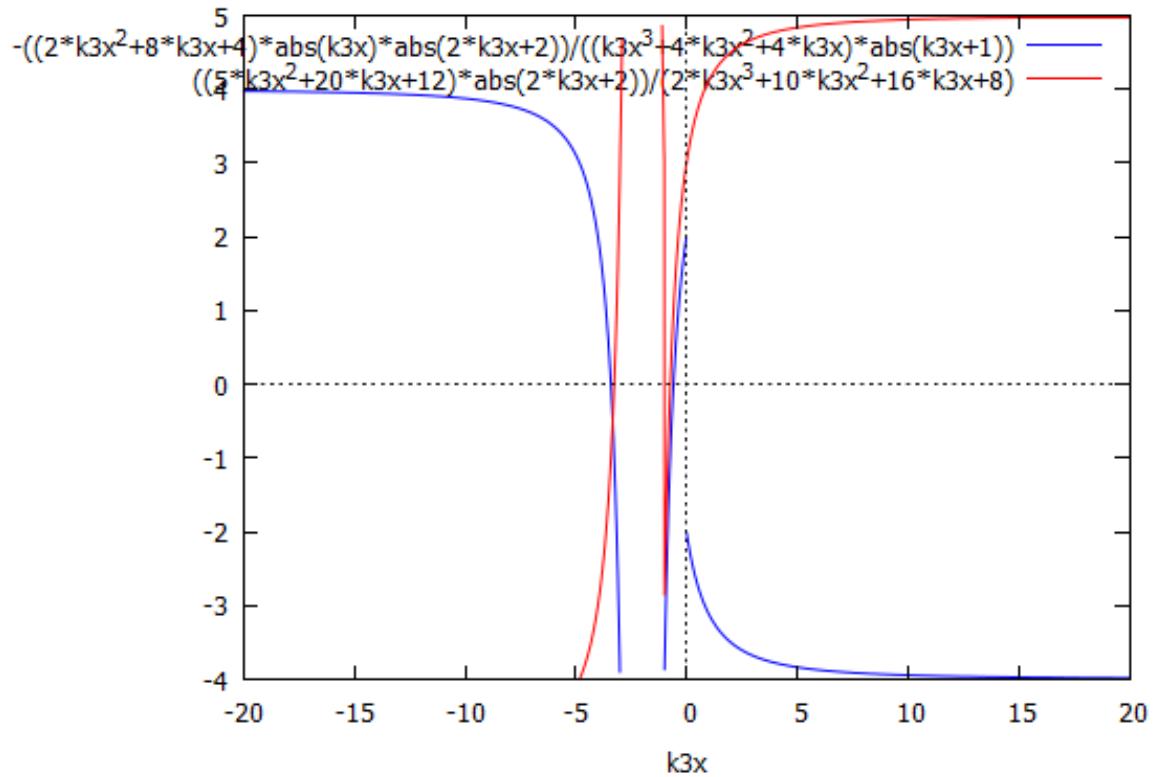
f2Ek3x=((5\*2^(3/4)\*gM\*k3x^3+25\*2^(3/4)\*gM\*k3x^2+2^(23/4)\*gM\*k3x+3\*2^(11/4)\*gM)\*abs(k3x)^(3/2)\*abs(2\*k3x+2)^(3/4))/((k3x^4+4\*k3x^3+4\*k3x^2)\*abs(k3x+1)^(3/2))}}

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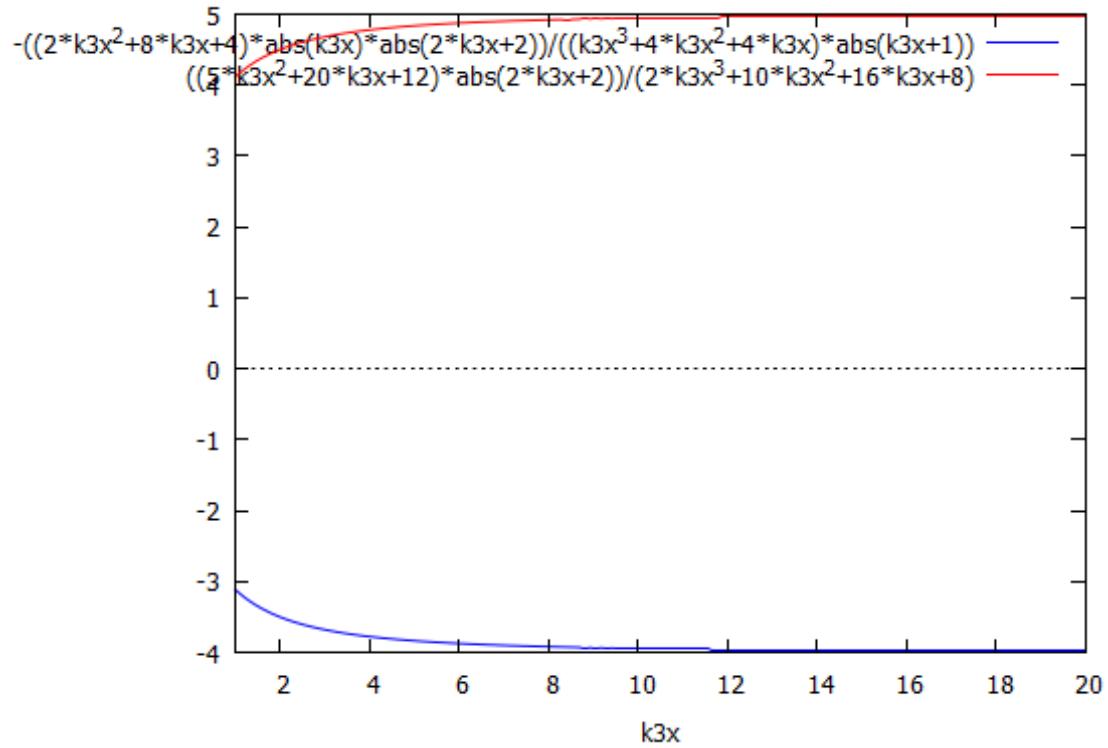
→ Plots



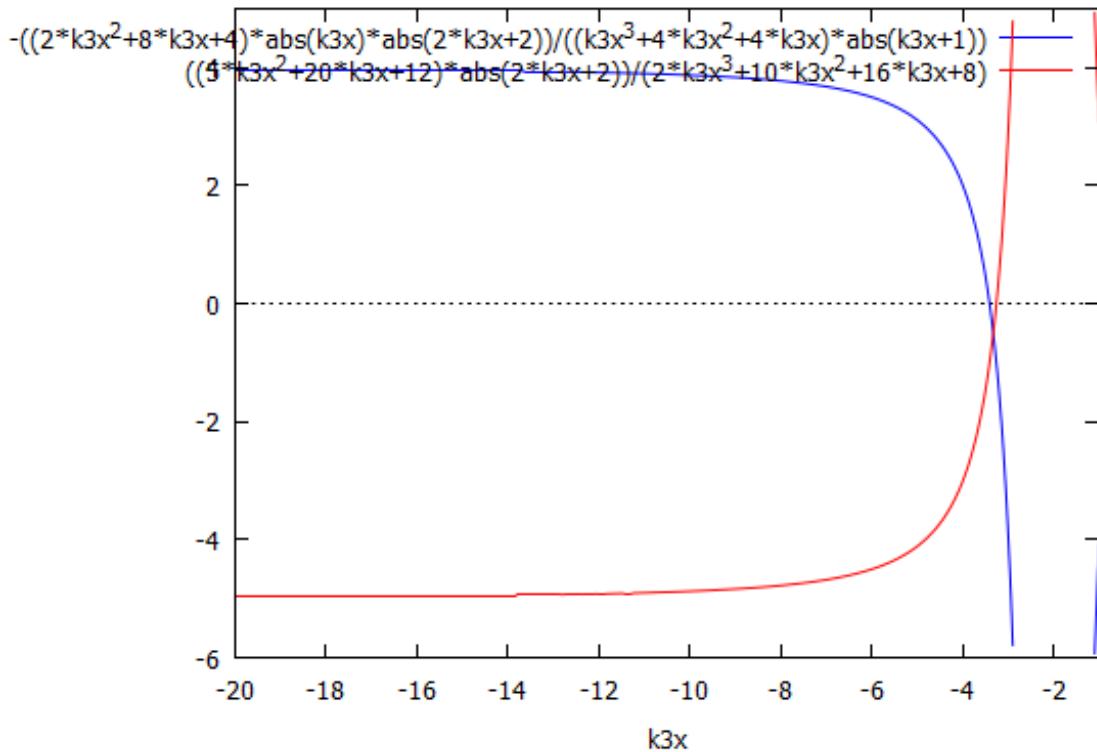
**Figure 2:** Plot2d  $([-((2*k3x^2+8*k3x+4)*abs(k3x)*abs(2*k3x+2))/((k3x^3+4*k3x^2+4*k3x)* abs(k3x+1)), ((5*k3x^2+20*k3x+12)*abs(2*k3x+2))/(2*k3x^3+10*k3x^2+16*k3x+8)], [k3x, -1, 20])\$$



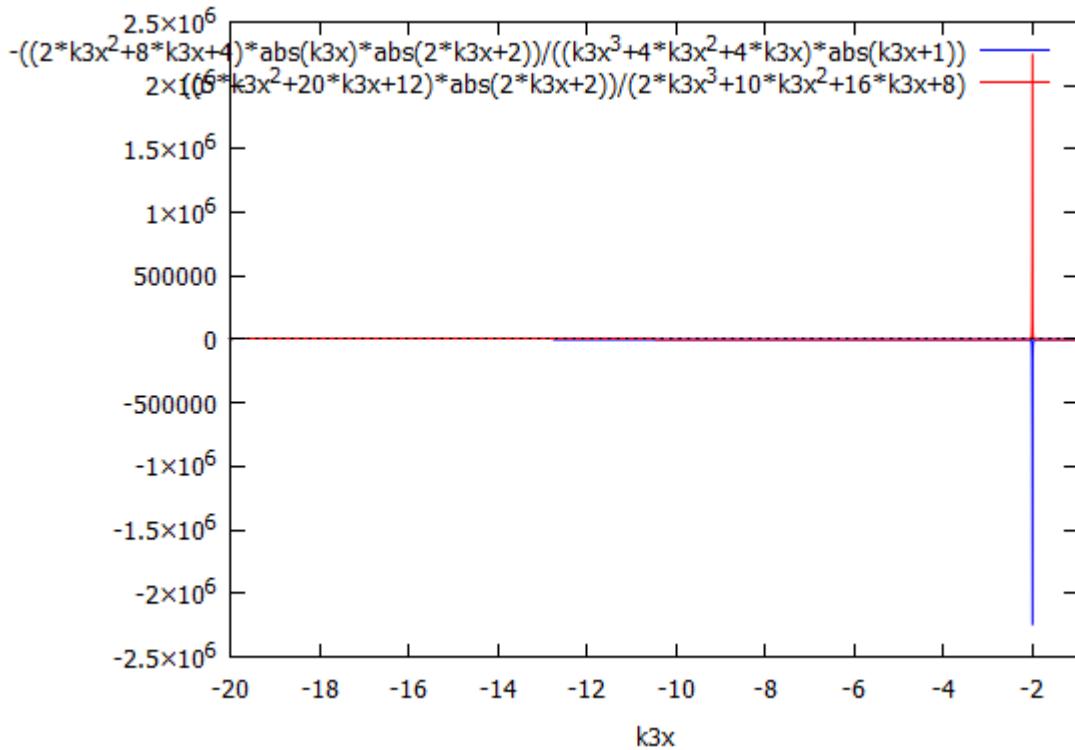
**Figure 3:** Plot2d  $([-((2*k3x^2+8*k3x+4)*abs(k3x)*abs(2*k3x+2))/((k3x^3+4*k3x^2+4*k3x)* abs(k3x+1)), ((5*k3x^2+20*k3x+12)*abs(2*k3x+2))/(2*k3x^3+10*k3x^2+16*k3x+8)], [k3x, -20, 20], [y, -4, 5])\$$



**Figure 4:** Plot2d ([-((2\*k3x^2+8\*k3x+4)\*abs(k3x)\*abs(2\*k3x+2))/((k3x^3+4\*k3x^2+4\*k3x)\* abs(k3x+1)), ((5\*k3x^2+20\*k3x+12)\*abs(2\*k3x+2))/(2\*k3x^3+10\*k3x^2+16\*k3x+8)], [k3x, 1, 20], [y,-4,5])\$



**Figure 5:** Plot2d ([-((2\*k3x^2+8\*k3x+4)\* abs(k3x)\*abs(2\*k3x+2))/((k3x^3+4\*k3x^2+4\*k3x)\* abs(k3x+1)), ((5\*k3x^2+20\*k3x+12)\*abs(2\*k3x+2))/(2\*k3x^3+10\*k3x^2+16\*k3x+8)], [k3x,-20, -1], [y,-6,5])\$



**Figure 6:** Plot2d ([-((2\*k3x^2+8\*k3x+4)\*abs(k3x)\*abs(2\*k3x+2))/((k3x^3+4\*k3x^2+4\*k3x)\*abs(k3x+1)), ((5\*k3x^2+20\*k3x+12)\*abs(2\*k3x+2))/(2\*k3x^3+10\*k3x^2+16\*k3x+8)], [k3x, -20, -1])\$

### 1.2.2. Case#2

{gM = sqrt(1393.6328858707575005182839547884),  
 {if k3x! = 0 and k3x! = -1 and k3x! = -2 then (dEd = (2^(7/4)\*gM\*sqrt(abs(k3x+1)))/(sqrt(abs(k3x))\*abs(2\*k3x+2)^(1/4)))

f1Ek3x

$$= -((2^{(11/4)}*gM*k3x^3+5*2^{(11/4)}*gM*k3x^2+3*2^{(15/4)}*gM*k3x+2^{(15/4)}*gM)*abs(k3x)^(3/2)*abs(2*k3x+2)^(3/4))/((k3x^4+4*k3x^3+4*k3x^2)*abs(k3x+1)^(3/2))$$

f2Ek3x

$$= ((2^{(27/4)}*gM*k3x+2^{(27/4)}*gM)*sqrt(abs(k3x))*abs(2*k3x+2)^(3/4))/((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*sqrt(abs(k3x+1)))$$

f3Ek3x

$$= -((5*2^{(11/4)}*gM*k3x^5+45*2^{(11/4)}*gM*k3x^4+71*2^{(15/4)}*gM*k3x^3+95*2^{(15/4)}*gM*k3x^2+7*2^{(27/4)}*gM*k3x+3*2^{(23/4)}*gM)*abs(k3x)^(3/2)*abs(2*k3x+2)^(3/4))/((k3x^6+8*k3x^5+24*k3x^4+32*k3x^3+16*k3x^2)*abs(k3x+1)^(3/2))$$

f4Ek3x

$$= -((5*2^{(11/4)}*gM*k3x^5+45*2^{(11/4)}*gM*k3x^4+71*2^{(15/4)}*gM*k3x^3+95*2^{(15/4)}*gM*k3x^2+7*2^{(27/4)}*gM*k3x+3*2^{(23/4)}*gM)*abs(k3x)^(3/2)*abs(2*k3x+2)^(3/4))/((k3x^6+8*k3x^5+24*k3x^4+32*k3x^3+16*k3x^2)*abs(k3x+1)^(3/2))$$

f5Ek3x

$$= (k3x^2*(45*gM*k3x^4+315*gM*k3x^3+594*gM*k3x^2+444*gM*k3x+120*gM)*sqrt(abs(k3x))*abs(2*k3x+2)^(7/4))/((k3x+1)^2*(2^(1/4)*k3x^6+3*2^(5/4)*k3x^5+3*2^(9/4)*k3x^4+2^(13/4)*k3x^3)*sqrt(abs(k3x+1)))\}$$

$$\rightarrow \{(-((2^{(11/4)}*gM*k3x^3+5*2^{(11/4)}*gM*k3x^2+3*2^{(15/4)}*gM*k3x+2^{(15/4)}*gM)*abs(k3x)^(3/2)*abs(2*k3x+2)^(3/4))/((k3x^4+4*k3x^3+4*k3x^2)*abs(k3x+1)^(3/2))),$$

$$(((2^{(27/4)}*gM*k3x+2^{(27/4)}*gM)*sqrt(abs(k3x))*abs(2*k3x+2)^(3/4))/((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*sqrt(abs(k3x+1))))/((2^{(7/4)}*gM*sqrt(abs(k3x+1)))/(sqrt(abs(k3x))*abs(2*k3x+2)^(1/4))),$$

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$$(-(5 \cdot 2^{11/4} \cdot gM \cdot k3x^5 + 45 \cdot 2^{11/4} \cdot gM \cdot k3x^4 + 71 \cdot 2^{15/4} \cdot gM \cdot k3x^3 + 95 \cdot 2^{15/4} \cdot gM \cdot k3x^2 + 7 \cdot 2^{27/4} \cdot gM \cdot k3x - 3 \cdot 2^{23/4} \cdot gM) \cdot \text{abs}(k3x)^{(3/2)} \cdot \text{abs}(2 \cdot k3x + 2)^{(3/4)}) / ((k3x^6 + 8 \cdot k3x^5 + 24 \cdot k3x^4 + 32 \cdot k3x^3 + 16 \cdot k3x^2) \cdot \text{abs}(k3x + 1)^{(3/2)}) /$$

$$((2 \cdot 2^{7/4} \cdot gM \cdot \text{sqrt}(\text{abs}(k3x + 1))) / (\text{sqrt}(\text{abs}(k3x)) \cdot \text{abs}(2 \cdot k3x + 2)^{(1/4)})),$$

$$\dots$$

$$/ ((2 \cdot 2^{7/4} \cdot gM \cdot \text{sqrt}(\text{abs}(k3x + 1))) / (\text{sqrt}(\text{abs}(k3x)) \cdot \text{abs}(2 \cdot k3x + 2)^{(1/4)}))$$

$$((k3x^2 \cdot (45 \cdot gM \cdot k3x^4 + 315 \cdot gM \cdot k3x^3 + 594 \cdot gM \cdot k3x^2 + 444 \cdot gM \cdot k3x + 120 \cdot gM) \cdot \text{sqrt}(\text{abs}(k3x)) \cdot \text{abs}(2 \cdot k3x + 2)^{(7/4)}) / ((k3x + 1)^2 \cdot (2 \cdot (1/4) \cdot k3x^6 + 3 \cdot 2^{(5/4)} \cdot k3x^5 + 3 \cdot 2^{(9/4)} \cdot k3x^4 + 2^{(13/4)} \cdot k3x^3) \cdot \text{sqrt}(\text{abs}(k3x + 1)))) /$$

$$((2 \cdot 2^{7/4} \cdot gM \cdot \text{sqrt}(\text{abs}(k3x + 1))) / (\text{sqrt}(\text{abs}(k3x)) \cdot \text{abs}(2 \cdot k3x + 2)^{(1/4)})) \}$$

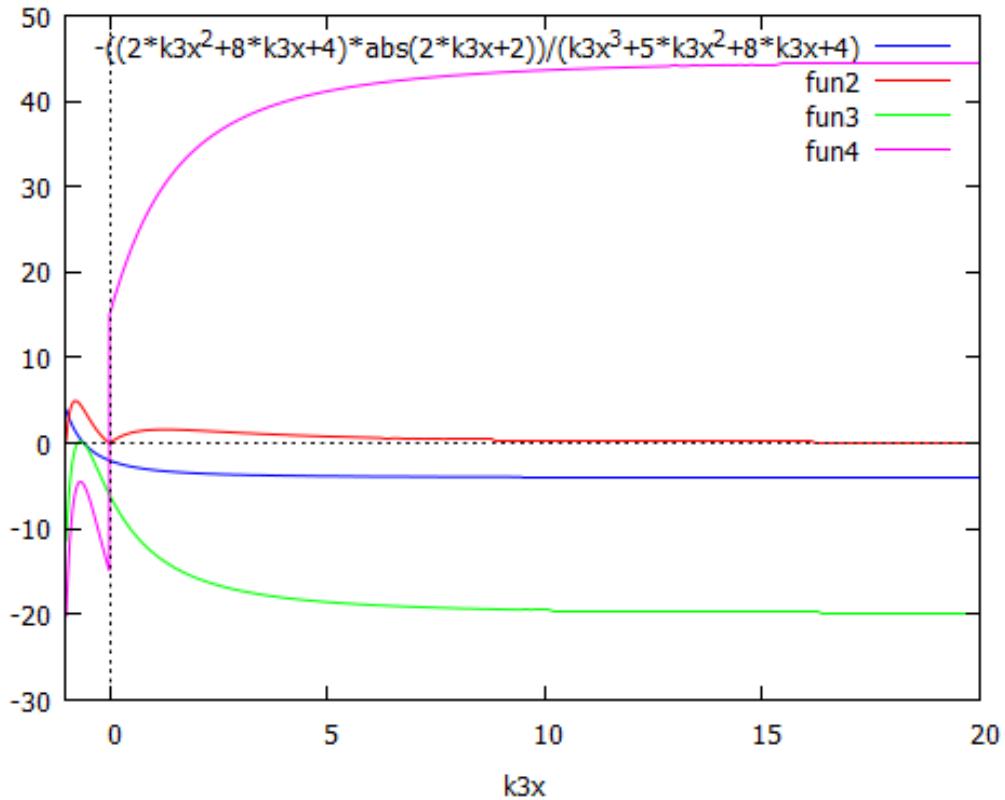
$$\rightarrow \{ -((2 \cdot k3x^2 + 8 \cdot k3x + 4) \cdot \text{abs}(2 \cdot k3x + 2)) / (k3x^3 + 5 \cdot k3x^2 + 8 \cdot k3x + 4), ((32 \cdot k3x + 32) \cdot \text{abs}(k3x) \cdot \text{abs}(2 \cdot k3x + 2)) / ((k3x^4 + 8 \cdot k3x^3 + 24 \cdot k3x^2 + 32 \cdot k3x + 16) \cdot \text{abs}(k3x + 1)),$$

$$-((10 \cdot k3x^4 + 80 \cdot k3x^3 + 204 \cdot k3x^2 + 176 \cdot k3x + 48) \cdot \text{abs}(2 \cdot k3x + 2)) / (k3x^5 + 9 \cdot k3x^4 + 32 \cdot k3x^3 + 56 \cdot k3x^2 + 48 \cdot k3x + 16),$$

Idem,

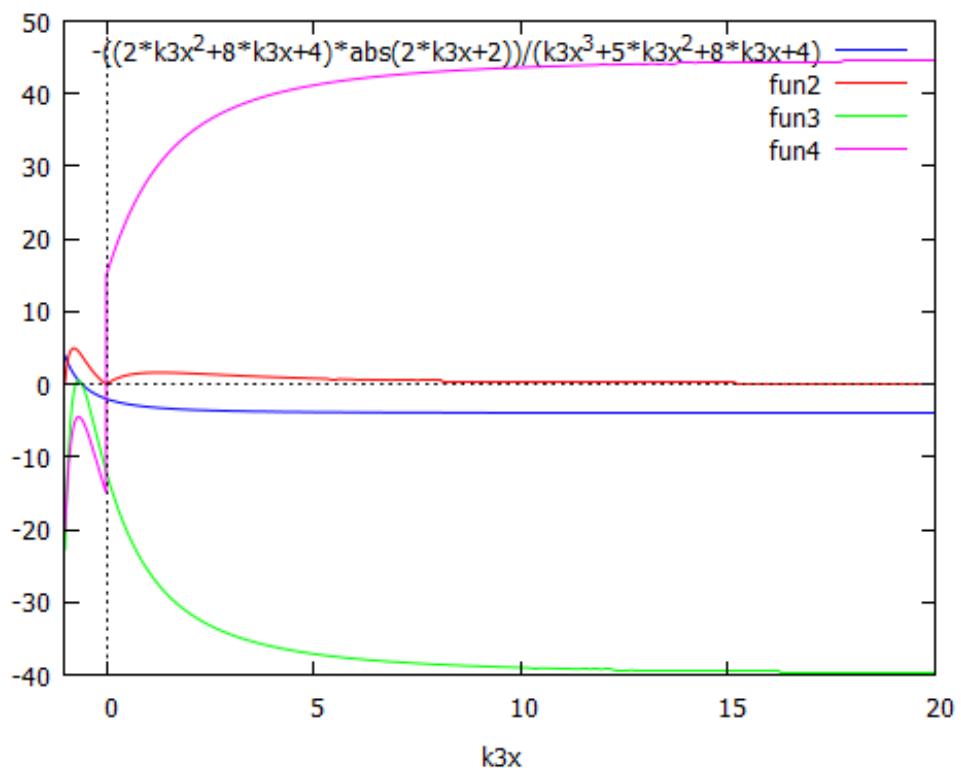
$((45 \cdot k3x^4 + 315 \cdot k3x^3 + 594 \cdot k3x^2 + 444 \cdot k3x + 120) \cdot \text{abs}(k3x)) / ((k3x^4 + 6 \cdot k3x^3 + 12 \cdot k3x^2 + 8 \cdot k3x) \cdot \text{abs}(k3x + 1)) \}$

## Plots

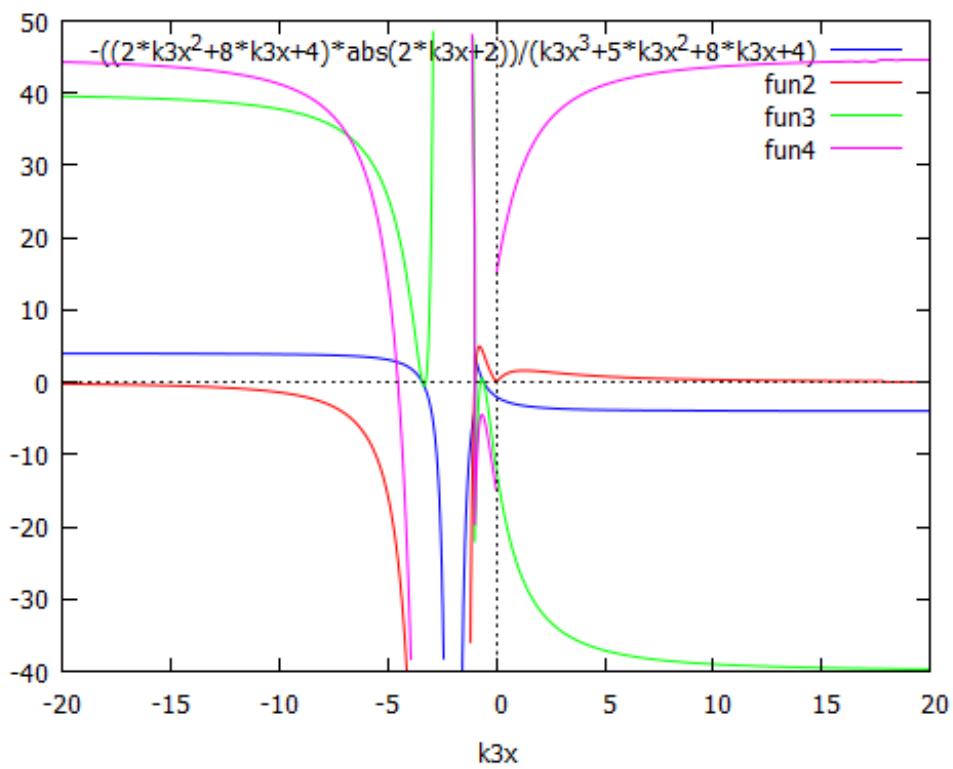


**Figure 7:** Plot2d  $\{ -((2 \cdot k3x^2 + 8 \cdot k3x + 4) \cdot \text{abs}(2 \cdot k3x + 2)) / (k3x^3 + 5 \cdot k3x^2 + 8 \cdot k3x + 4), ((32 \cdot k3x + 32) \cdot \text{abs}(k3x) \cdot \text{abs}(2 \cdot k3x + 2)) / ((k3x^4 + 8 \cdot k3x^3 + 24 \cdot k3x^2 + 32 \cdot k3x + 16) \cdot \text{abs}(k3x + 1)), -((10 \cdot k3x^4 + 80 \cdot k3x^3 + 204 \cdot k3x^2 + 176 \cdot k3x + 48) \cdot \text{abs}(2 \cdot k3x + 2)) / (k3x^5 + 9 \cdot k3x^4 + 32 \cdot k3x^3 + 56 \cdot k3x^2 + 48 \cdot k3x + 16), ((45 \cdot k3x^4 + 315 \cdot k3x^3 + 594 \cdot k3x^2 + 444 \cdot k3x + 120) \cdot \text{abs}(k3x)) / ((k3x^4 + 6 \cdot k3x^3 + 12 \cdot k3x^2 + 8 \cdot k3x) \cdot \text{abs}(k3x + 1)) \}, [k3x, -1, 20] \}$

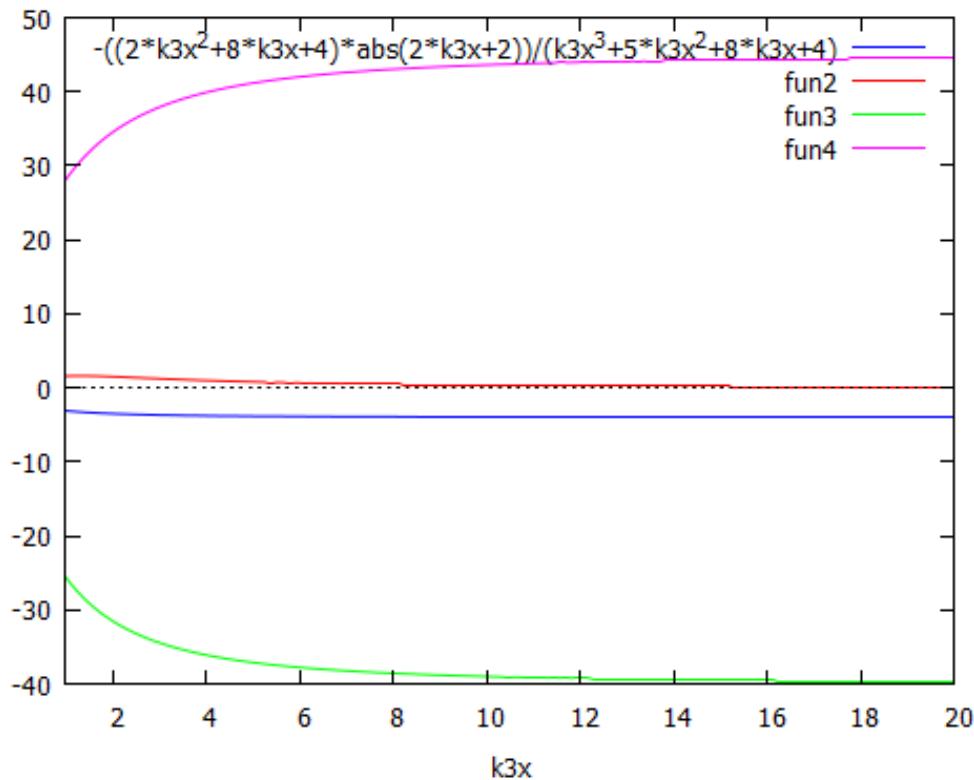
or



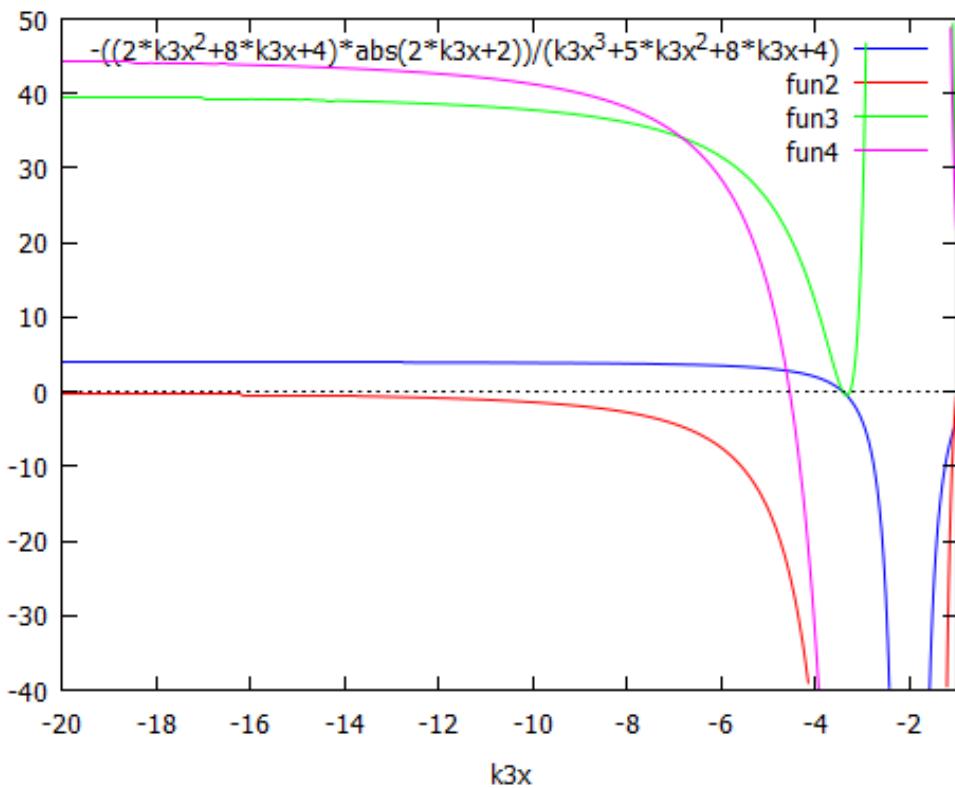
**Figure 8:** Plot2d  $\left[ \frac{-(2*k3x^2+8*k3x+4)*\text{abs}(2*k3x+2)}{(k3x^3+5*k3x^2+8*k3x+4)}, \frac{((32*k3x +32)*\text{abs}(k3x)*\text{abs}(2*k3x+2))}{((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*\text{abs}(k3x+1))}, 2*\left( \frac{(-((10*k3x^4+80*k3x^3+204*k3x^2+176*k3x+48)*\text{abs}(2*k3x+2))}{(k3x^5+9*k3x^4+32*k3x^3+56*k3x^2+48*k3x+16)} \right), \frac{((45*k3x^4+315*k3x^3+594*k3x^2+444*k3x+120)*\text{abs}(k3x))}{((k3x^4+6*k3x^3+12*k3x^2+8*k3x)*\text{abs}(k3x+1))} \right], [k3x, -1, 20]\$$



**Figure 9:** Plot2d  $\left[ \frac{-(2*k3x^2+8*k3x+4)*\text{abs}(2*k3x+2)}{(k3x^3+5*k3x^2+8*k3x+4)}, \frac{((32*k3x +32)*\text{abs}(k3x)*\text{abs}(2*k3x+2))}{((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*\text{abs}(k3x+1))}, 2*\left( \frac{(-((10*k3x^4+80*k3x^3+204*k3x^2+176*k3x+48)*\text{abs}(2*k3x+2))}{(k3x^5+9*k3x^4+32*k3x^3+56*k3x^2+48*k3x+16)} \right), \frac{((45*k3x^4+315*k3x^3+594*k3x^2+444*k3x+120)*\text{abs}(k3x))}{((k3x^4+6*k3x^3+12*k3x^2+8*k3x)*\text{abs}(k3x+1))} \right], [k3x, -20, 20], [y, -40, 50]\$$



**Figure 10:** Plot2d ([ $-((2*k3x^2+8*k3x+4)*abs(2*k3x+2))/(k3x^3+5*k3x^2+8*k3x+4)$ ,  $((32*k3x +32)*abs(k3x)*abs(2*k3x+2))/((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*abs(k3x+1))$ ,  $2*(- ((10*k3x^4+80*k3x^3+204*k3x^2+176*k3x+48)*abs(2*k3x+2))/(k3x^5+9*k3x^4+32*k3x^3+56*k3x^2+48*k3x+16))$ ,  $((45*k3x^4+315*k3x^3+594*k3x^2+444*k3x+120)*abs(k3x))/((k3x^4+6*k3x^3+12*k3x^2+8*k3x)*abs(k3x+1))]$ ], [k3x, 1, 20], [y, -40, 50])\$



**Figure 11:** Plot2d ([ $-((2*k3x^2+8*k3x+4)*abs(2*k3x+2))/(k3x^3+5*k3x^2+8*k3x+4)$ ,  $((32*k3x +32)*abs(k3x)*abs(2*k3x+2))/((k3x^4+8*k3x^3+24*k3x^2+32*k3x+16)*abs(k3x+1))$ ,  $2*(- ((10*k3x^4+80*k3x^3+204*k3x^2+176*k3x+48)*abs(2*k3x+2))/(k3x^5+9*k3x^4+32*k3x^3+56*k3x^2+48*k3x+16))$ ,  $((45*k3x^4+315*k3x^3+594*k3x^2+444*k3x+120)*abs(k3x))/((k3x^4+6*k3x^3+12*k3x^2+8*k3x)*abs(k3x+1))]$ ], [k3x, -20, -1], [y, -40, 50])\$

Obtaining of an algorithm for the more massive dark energy's massive boson and the distance at which the effects of dark energy begin. A quantum multi-entanglement system due to  $\{\Delta k_3 = dk_3d \text{ or } \Delta k_3 = dk_3n\} \neq 0$  allowing both a tendency towards the idea of a single time and the fact of a multi dilation of time.

### Constants Multi-Parts Effective of Things

$$(1bis) dE_{k3} = 4.\sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2.k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2}))} \quad (4dprocess)$$

$$\rightarrow f0.d(dE[k3])/dk3=dE[k3] \rightarrow f0=2/(sqrt(2*k3+2)*(4-8/(2*k3+2))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))$$

then  
 $f1.d(f0.d(dE[k3])/dk3)/dk3 = dE[k3] \rightarrow f1 = (4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2))))/(d(f0*d(dE[k3])/dk3)/dk3)$

$$f1=(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2))))/(diff((2/(sqrt(2*k3+2)*(4-8/(2*k3+2))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))))*diff((4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2))))),k3,1),k3,1))$$

$$f1 = -(4*k3^2+4*k3)/(k3+2), \text{ and } dE[k3] = f1*(d(f0)/dk3)*d(dE[k3])/dk3 + f1*f0*d^2(dE[k3])/dk3^2,$$

### Parts

$$f1*(d(f0)/dk3)*d(dE[k3])/dk3 + f1*f0*d^2(dE[k3])/dk3^2 = -(sqrt(2*k3+2)*(2^(11/4)*gM*k3^2+2^(19/4)*gM*k3+2^(15/4)*gM))/((k3^3+4*k3^2+4*k3)*sqrt((k3+1)/(k3*sqrt(2*k3+2)))) + (5*2^(3/4)*gM*k3^3+25*2^(3/4)*gM*k3^2+2^(23/4)*gM*k3+3*2^(11/4)*gM)/((k3^4+4*k3^3+4*k3^2)*((k3+1)/(k3*sqrt(2*k3+2))))^(3/2)),$$

$$[dE[k3] \rightarrow -sqrt(2*k3+2)*(2^(11/4)*gM*k3^2+2^(19/4)*gM*k3+2^(15/4)*gM)/((k3^3+4*k3^2+4*k3)*sqrt((k3+1)/(k3*sqrt(2*k3+2)))),k3) + (5*2^(3/4)*gM*k3^3+25*2^(3/4)*gM*k3^2+2^(23/4)*gM*k3+3*2^(11/4)*gM)/((k3^4+4*k3^3+4*k3^2)*((k3+1)/(k3*sqrt(2*k3+2))))^(3/2)).$$

$$f2.d(f1.d(f0.d(dE[k3])/dk3)/dk3)/dk3 = dE[k3] \rightarrow f2 = (4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2)))) / (d(f1*d(f0*d(dE[k3])/dk3)/dk3)/dk3)$$

$$f2=(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2))))/((((-4*k3^2)-4*k3)*((3*2^(3/4)*abs(gM)*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))^2)/(sqrt(2*k3+2)*(4-8/(2*k3+2))*((1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(5/2))+((3*2^(11/4)*abs(gM))/((2*k3+2)^(5/2)*(4-8/(2*k3+2)))*sqrt(1/(sqrt(2*k3+2)*(48/(2*k3+2)))))+(3*2^(31/4)*abs(gM))/((2*k3+2)^(7/2)*(4-8/(2*k3+2))^2)*sqrt(1/(sqrt(2*k3+2)*(4-8/(2*k3+2)))))+(2^(47/4)*abs(gM)/((2*k3+2)^(9/2)*(4-8/(2*k3+2))^3)*sqrt(1/(sqrt(2*k3+2)*(4-8/(2*k3+2)))))+(2^(11/4)*abs(gM)*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))/((2*k3+2)^(3/2)*(4-8/(2*k3+2))*((1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(3/2))+((2^(27/4)*abs(gM)*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)*((1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(3/2))-((2^(7/4)*abs(gM)*((3/((2*k3+2)^(5/2)*(4-8/(2*k3+2))))+96/((2*k3+2)^(7/2)*(4-8/(2*k3+2))^2)+512/((2*k3+2)^(9/2)*(4-8/(2*k3+2))^3)))/((sqrt(2*k3+2)*(48/(2*k3+2)))*(1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(3/2)))/(k3+2)+(((-8*k3)-4)*((-2^(11/4)*abs(gM))/((2*k3+2)^(3/2)*(4-8/(2*k3+2)))*sqrt(1/(sqrt(2*k3+2)*(4-8/(2*k3+2)))))-(2^(27/4)*abs(gM))/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)*sqrt(1/(sqrt(2*k3+2)*(4-8/(2*k3+2)))))-(2^(7/4)*abs(gM)*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))/((sqrt(2*k3+2)*(4-8/(2*k3+2)))*(1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(3/2)))/(k3+2)-((-4*k3^2)-4*k3)*((-2^(11/4)*abs(gM))/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-(2^(27/4)*abs(gM))/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)*sqrt(1/(sqrt(2*k3+2)*(4-8/(2*k3+2)))))-(2^(7/4)*abs(gM)*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))/((sqrt(2*k3+2)*(4-8/(2*k3+2)))*(1/(sqrt(2*k3+2)*(4-8/(2*k3+2))))^(3/2)))/(k3+2)^2))$$

$$f2 = -(4*k3^2+4*k3)/(k3+2)= f1.$$

### 1.3. Parts

$$f2.d(f1.d(f0.d(dE[k3])/dk3)/dk3)/dk3=f2.d(f1.{(d(f0)/dk3)*d(dE[k3])/dk3 + f0*d^2(dE[k3])/dk3^2})/dk3$$

$$f2.(d(f1.\{(d(f0)/dk3)*d(dE[k3])/dk3 + f0*d^2(dE[k3])/dk3^2\}/dk3) = f2.((d(f1)/dk3)*\{(d(f0)/dk3)* d(dE[k3])/dk3 + f0*d^2(dE[k3])/dk3^2\} + f1*\{d^2(f0)/dk3^2*d(dE[k3])/dk3 + (d^2(dE[k3])/dk3^2)^*(d(f0)/dk3)\} + d(f0)/dk3*d^2(dE[k3])/dk3^2 + (d^3(dE[k3])/dk3^3)^*f0\}) = \{f2.(d(f1)/dk3)*(d(f0)/dk3)* d(dE[k3])/dk3 + f2.(d(f1)/dk3)*f0*d^2(dE[k3])/dk3^2 + f2.f1*d^2(f0)/dk3^2*d(dE[k3])/dk3 + f2.f1*(d^2(dE[k3])/dk3^2)^*(d(f0)/dk3) + f2.f1*d(f0)/dk3*d^2(dE[k3])/dk3^2 + f2.f1*(d^3(dE[k3])/dk3^3)^*f0\};$$

$$\{(-(4*k3^2+4*k3)/(k3+2))^*(diff((-4*k3^2+4*k3)/(k3+2)),k3,1))^*(diff((2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))),k3,1))^*(diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,1))$$

$$+(-(4*k3^2+4*k3)/(k3+2))^*(diff((-4*k3^2+4*k3)/(k3+2)),k3,1))^*(2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2)))^*(diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,2))$$

$$+(-(4*k3^2+4*k3)/(k3+2))^*(-(4*k3^2+4*k3)/(k3+2))^*diff((2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))),k3,2)^*(diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,1))$$

$$+(-(4*k3^2+4*k3)/(k3+2))^*(-(4*k3^2+4*k3)/(k3+2))^*((diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,2))^*(diff((2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))),k3,1))$$

$$+(-(4*k3^2+4*k3)/(k3+2))^*(-(4*k3^2+4*k3)/(k3+2))^*diff((2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))),k3,2)^*(diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,1))$$

$$+(-(4*k3^2+4*k3)/(k3+2))^*(-(4*k3^2+4*k3)/(k3+2))^*((diff(4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3)))^(1/2)/(-2^3/(2+2*k3)+2^2))),k3,3))^*(2/(sqrt(2*k3+2)*(4-8/(2*k3+2)))*((-1/((2*k3+2)^(3/2)*(4-8/(2*k3+2))))-16/((2*k3+2)^(5/2)*(4-8/(2*k3+2))^2))))\}$$

$$(2) \quad \left\{ -\frac{(2^{(11/4)}.gM.k3^3+5.2^{(11/4)}.gM.k3^2+3.2^{(15/4)}.gM.k3+2^{(15/4)}.gM)}{((k3^4+4.k3^3+4.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})} \right.$$

$$+\frac{(\sqrt(2.k3+2).(2^{(27/4)}.gM.k3+2^{(27/4)}.gM))}{((k3^4+8.k3^3+24.k3^2+32.k3+16).\sqrt((k3+1)/(k3.\sqrt(2.k3+2))))}$$

$$-\frac{(5.2^{(11/4)}.gM.k3^5+45.2^{(11/4)}.gM.k3^4+71.2^{(15/4)}.gM.k3^3+95.2^{(15/4)}.gM.k3^2+7.2^{(27/4)}.gM.k3+3.2^{(23/4)}.gM)}{((k3^6+8.k3^5+24.k3^4+32.k3^3+16.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})}$$

$$-\frac{(5.2^{(11/4)}.gM.k3^5+45.2^{(11/4)}.gM.k3^4+71.2^{(15/4)}.gM.k3^3+95.2^{(15/4)}.gM.k3^2+7.2^{(27/4)}.gM.k3+3.2^{(23/4)}.gM)}{((k3^6+8.k3^5+24.k3^4+32.k3^3+16.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})}$$

$$+\frac{(\sqrt(2.k3+2).(45.gM.k3^4+315.gM.k3^3+594.gM.k3^2+444.gM.k3+120.gM))}{((2^{(1/4)}.k3^6+3.2^{(5/4)}.k3^5+3.2^{(9/4)}.k3^4+2^{(13/4)}.k3^3).((k3+1)/(k3.\sqrt(2.k3+2)))^{(5/2)})}$$

},

$$(2-1) \quad \int dE_{k3} \longrightarrow = \int -\frac{(2^{(11/4)}.gM.k3^3+5.2^{(11/4)}.gM.k3^2+3.2^{(15/4)}.gM.k3+2^{(15/4)}.gM)}{((k3^4+4.k3^3+4.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})}$$

$$+ \int \frac{(\sqrt(2.k3+2).(2^{(27/4)}.gM.k3+2^{(27/4)}.gM))}{((k3^4+8.k3^3+24.k3^2+32.k3+16).\sqrt((k3+1)/(k3.\sqrt(2.k3+2))))}$$

$$+ \int -\frac{(5.2^{(11/4)}.gM.k3^5+45.2^{(11/4)}.gM.k3^4+71.2^{(15/4)}.gM.k3^3+95.2^{(15/4)}.gM.k3^2+7.2^{(27/4)}.gM.k3+3.2^{(23/4)}.gM)}{((k3^6+8.k3^5+24.k3^4+32.k3^3+16.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})}$$

$$+ \int -\frac{(5.2^{(11/4)}.gM.k3^5+45.2^{(11/4)}.gM.k3^4+71.2^{(15/4)}.gM.k3^3+95.2^{(15/4)}.gM.k3^2+7.2^{(27/4)}.gM.k3+3.2^{(23/4)}.gM)}{((k3^6+8.k3^5+24.k3^4+32.k3^3+16.k3^2).((k3+1)/(k3.\sqrt(2.k3+2)))^{(3/2)})}$$

$$+ \int \frac{(\sqrt(2.k3+2).(45.gM.k3^4+315.gM.k3^3+594.gM.k3^2+444.gM.k3+120.gM))}{((2^{(1/4)}.k3^6+3.2^{(5/4)}.k3^5+3.2^{(9/4)}.k3^4+2^{(13/4)}.k3^3).((k3+1)/(k3.\sqrt(2.k3+2)))^{(5/2)})}$$

With

$$f_0 = \frac{2}{\sqrt{2k_3+2}} \cdot \frac{(4-8/(2k_3+2)) \cdot ((-1/(2k_3+2)^{3/2}) \cdot (4-8/(2k_3+2))) - 16/(2k_3+2)^{5/2} \cdot (4-8/(2k_3+2)^2))}{((2k_3+2)^{5/2} \cdot (4-8/(2k_3+2)^2))}$$

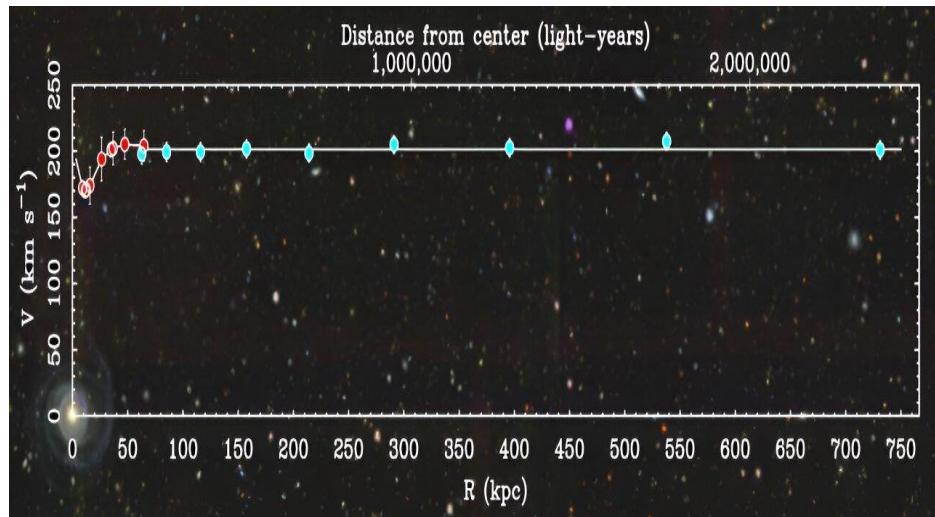
$$f_1 = -(4k_3^2 + 4k_3)/(k_3+2) = f_2 \quad d(f_0)/dk_3 = \frac{\text{diff}(2/\sqrt{2k_3+2} \cdot (4-8/(2k_3+2)) \cdot ((-1/(2k_3+2)^{3/2}) \cdot (4-8/(2k_3+2))) - 16/(2k_3+2)^{5/2} \cdot (4-8/(2k_3+2)^2)), k_3, 1)}$$

$$d(dE[k_3])/dk_3 = \text{diff}(4*\sqrt{gM^2*(-%i*(-2^3/(2+2*k_3))^{1/2}/(-2^3/(2+2*k_3)+2^2))), k_3, 1)$$

$$d^2(dE[k_3])/dk_3^2 = \text{diff}(4*\sqrt{gM^2*(-%i*(-2^3/(2+2*k_3))^{1/2}/(-2^3/(2+2*k_3)+2^2))), k_3, 2))$$

#### 1.4. Next Algorithm

(3) It makes it possible to obtain a permanent distribution of dark matter effects from the injunction  $\Sigma E_{\text{darkenergy}}/\Sigma E_{\text{darkmatter}} = 3$  [1].



**Figure 12:** The primary technique Mistele used in his research, gravitational lensing, is a phenomenon predicted by Einstein's theory of general relativity. As part of the research, Mistele plotted out what's called Tully–Fisher relation on a chart to highlight the empirical relationship between the visible mass of a galaxy and its rotation speed [1].

from math import\*

#An algorithm giving sets of massive bosons-dark energy: { $dE[k_3] = 2^{(7/4)} \cdot gM \cdot \sqrt{(k_3d+1)/(k_3d \cdot \sqrt{2k_3d+2})}$ },  $k_3d = 1+n \cdot dk_3d$ }

#and sets of massive bosons-dark matter: { $dE[k_3] = 2^{(7/4)} \cdot gM \cdot \sqrt{(k_3n+1)/(k_3n \cdot \sqrt{2k_3n+2})}$ },  $k_3n = 1+n \cdot dk_3n$ }

$gM = \sqrt{1393.6328858707575005182839547884}$

$\text{rangeX} = 100$

$dk_3n = 1.255314934818507 \cdot 10^{89}$

$dk_3d = 1.862840706286786 \cdot 10^{147}$

$#[a+b = -1.862840706286786 \cdot 10^{147} - \text{rangeX} \cdot dk_3n, a \cdot \text{rangeX} + b = 1.862840706286786 \cdot 10^{147} + \text{rangeX} \cdot dk_3n], [a, b]$

$a1 = (2 \cdot dk_3n \cdot \text{rangeX} + 3725681412573572053798732231988392423924366540993079083546201130940157386196842088959709555874110580129173407513251075528237648435976026867340673024) / (\text{rangeX} - 1)$

$b1 = -(dk_3n \cdot \text{rangeX}^{1/2} + (dk_3n + 1862840706286786026899366115994196211962183270496539541773100565470078693098421044479854777937055290064586703756625537764118824217988013433670336512) / (\text{rangeX} - 1)$

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```

#[a+b = -1.862840706286786*10^147-rangeX*dk3d, a*rangeX+b=1.862840706286786*10 ^147 +rangeX*dk3d],[a,b]

a2=(2*dk3d*rangeX+372568141257357205379873223198839242392436654099307908354620113094015738619684208895970955587
4110580129173407513251075528237648435976026867340673024)/(rangeX-1)

b2=-(dk3d*rangeX**2+(dk3d+1862840706286786026899366115994196211962183270496539541773100565470078693098421044479
854777937055290064586703756625537764118824217988013433670336512)*rangeX+186284070628678602689936611599419621196
2183270496539541773100565470078693098421044479854777937055290064586703756625537764118824217988013433670336512)/(rangeX-1)

for q in range (1,300 + 1):
Sidn = 0
Sidd = 0
tmax = 10*10***q

d0 =1.862840706286786*10***147
for t0 in range(1,10000 + 1) :
if d0 > 10**(-3)*1.862840706286786*10***147 :
Sidn = 0
Sidd = 0
k3n = 1.862840706286786*10***147
k3d = 1.862840706286786*10***147
for t in range(1, tmax + 1):
for k3n1i in range(1, rangeX + 1):
k3n1 = a1*k3n1i+b1
k3n2 = k3n-k3n1
for k3d1i in range(1, rangeX + 1):
k3d1 = a2*k3d1i+b2
k3d2 = k3d-k3d1
#[k3!= -1, k3!= -2, k3!= 0]

if k3n1*k3n2*k3d1*k3d2!= 0 and (k3n1!= -1 or k3n2!= -1 or k3d1!= -1 or k3d2!= -1) and (k3n1!= -2 or k3n2!= -2 or k3d1!= -2 or k3d2!= -2):

fiEk3n1 = -((2**((11/4)*gM*k3n1**2+2**((19/4)*gM*k3n1+2**((15/4)*gM)*sqrt(abs(k3n1)))*abs(2*k3n1+2)**(3/4))/((k3n1**3+4*k3n1**2+4*k3n1)*sqrt(abs(k3n1+1))))
#imfiEk3n1 = 0
fiEk3d1= -((2**((11/4)*gM*k3d1**2+2**((19/4)*gM*k3d1+2**((15/4)*gM)*sqrt(abs(k3d1)))*abs(2*k3d1+2)**(3/4))/((k3d1**3+4*k3d1**2+4*k3d1)*sqrt(abs(k3d1+1))))
#imfiEk3d1 = 0
fiEk3n2=((5*2**((3/4)*gM*k3n2**3+25*2**((3/4)*gM*k3n2**2+2**((23/4)*gM*k3n2+3*2**((11/4)*gM)*abs(k3n2)**(3/2)*abs(2*k3n2+2)**(3/4)))/((k3n2**4+4*k3n2**3+4*k3n2**2)*abs(k3n2+1)**(3/2)))
#imfiEk3n2 = 0
fiEk3d2=((5*2**((3/4)*gM*k3d2**3+25*2**((3/4)*gM*k3d2**2+2**((23/4)*gM*k3d2+3*2**((11/4)*gM)*abs(k3d2)**(3/2)*abs(2*k3d2+2)**(3/4)))/((k3d2**4+4*k3d2**3+4*k3d2**2)*abs(k3d2+1)**(3/2)))
#imfiEk3d2 = 0
#fiEk3n = 2**((7/4)*sqrt((k3n+1)/(k3n*sqrt(2*k3n+2))))
#fiEk3d = 2**((7/4)*sqrt((k3d+1)/(k3d*sqrt(2*k3d+2))))
Sidn = fiEk3n1*dk3n + fiEk3n2*dk3n + Sidd
Sidd = fiEk3d1*dk3d + fiEk3d2*dk3d + Sidd
k3n = k3n+dk3n
k3d = k3d+dk3d
if t == tmax or (Sidd/Sidn >= 3 and Sidd/Sidn < 4):
if (Sidd/Sidn >= 3 and Sidd/Sidn < 4):

```

---

```

k3n = k3n-dk3n
k3d = k3d-dk3d
#imdEd = 0
dEd = (2**((7/4)*gM*sqrt(abs(dk3d+1)))/(sqrt(abs(dk3d))*abs(2*dk3d+2)**(1/4)))
print("dk3n = ",dk3n, ", dk3d = ",dk3d, ", dEd = ",dEd," GeV, Sidd = ",Sidd," GeV, Sidn = ",Sidn," GeV}")
dk3d = dk3d-d0
d0 = d0/10
elif Sidd/Sidn < 3:
    k3n = k3n-dk3n
    k3d = k3d-dk3d0
    dk3d = dk3d+d0
elif Sidd/Sidn >= 4:
    k3n = k3n-dk3n
    k3d = k3d-dk3d
    dk3d : dk3d-d0/10

→ 10 random results obtained from this algorithm:
dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.79830744151244e-74 GeV, Sidd = 1.9655608964861628 e-36 GeV, Sidn = 1.720661362331221e-35 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 1.8997311639864714e-73 GeV, Sidd = 3.9470038906840624e-36 GeV, Sidn = 3.327536832849558e-35 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 1.292657988800866e-72 GeV, Sidd = 8.362666736674076e-36 GeV, Sidn = 6.946773655328476e-34 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 8.797703726238509e-72 GeV, Sidd = 1.7458341055671412e-35 GeV, Sidn = 1.4268487449721526e-33 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 5.978410274963025e-71 GeV, Sidd = 3.438907353997907e-35 GeV, Sidn = 2.769285652452027e-32 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 4.069281829039938e-70 GeV, Sidd = 6.825821750343634e-35 GeV, Sidn = 5.4426496841847744e-31 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.7694444026077187e-69 GeV, Sidd = 1.3386847680207826e-34 GeV, Sidn = 2.6347047724784477e-30 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 1.8854892370910166e-68 GeV, Sidd = 2.59334318002548e-34 GeV, Sidn = 1.275580526733872e-29 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 1.2820697992200913e-67 GeV, Sidd = 4.9859340816602605e-34 GeV, Sidn = 2.452573181646847e-28 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 8.721950193075937e-67 GeV, Sidd = 9.639921928740116e-34 GeV, Sidn = 4.682117092280432e-27 GeV}

```

Then in C++ :

```

#include <cmath>
#include <boost/multiprecision/cpp_int.hpp>
#include <iostream>
using namespace std;
int main() {
    double gM = sqrt(1393.6328858707575005182839547884);
    int rangeX = 100;
    double dk3n = 1.255314934818507*pow(10,89);
    double dk3d = 1.862840706286786*pow(10,147);

```

```

double a1= (2*dk3n*rangeX+37256814125735720537987322319883924239243665409930790835462011309401573861968420
88959709555874110580129173407513251075528237648435976026867340673024)/(ran geX-1);

doubleb 1=-(dk3n*rangeX*rangeX+(dk3n+186284070628678602689936611599419621196218327049653954177310056547007
86930984210444798547779370552 90064586703756625537764118824217988013433670336512)*rangeX+1862840706286786
026899366115994196211962183270496539541773100565470078693098 42104447985477793705529006458670375662553776
411882421798801343367033 6512)/(ran geX-1);

double a2= (2*dk3d*rangeX+37256814125735720537987322319883924239243665409930790835462011309401573861968420
88959709555874110580129173407513251075528237648435976026867340673024)/(ran geX-1);

double b2=-(dk3d*rangeX*rangeX+(dk3d+186284070628678602689936611599419621196218327049653954177310056547007
86930984 21044479854777937055290064586703756625537764118824217988013433670336512)*rangeX+1862840706286786
026899366115994196 2119621832704965395417731005654700786930984210444798547779370552900645867037566255377
6411882421798801343367033651 2)/(ran geX-1);

for (int q=1; q<=300; q++) {
    double Sidn = 0;
    double Sidd = 0;
    double tmax = 10*pow(10,q);
    double d0 = 1.862840706286786*pow(10,147);
    for (int t0=1; t0<=10000; t0++) {
        if (d0 > 10e-3*1.862840706286786*pow(10,147)) {
            Sidn = 0;
            Sidd = 0;
        }

        double k3n = 1.862840706286786*pow(10,147);
        double k3d = 1.862840706286786*pow(10,147);
        for (int t=1; t<=tmax; t++) {
            for (int k3n1i=1; k3n1i<=rangeX; k3n1i++) {
                double k3n1 = a1*k3n1i+b1;
                double k3n2 = k3n-k3n1;
                for (int k3d1i=1; k3d1i<=rangeX; k3d1i++) {
                    double k3d1 = a2*k3d1i+b2;
                    double k3d2 = k3d-k3d1;
                    if (k3n1*k3n2*k3d1*k3d2!= 0 && (k3n1!= -1 or k3n2!= -1 or k3d1!= -1 or k3d2!= -1) && (k3n1!= -2 or k3n2!= -2 or k3d1!= -2
                    or k3d2!= -2)) {

                        double fiEk3n1=-((pow(2,11/4)*gM*pow(k3n1,2)+pow(2,19/4)*gM*k3n1+pow(2,15/4)*gM)*sqrt(abs(k3n1))*pow(abs(2*k3n1+2),3/4))/(
                            (pow(k3n1,3)+4*pow(k3n1,2)+4*k3n1)*sqrt(abs(k3n1+1)));

                        double fiEk3d1=-((pow(2,11/4)*gM*pow(k3d1,2)+pow(2,19/4)*gM*k3d1+pow(2,15/4)*gM)*sqrt(abs(k3d1))*pow(abs(2*k3d1+2),3/4))/(
                            (pow(k3d1,3)+4*pow(k3d1,2)+4*k3d1)*sqrt(abs(k3d1+1))));

                        double fiEk3n2=((5*pow(2,3/4)*gM*pow(k3n2,3)+25*pow(2,3/4)*gM*pow(k3n2,2)+pow(2, 23/4)*gM*k3n2+3*pow(2,11/4)*g-
                            M)*pow(abs(k3n2),3/2)*pow(abs(2*k3n2+2),3/4))/((pow(k3n2,4)+4*pow(k3n2,3)+4*pow(k3n2,2))*pow(abs(k3n2+1),3/2));

                        double fiEk3d2=((5*pow(2,3/4)*gM*pow(k3d2,3)+25*pow(2,3/4)*gM*pow(k3d2,2)+pow(2,23/4)*gM*k3d2+3*pow(2,11/4)*g-
                            M)*pow(abs(k3d2),3/2)*pow(abs(2*k3d2+2),3/4))/((pow(k3d2,4)+4*pow(k3d2,3)+4*pow(k3d2,2))*pow(abs(k3d2+1),3/2));

                        Sidn = fiEk3n1*dk3n + fiEk3n2*dk3n + Sidn;
                        Sidd = fiEk3d1*dk3d + fiEk3d2*dk3d + Sidd;
                        k3n = k3n+dk3n;
                        k3d = k3d+dk3d;
                        if (t == tmax or (Sidd/Sidn >= 3 and Sidd/Sidn < 4)) {
                            if (Sidd/Sidn >= 3 and Sidd/Sidn < 4) {
                                k3n = k3n-dk3n;
                                k3d = k3d-dk3d;
                            }
                        }
                    }
                }
            }
        }
    }
}

```

```
return 0;  
}
```

→ ...

Or  
(3-1) Algorithm in Python  
from math import\*

#An algorithm giving sets of massive bosons-dark energy: {dE[k3] = 2^(7/4)\*gM\*sqrt((k3d+1)/(k 3d\*sqrt(2\*k3d+2))), k3d = 1+n. dk3d}

```
#and sets of massive bosons-dark matter: {dE[k3] = 2^(7/4)*gM*sqrt((k3n+1)/(k3n*sqrt(2*k3n + 2))), k3n = 1+n.dk3n}
gM = sart(1393.6328858707575005182839547884)
```

gM = sqrt(15)  
rangeX = 100

dk3n ≡ 1.255314934818507\*10\*\*89

$$dk3d \equiv 1.862840706286786 * 10^{**147}$$

$\text{dk3n} = -1.862840706286786^{*}10^{14}$  7+rangeX\*dk3n,  $a*rangeX+b = 1.862840706286786^{*}10^{14}$  14 7+rangeX\*dk3n, [a b]

```
a1=(2*dk3n^*rangeX+37256814125735720537987322319883924239243665409930790835462011309401573861968420889597095558  
74110580129173407513251075528237648435976026867340673024)/(rangeX-1)
```

```
b1=-(dk3n*rangeX**2+(dk3n+18628407062867860268993661159941962119621832704965395417731005654700786930984210
44479854777937055290064586703756625537764118824217988013433670336512)* rangeX+1862840706286786026899366115
9941962119621832704965395417731005654700786930984210444798547779370552900 64586703756625537764118824217988
013433670336512)/(rangeX-1)
```

```
#[a+b= -1.862840706286786*10^147-rangeX*X*dk3d, a*rangeX+b= 1.862840706286786*10^147 +rangeX*X*dk3d], [a,b]
```

a2=(2\*dk3d\*rangeX+37256814125735720537987322319883924239243665409930790835462011130940157386196842088959  
709555874110580129173407513251075528237648435976026867 340673024)/(rangeX-1)

---

```
b2=-(dk3d*rangeX**2+(dk3d+186284070628678602689936611599419621196218327049653954177310056547007869309842
1044479854777937055290064586703756625537764118824217988013433670336512)*rangeX+1862840706286786026899366
11599419621196218327049653954177310056547007869309842104447985477793705529006458670375662553776411882421
7988013433670336512)/(rangeX-1)
```

```
for q in range (1,300 + 1):
```

```
    Sidn = 0
```

```
    Sidd = 0
```

```
    tmax = 10*10**q
```

```
    d0 = 1.862840706286786*10**147
```

```
    for t0 in range(1,10000 + 1):
```

```
        if d0 > 10**(-3)*1.862840706286786*10**147:
```

```
            Sidn = 0
```

```
            Sidd = 0
```

```
            k3n = 1.862840706286786*10**147
```

```
            k3d = 1.862840706286786*10**147
```

```
            for t in range(1, tmax + 1):
```

```
                for k3n1i in range(1, rangeX + 1):
```

```
                    k3n1 = a1*k3n1i+b1
```

```
                    for k3n2i in range(1, rangeX + 1):
```

```
                        k3n2 = a1*k3n2i+b1
```

```
                        for k3n3i in range(1, rangeX + 1):
```

```
                            k3n3 = a1*k3n3i+b1
```

```
                            for k3n4i in range(1, rangeX + 1):
```

```
                                k3n4 = a1*k3n4i+b1
```

```
                                k3n5 = k3n-(k3n1+k3n2+k3n3+k3n4)
```

```
                                for k3d1i in range(1, rangeX + 1):
```

```
                                    k3d1 = a2*k3d1i+b2
```

```
                                    for k3d2i in range(1, rangeX + 1):
```

```
                                        k3d2 = a2*k3d2i+b2
```

```
                                        for k3d3i in range(1, rangeX + 1):
```

```
                                            k3d3 = a2*k3d3i+b2
```

```
                                            for k3d4i in range(1, rangeX + 1):
```

```
                                                k3d4 = a2*k3d4i+b2
```

```
                                                k3d5 = k3d-(k3d1+k3d2+k3d3+k3d4)
```

```
##[k3!= -1, k3!= -2, k3!= 0]
```

```
if k3n1*k3n2*k3n3*k3n4*k3n5*k3d1*k3d2*k3d3*k3d4*k3d5!= 0 and (k3n1!= -1 or k3n2!= -1 or k3n3!= -1 or k3n4!= -1 or
k3n5!= -1 or k3d1!= -1 or k3d2!= -1 or k3d3!= -1 or k3d4!= -1 or k3d5!= -1) and (k3n1!= -2 or k3n2!= -2 or k3n3!= -2 or k3n4!=
-2 or k3n5!= -2 or k3d1!= -2 or k3d2!= -2 or k3d3!= -2 or k3d4!= -2 or k3d5!= -2):
```

```
fiEk3n1= -(2**((11/4)*gM*k3n1**3+5*2**((11/4)*gM*k3n1**2+3*2**((15/4)*gM*k3n1+2**((1 5/4)*gM)*abs(k3n1)**(3/2)*abs
(2*k3n1+2)**(3/4))/((k3n1**4+4*k3n1**3+4*k3n1**2)*abs(k3n1+1)**(3/2)))
```

```
#imfiEk3n1 = 0
```

```
fiEk3n2= ((2**((27/4)*gM*k3n2+2**((27/4)*gM)*sqrt(abs(k3n2)))*abs(2*k3n2+2)**(3/4))/((k3n2 **4+8*k3n2**3+24*k3n2**2+
32*k3n2+ 16)*sqrt(abs(k3n2+1)))
```

```
#imfiEk3n2 = 0
```

```
fiEk3n3=-(5*2**((11/4)*gM*k3n3**5+45*2**((11/4)*gM*k3n3**4+71*2**((15/4)*gM*k3n3**3+95*2**((15/4)*gM*k3n3**2+7
*2**((27/4)*gM*k3n3+3*2**((23/4)*gM)*abs(k3n3)**(3/2)*abs(2*k3n3+2)**(3/4))/((k3n3**6+8*k3n3**5+24*k3n3**4+32*k3
n3**3+16*k3n3**2)*abs(k3n3+1)**(3/2)))
```

```
#imfiEk3n3 = 0
```

```
fiEk3n4=-(5*2**((11/4)*gM*k3n4**5+45*2**((11/4)*gM*k3n4**4+71*2**((15/4)*gM*k3n4**3+95*2**((15/4)*gM*k3n4**2+7*2**((27/4)*gM*k
3n4+3*2**((23/4)*gM)*abs(k3n4)**(3/2)*abs(2*k3n4+2)**(3/4))/((k3n4**6+8*k3n4**5+24*k3n4**4+32*k3n4**3+16*k3n4**2)*abs(k3n4+1)**(3/2)))
```

---

```

#imfiEk3n4 = 0
fiEk3n5= (k3n5**2*(45*gM*k3n5**4+315*gM*k3n5**3+594*gM*k3n5**2+444*gM*k3n5+ 120*gM)*sqrt(abs(k3n5))*abs(2*k3n5+2)**(7/4))/((k3n5+1)**2*(2**((1/4)*k3n5**6+3*2**((5/4)*k3n5**5+3*2**((9/4)*k3n5**4+2**((13/4)*k3n5**3)*sqrt(abs(k3n5+1)))))

#imfiEk3n5] = 0
fiEk3d1 = -((2**((11/4)*gM*k3d1**3+5*2**((11/4)*gM*k3d1**2+3*2**((15/4)*gM*k3d1+2**((15/4)*gM)*abs(k3d1)**(3/2)*abs(2*k3d1+2)**(3/4)))/((k3d1**4+4*k3d1**3+4*k3d1**2)*abs(k3d1+1)**(3/2)))

#imfiEk3d1 = 0
fiEk3d2 = ((2**((27/4)*gM*k3d2+2**((27/4)*gM)*sqrt(abs(k3d2))*abs(2*k3d2+2)**(3/4))/((k3d2**4+8*k3d2**3+24*k3d2**2+32*k3d2+16)*sqrt(abs(k3d2+1)))) 

#imfiEk3d2 = 0
fiEk3d3= -((5*2**((11/4)*gM*k3d3**5+45*2**((11/4)*gM*k3d3**4+71*2**((15/4)*gM*k3d3**3+95*2**((15/4)*gM*k3d3**2+7*2**((27/4)*gM*k3d3+3*2**((23/4)*gM)*abs(k3d3)**(3/2)*abs(2*k3d3+2)**(3/4)))/((k3d3**6+8*k3d3**5+24*k3d3**4+32*k3d3**3+16*k3d3**2)*abs(k3d3+1)**(3/2)))

#imfiEk3d3 = 0
fiEk3d4= -((5*2**((11/4)*gM*k3d4**5+45*2**((11/4)*gM*k3d4**4+71*2**((15/4)*gM*k3d4**3+95*2**((15/4)*gM*k3d4**2+7*2**((27/4)*gM*k3d4+3*2**((23/4)*gM)*abs(k3d4)**(3/2)*abs(2*k3d4+2)**(3/4)))/((k3d4**6+8*k3d4**5+24*k3d4**4+32*k3d4**3+16*k3d4**2)*abs(k3d4+1)**(3/2)))

#imfiEk3d4 = 0
fiEk3d5 = (k3d5**2*(45*gM*k3d5**4+315*gM*k3d5**3+594*gM*k3d5**2+444*gM*k3d5+120*gM)*sqrt(abs(k3d5))*abs(2*k3d5+2)**(7/4))/((k3d5+1)**2*(2**((1/4)*k3d5**6+3*2**((5/4)*k3d5**5+3*2**((9/4)*k3d5**4+2**((13/4)*k3d5**3)*sqrt(abs(k3d5+1)))))

#imfiEk3d5] = 0

#fiEk3n = 2**((7/4)*sqrt((k3n+1)/(k3n*sqrt(2*k3n+2))))
#fiEk3d = 2**((7/4)*sqrt((k3d+1)/(k3d*sqrt(2*k3d+2))))
Sidn = fiEk3n1*dk3n + fiEk3n2*dk3n + fiEk3n3*dk3n + fiEk3n4*dk3n + fiEk3n5*dk3n + Sidn
Sidd = fiEk3d1*dk3d + fiEk3d2*dk3d + fiEk3d3*dk3d + fiEk3d4*dk3d + fiEk3d5*dk3d + Sidd
k3n = k3n+dk3n
k3d = k3d+dk3d
if t == tmax or (Sidd/Sidn >= 3 and Sidd/Sidn < 4) :
    if (Sidd/Sidn >= 3 and Sidd/Sidn < 4) :
        k3n = k3n-dk3n
        k3d = k3d-dk3d
        #imdEd = 0
        dEd = (2**((7/4)*gM*sqrt(abs(dk3d+1)))/(sqrt(abs(dk3d))*abs(2*dk3d+2)**(1/4)))
        print("dk3n =", dk3n, ", dk3d =", dk3d, ", dEd =", dEd, " GeV, Sidd =", Sidd, " GeV, Sidn =", Sidn, " GeV")
        dk3d = dk3d-d0
        d0 = d0/10
    elif Sidd/Sidn < 3 :
        k3n = k3n-dk3n
        k3d = k3d-dk3d
        dk3d = dk3d+d0
    elif Sidd/Sidn >= 4 :
        k3n = k3n-dk3n
        k3d = k3d-dk3d
        dk3d : dk3d-d0/10

```

→ 10 random results obtained from this algorithm:

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 34.00167505713088 GeV, Sidn = 91947574.94277224 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd =

---

33.230939375949144 GeV, Sidn = 90728907.96697694 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 33.678777500551045 GeV, Sidn = 91325416.35519207 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 34.849266349418905 GeV, Sidn = 93330984.8136157 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 33.89461233274664 GeV, Sidn = 91824290.75378305 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 33.244760246712135 GeV, Sidn = 90750340.43227911 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 34.00659639485112 GeV, Sidn = 91956656.87543966 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 34.846724496494086 GeV, Sidn = 93324629.89333412 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 34.93276333543492 GeV, Sidn = 93587080.2677182 GeV}

dk3n = 1.255314934818507e+89, {dk3d = 1.862840706286786e+147, dEd = 2.206294095250117 e-70 GeV, Sidd = 33.881464159185175 GeV, Sidn = 91736474.225333 GeV}

#### 1.4.1. From Algorithm

##### Example 1:

C++ :

```
#include <iostream>
#include <cmath>
using namespace std;

int main() {
    int N = 1;
    int t = 1000;
    double dP1[1000 + 1] = {0};
    double dP2[1000 + 1] = {0};
    double dE[1000 + 1] = {0};
    double S[1000 + 1] = {0};
    double gM = sqrt(1393.6328858707575005182839547884);

    for (int k3 = -t; k3 <= t; k3++) {
        if (k3 != 0 && k3 != -1 && k3 != -2) {
            dP1[k3] = -((pow(2, (11.0 / 4.0)) * gM * pow(k3, 2) + pow(2, (19.0 / 4.0)) * gM * k3 + pow(2, (15.0 / 4.0)) * gM) * sqrt(abs(k3)) * pow(abs(2 * k3 + 2), (3.0 / 4.0))) / ((pow(k3, 3) + 4 * pow(k3, 2) + 4 * k3) * sqrt(abs(k3 + 1)));
            dP2[k3] = ((5 * pow(2, (3.0 / 4.0)) * gM * pow(k3, 3) + 25 * pow(2, (3.0 / 4.0)) * gM * pow(k3, 2) + pow(2, (23.0 / 4.0)) * gM * k3 + 3 * pow(2, (11.0 / 4.0)) * gM) * pow(abs(k3), (3.0 / 2.0)) * pow(abs(2 * k3 + 2), (3.0 / 4.0))) / ((pow(k3, 4) + 4 * pow(k3, 3) + 4 * pow(k3, 2)) * pow(abs(k3 + 1), (3.0 / 2.0)));
            dE[k3] = (pow(2, (7.0 / 4.0)) * gM * sqrt(abs(k3 + 1))) / (sqrt(abs(k3)) * pow(abs(2 * k3 + 2), (1.0 / 4.0)));
        }
        if (k3 == t) {
            N = floor(dE[1] / dE[t]);
        }
    }
}
```

---

```

for (int l1 = 1; l1 <= t - 1; l1++) {
    cout << l1 << " > (" << dP1[l1] << " and " << dP2[l1] << ") GeV" << endl;
}

int l1 = t - 1 + 1;
for (int l2 = N; l2 >= l1 - 1; l2--) {
    for (int q1 = 1; q1 <= N; q1++) {
        for (int q2 = 1; q2 <= N; q2++) {
            if ((dP1[l1] + dP2[l1]) - (q1 * dP1[l2] + q2 * dP2[l2]) > 0 && (dP1[l1] + dP2[l1]) - (q1 * dP1[l2] + q2 * dP2[l2]) < (dP1[l1] + dP2[l1]) - (dP1[l1 + 1] + dP2[l1 + 1])) {
                cout << l1 << " > ~ {" << q1 << "+" << q2 << " } ." << l2 << " >" << endl;
                S[l1] = S[l1] + q1 + q2;
            }
        }
    }
}
else if (l2 == l1 - 1 && q1 == N && q2 == N) {
    cout << S[l1] << endl;
}
}
}
return 0;
}

→ 1 > (-390.654 and 516.221) GeV
2 > (-343.916 and 442.178) GeV
3 > (-317.264 and 403.478) GeV
4 > (-298.242 and 377.188) GeV
5 > (-283.553 and 357.457) GeV
6 > (-271.7 and 341.816) GeV
7 > (-261.845 and 328.964) GeV
8 > (-253.467 and 318.127) GeV
9 > (-246.218 and 308.807) GeV
10 > (-239.857 and 300.666) GeV
11 > (-234.211 and 293.465) GeV
12 > (-229.15 and 287.028) GeV
13 > (-224.575 and 281.223) GeV
14 > (-220.41 and 275.947) GeV
15 > (-216.595 and 271.121) GeV
16 > (-213.08 and 266.681) GeV
17 > (-209.826 and 262.575) GeV
18 > (-206.802 and 258.762) GeV
19 > (-203.979 and 255.206) GeV
20 > (-201.336 and 251.878) GeV
21 > (-198.852 and 248.754) GeV
22 > (-196.512 and 245.811) GeV
23 > (-194.301 and 243.033) GeV
24 > (-192.208 and 240.403) GeV
25 > (-190.221 and 237.908) GeV
26 > (-188.332 and 235.535) GeV
27 > (-186.532 and 233.276) GeV
28 > (-184.813 and 231.12) GeV
29 > (-183.171 and 229.059) GeV
30 > (-181.598 and 227.086) GeV
31 > (-180.089 and 225.194) GeV
32 > (-178.641 and 223.378) GeV
33 > (-177.248 and 221.633) GeV
34 > (-175.908 and 219.953) GeV
35 > (-174.617 and 218.335) GeV
36 > (-173.371 and 216.774) GeV

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37 > (-172.168 and 215.267) GeV  
38 > (-171.006 and 213.811) GeV  
39 > (-169.881 and 212.402) GeV  
40 > (-168.792 and 211.038) GeV  
41 > (-167.737 and 209.717) GeV  
42 > (-166.714 and 208.436) GeV  
43 > (-165.722 and 207.193) GeV  
44 > (-164.758 and 205.986) GeV  
45 > (-163.821 and 204.813) GeV  
46 > (-162.91 and 203.673) GeV  
47 > (-162.024 and 202.563) GeV  
48 > (-161.161 and 201.484) GeV  
49 > (-160.321 and 200.432) GeV  
50 > (-159.502 and 199.407) GeV  
51 > (-158.703 and 198.407) GeV  
52 > (-157.924 and 197.432) GeV  
53 > (-157.164 and 196.481) GeV  
54 > (-156.421 and 195.552) GeV  
55 > (-155.696 and 194.644) GeV  
56 > (-154.987 and 193.757) GeV  
57 > (-154.294 and 192.89) GeV  
58 > (-153.616 and 192.042) GeV  
59 > (-152.953 and 191.212) GeV  
60 > (-152.304 and 190.399) GeV  
61 > (-151.668 and 189.604) GeV  
62 > (-151.045 and 188.825) GeV  
63 > (-150.435 and 188.061) GeV  
64 > (-149.837 and 187.313) GeV  
65 > (-149.25 and 186.579) GeV  
66 > (-148.675 and 185.86) GeV  
67 > (-148.111 and 185.154) GeV  
68 > (-147.557 and 184.461) GeV  
69 > (-147.013 and 183.781) GeV  
70 > (-146.48 and 183.114) GeV  
71 > (-145.955 and 182.458) GeV  
72 > (-145.44 and 181.814) GeV  
73 > (-144.934 and 181.181) GeV  
74 > (-144.437 and 180.559) GeV  
75 > (-143.948 and 179.947) GeV  
76 > (-143.467 and 179.346) GeV  
77 > (-142.994 and 178.754) GeV  
78 > (-142.529 and 178.172) GeV  
79 > (-142.071 and 177.6) GeV  
80 > (-141.621 and 177.036) GeV  
81 > (-141.177 and 176.482) GeV  
82 > (-140.74 and 175.935) GeV  
83 > (-140.31 and 175.398) GeV  
84 > (-139.887 and 174.868) GeV  
85 > (-139.47 and 174.346) GeV  
86 > (-139.059 and 173.832) GeV  
87 > (-138.653 and 173.326) GeV  
88 > (-138.254 and 172.826) GeV  
89 > (-137.861 and 172.334) GeV  
90 > (-137.472 and 171.849) GeV  
91 > (-137.09 and 171.37) GeV  
92 > (-136.712 and 170.898) GeV  
93 > (-136.34 and 170.433) GeV  
94 > (-135.973 and 169.973) GeV

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95 > (-135.61 and 169.52) GeV  
96 > (-135.253 and 169.073) GeV  
97 > (-134.9 and 168.632) GeV  
98 > (-134.551 and 168.196) GeV  
99 > (-134.207 and 167.766) GeV  
100 > (-133.868 and 167.341) GeV  
101 > (-133.532 and 166.922) GeV  
102 > (-133.201 and 166.508) GeV  
103 > (-132.874 and 166.099) GeV  
104 > (-132.551 and 165.694) GeV  
105 > (-132.232 and 165.295) GeV  
106 > (-131.916 and 164.901) GeV  
107 > (-131.604 and 164.511) GeV  
108 > (-131.296 and 164.126) GeV  
109 > (-130.992 and 163.745) GeV  
110 > (-130.691 and 163.368) GeV  
111 > (-130.393 and 162.996) GeV  
112 > (-130.099 and 162.628) GeV  
113 > (-129.808 and 162.265) GeV  
114 > (-129.52 and 161.905) GeV  
115 > (-129.235 and 161.549) GeV  
116 > (-128.954 and 161.197) GeV  
117 > (-128.675 and 160.849) GeV  
118 > (-128.4 and 160.504) GeV  
119 > (-128.127 and 160.164) GeV  
120 > (-127.858 and 159.826) GeV  
121 > (-127.591 and 159.493) GeV  
122 > (-127.327 and 159.162) GeV  
123 > (-127.065 and 158.836) GeV  
124 > (-126.806 and 158.512) GeV  
125 > (-126.55 and 158.192) GeV  
126 > (-126.297 and 157.875) GeV  
127 > (-126.046 and 157.561) GeV  
128 > (-125.797 and 157.25) GeV  
129 > (-125.551 and 156.942) GeV  
130 > (-125.307 and 156.637) GeV  
131 > (-125.066 and 156.336) GeV  
132 > (-124.826 and 156.037) GeV  
133 > (-124.59 and 155.74) GeV  
134 > (-124.355 and 155.447) GeV  
135 > (-124.123 and 155.157) GeV  
136 > (-123.892 and 154.869) GeV  
137 > (-123.664 and 154.583) GeV  
138 > (-123.438 and 154.301) GeV  
139 > (-123.214 and 154.021) GeV  
140 > (-122.992 and 153.743) GeV  
141 > (-122.772 and 153.468) GeV  
142 > (-122.554 and 153.195) GeV  
143 > (-122.338 and 152.925) GeV  
144 > (-122.123 and 152.657) GeV  
145 > (-121.911 and 152.392) GeV  
146 > (-121.701 and 152.128) GeV  
147 > (-121.492 and 151.867) GeV  
148 > (-121.285 and 151.609) GeV  
149 > (-121.08 and 151.352) GeV  
150 > (-120.876 and 151.098) GeV  
151 > (-120.674 and 150.845) GeV  
152 > (-120.474 and 150.595) GeV

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153 > (-120.276 and 150.347) GeV  
154 > (-120.079 and 150.101) GeV  
155 > (-119.883 and 149.857) GeV  
156 > (-119.69 and 149.615) GeV  
157 > (-119.498 and 149.374) GeV  
158 > (-119.307 and 149.136) GeV  
159 > (-119.118 and 148.9) GeV  
160 > (-118.93 and 148.665) GeV  
161 > (-118.744 and 148.432) GeV  
162 > (-118.559 and 148.202) GeV  
163 > (-118.376 and 147.972) GeV  
164 > (-118.194 and 147.745) GeV  
165 > (-118.014 and 147.519) GeV  
166 > (-117.835 and 147.296) GeV  
167 > (-117.657 and 147.073) GeV  
168 > (-117.481 and 146.853) GeV  
169 > (-117.305 and 146.634) GeV  
170 > (-117.132 and 146.417) GeV  
171 > (-116.959 and 146.201) GeV  
172 > (-116.788 and 145.987) GeV  
173 > (-116.618 and 145.774) GeV  
174 > (-116.449 and 145.563) GeV  
175 > (-116.281 and 145.354) GeV  
176 > (-116.115 and 145.146) GeV  
177 > (-115.95 and 144.939) GeV  
178 > (-115.786 and 144.734) GeV  
179 > (-115.623 and 144.531) GeV  
180 > (-115.461 and 144.328) GeV  
181 > (-115.301 and 144.128) GeV  
182 > (-115.141 and 143.928) GeV  
183 > (-114.983 and 143.73) GeV  
184 > (-114.825 and 143.533) GeV  
185 > (-114.669 and 143.338) GeV  
186 > (-114.514 and 143.144) GeV  
187 > (-114.36 and 142.951) GeV  
188 > (-114.207 and 142.76) GeV  
189 > (-114.055 and 142.57) GeV  
190 > (-113.904 and 142.381) GeV  
191 > (-113.753 and 142.193) GeV  
192 > (-113.604 and 142.007) GeV  
193 > (-113.456 and 141.822) GeV  
194 > (-113.309 and 141.638) GeV  
195 > (-113.163 and 141.455) GeV  
196 > (-113.017 and 141.273) GeV  
197 > (-112.873 and 141.093) GeV  
198 > (-112.73 and 140.913) GeV  
199 > (-112.587 and 140.735) GeV  
200 > (-112.445 and 140.558) GeV  
201 > (-112.305 and 140.382) GeV  
202 > (-112.165 and 140.207) GeV  
203 > (-112.026 and 140.034) GeV  
204 > (-111.888 and 139.861) GeV  
205 > (-111.75 and 139.689) GeV  
206 > (-111.614 and 139.519) GeV  
207 > (-111.478 and 139.349) GeV  
208 > (-111.343 and 139.18) GeV  
209 > (-111.209 and 139.013) GeV  
210 > (-111.076 and 138.846) GeV

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211 > (-110.944 and 138.681) GeV  
212 > (-110.812 and 138.516) GeV  
213 > (-110.681 and 138.353) GeV  
214 > (-110.551 and 138.19) GeV  
215 > (-110.422 and 138.028) GeV  
216 > (-110.293 and 137.868) GeV  
217 > (-110.165 and 137.708) GeV  
218 > (-110.038 and 137.549) GeV  
219 > (-109.912 and 137.391) GeV  
220 > (-109.786 and 137.234) GeV  
221 > (-109.661 and 137.078) GeV  
222 > (-109.537 and 136.923) GeV  
223 > (-109.414 and 136.768) GeV  
224 > (-109.291 and 136.615) GeV  
225 > (-109.169 and 136.462) GeV  
226 > (-109.047 and 136.31) GeV  
227 > (-108.926 and 136.159) GeV  
228 > (-108.806 and 136.009) GeV  
229 > (-108.687 and 135.86) GeV  
230 > (-108.568 and 135.711) GeV  
231 > (-108.45 and 135.563) GeV  
232 > (-108.332 and 135.416) GeV  
233 > (-108.215 and 135.27) GeV  
234 > (-108.099 and 135.125) GeV  
235 > (-107.984 and 134.98) GeV  
236 > (-107.869 and 134.837) GeV  
237 > (-107.754 and 134.694) GeV  
238 > (-107.64 and 134.551) GeV  
239 > (-107.527 and 134.41) GeV  
240 > (-107.415 and 134.269) GeV  
241 > (-107.302 and 134.129) GeV  
242 > (-107.191 and 133.99) GeV  
243 > (-107.08 and 133.851) GeV  
244 > (-106.97 and 133.713) GeV  
245 > (-106.86 and 133.576) GeV  
246 > (-106.751 and 133.44) GeV  
247 > (-106.642 and 133.304) GeV  
248 > (-106.534 and 133.169) GeV  
249 > (-106.427 and 133.034) GeV  
250 > (-106.32 and 132.901) GeV  
251 > (-106.213 and 132.767) GeV  
252 > (-106.107 and 132.635) GeV  
253 > (-106.002 and 132.503) GeV  
254 > (-105.897 and 132.372) GeV  
255 > (-105.793 and 132.242) GeV  
256 > (-105.689 and 132.112) GeV  
257 > (-105.586 and 131.983) GeV  
258 > (-105.483 and 131.854) GeV  
259 > (-105.38 and 131.726) GeV  
260 > (-105.279 and 131.599) GeV  
261 > (-105.177 and 131.472) GeV  
262 > (-105.076 and 131.346) GeV  
263 > (-104.976 and 131.221) GeV  
264 > (-104.876 and 131.096) GeV  
265 > (-104.777 and 130.972) GeV  
266 > (-104.678 and 130.848) GeV  
267 > (-104.579 and 130.725) GeV  
268 > (-104.481 and 130.602) GeV

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269 > (-104.384 and 130.48) GeV  
270 > (-104.286 and 130.359) GeV  
271 > (-104.19 and 130.238) GeV  
272 > (-104.094 and 130.118) GeV  
273 > (-103.998 and 129.998) GeV  
274 > (-103.902 and 129.879) GeV  
275 > (-103.808 and 129.76) GeV  
276 > (-103.713 and 129.642) GeV  
277 > (-103.619 and 129.524) GeV  
278 > (-103.525 and 129.407) GeV  
279 > (-103.432 and 129.291) GeV  
280 > (-103.339 and 129.175) GeV  
281 > (-103.247 and 129.059) GeV  
282 > (-103.155 and 128.944) GeV  
283 > (-103.063 and 128.83) GeV  
284 > (-102.972 and 128.716) GeV  
285 > (-102.882 and 128.603) GeV  
286 > (-102.791 and 128.49) GeV  
287 > (-102.701 and 128.377) GeV  
288 > (-102.612 and 128.265) GeV  
289 > (-102.523 and 128.154) GeV  
290 > (-102.434 and 128.043) GeV  
291 > (-102.345 and 127.932) GeV  
292 > (-102.257 and 127.822) GeV  
293 > (-102.17 and 127.713) GeV  
294 > (-102.082 and 127.604) GeV  
295 > (-101.996 and 127.495) GeV  
296 > (-101.909 and 127.387) GeV  
297 > (-101.823 and 127.279) GeV  
298 > (-101.737 and 127.172) GeV  
299 > (-101.652 and 127.065) GeV  
300 > (-101.567 and 126.959) GeV  
301 > (-101.482 and 126.853) GeV  
302 > (-101.397 and 126.747) GeV  
303 > (-101.313 and 126.642) GeV  
304 > (-101.23 and 126.538) GeV  
305 > (-101.146 and 126.434) GeV  
306 > (-101.063 and 126.33) GeV  
307 > (-100.981 and 126.226) GeV  
308 > (-100.898 and 126.124) GeV  
309 > (-100.816 and 126.021) GeV  
310 > (-100.735 and 125.919) GeV  
311 > (-100.653 and 125.817) GeV  
312 > (-100.572 and 125.716) GeV  
313 > (-100.492 and 125.615) GeV  
314 > (-100.411 and 125.515) GeV  
315 > (-100.331 and 125.415) GeV  
316 > (-100.252 and 125.315) GeV  
317 > (-100.172 and 125.216) GeV  
318 > (-100.093 and 125.117) GeV  
319 > (-100.014 and 125.019) GeV  
320 > (-99.936 and 124.921) GeV  
321 > (-99.8579 and 124.823) GeV  
322 > (-99.78 and 124.726) GeV  
323 > (-99.7025 and 124.629) GeV  
324 > (-99.6252 and 124.532) GeV  
325 > (-99.5483 and 124.436) GeV  
326 > (-99.4716 and 124.34) GeV

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327 > (-99.3953 and 124.245) GeV  
328 > (-99.3192 and 124.149) GeV  
329 > (-99.2434 and 124.055) GeV  
330 > (-99.1679 and 123.96) GeV  
331 > (-99.0927 and 123.866) GeV  
332 > (-99.0178 and 123.773) GeV  
333 > (-98.9432 and 123.679) GeV  
334 > (-98.8688 and 123.586) GeV  
335 > (-98.7948 and 123.494) GeV  
336 > (-98.721 and 123.402) GeV  
337 > (-98.6474 and 123.31) GeV  
338 > (-98.5742 and 123.218) GeV  
339 > (-98.5012 and 123.127) GeV  
340 > (-98.4285 and 123.036) GeV  
341 > (-98.3561 and 122.945) GeV  
342 > (-98.2839 and 122.855) GeV  
343 > (-98.212 and 122.765) GeV  
344 > (-98.1403 and 122.676) GeV  
345 > (-98.0689 and 122.587) GeV  
346 > (-97.9978 and 122.498) GeV  
347 > (-97.9269 and 122.409) GeV  
348 > (-97.8563 and 122.321) GeV  
349 > (-97.7859 and 122.233) GeV  
350 > (-97.7158 and 122.145) GeV  
351 > (-97.646 and 122.058) GeV  
352 > (-97.5764 and 121.971) GeV  
353 > (-97.507 and 121.884) GeV  
354 > (-97.4379 and 121.798) GeV  
355 > (-97.369 and 121.712) GeV  
356 > (-97.3004 and 121.626) GeV  
357 > (-97.232 and 121.54) GeV  
358 > (-97.1638 and 121.455) GeV  
359 > (-97.0959 and 121.37) GeV  
360 > (-97.0282 and 121.286) GeV  
361 > (-96.9608 and 121.201) GeV  
362 > (-96.8936 and 121.117) GeV  
363 > (-96.8266 and 121.034) GeV  
364 > (-96.7599 and 120.95) GeV  
365 > (-96.6933 and 120.867) GeV  
366 > (-96.6271 and 120.784) GeV  
367 > (-96.561 and 120.702) GeV  
368 > (-96.4952 and 120.619) GeV  
369 > (-96.4295 and 120.537) GeV  
370 > (-96.3642 and 120.456) GeV  
371 > (-96.299 and 120.374) GeV  
372 > (-96.234 and 120.293) GeV  
373 > (-96.1693 and 120.212) GeV  
374 > (-96.1048 and 120.131) GeV  
375 > (-96.0405 and 120.051) GeV  
376 > (-95.9764 and 119.971) GeV  
377 > (-95.9125 and 119.891) GeV  
378 > (-95.8489 and 119.811) GeV  
379 > (-95.7854 and 119.732) GeV  
380 > (-95.7222 and 119.653) GeV  
381 > (-95.6592 and 119.574) GeV  
382 > (-95.5963 and 119.496) GeV  
383 > (-95.5337 and 119.417) GeV  
384 > (-95.4713 and 119.339) GeV

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385 > (-95.4091 and 119.262) GeV  
386 > (-95.3471 and 119.184) GeV  
387 > (-95.2853 and 119.107) GeV  
388 > (-95.2237 and 119.03) GeV  
389 > (-95.1623 and 118.953) GeV  
390 > (-95.1011 and 118.877) GeV  
391 > (-95.0401 and 118.8) GeV  
392 > (-94.9792 and 118.724) GeV  
393 > (-94.9186 and 118.649) GeV  
394 > (-94.8582 and 118.573) GeV  
395 > (-94.7979 and 118.498) GeV  
396 > (-94.7379 and 118.423) GeV  
397 > (-94.678 and 118.348) GeV  
398 > (-94.6184 and 118.273) GeV  
399 > (-94.5589 and 118.199) GeV  
400 > (-94.4996 and 118.125) GeV  
401 > (-94.4405 and 118.051) GeV  
402 > (-94.3815 and 117.977) GeV  
403 > (-94.3228 and 117.904) GeV  
404 > (-94.2642 and 117.831) GeV  
405 > (-94.2059 and 117.758) GeV  
406 > (-94.1477 and 117.685) GeV  
407 > (-94.0896 and 117.612) GeV  
408 > (-94.0318 and 117.54) GeV  
409 > (-93.9741 and 117.468) GeV  
410 > (-93.9166 and 117.396) GeV  
411 > (-93.8593 and 117.324) GeV  
412 > (-93.8022 and 117.253) GeV  
413 > (-93.7452 and 117.182) GeV  
414 > (-93.6884 and 117.111) GeV  
415 > (-93.6318 and 117.04) GeV  
416 > (-93.5754 and 116.969) GeV  
417 > (-93.5191 and 116.899) GeV  
418 > (-93.463 and 116.829) GeV  
419 > (-93.407 and 116.759) GeV  
420 > (-93.3513 and 116.689) GeV  
421 > (-93.2956 and 116.62) GeV  
422 > (-93.2402 and 116.551) GeV  
423 > (-93.1849 and 116.481) GeV  
424 > (-93.1298 and 116.413) GeV  
425 > (-93.0749 and 116.344) GeV  
426 > (-93.0201 and 116.275) GeV  
427 > (-92.9654 and 116.207) GeV  
428 > (-92.911 and 116.139) GeV  
429 > (-92.8566 and 116.071) GeV  
430 > (-92.8025 and 116.003) GeV  
431 > (-92.7485 and 115.936) GeV  
432 > (-92.6946 and 115.869) GeV  
433 > (-92.641 and 115.801) GeV  
434 > (-92.5874 and 115.735) GeV  
435 > (-92.5341 and 115.668) GeV  
436 > (-92.4808 and 115.601) GeV  
437 > (-92.4278 and 115.535) GeV  
438 > (-92.3749 and 115.469) GeV  
439 > (-92.3221 and 115.403) GeV  
440 > (-92.2695 and 115.337) GeV  
441 > (-92.217 and 115.271) GeV  
442 > (-92.1647 and 115.206) GeV

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443 > (-92.1125 and 115.141) GeV  
444 > (-92.0605 and 115.076) GeV  
445 > (-92.0086 and 115.011) GeV  
446 > (-91.9569 and 114.946) GeV  
447 > (-91.9053 and 114.882) GeV  
448 > (-91.8539 and 114.818) GeV  
449 > (-91.8026 and 114.753) GeV  
450 > (-91.7514 and 114.69) GeV  
451 > (-91.7004 and 114.626) GeV  
452 > (-91.6495 and 114.562) GeV  
453 > (-91.5988 and 114.499) GeV  
454 > (-91.5482 and 114.436) GeV  
455 > (-91.4978 and 114.372) GeV  
456 > (-91.4475 and 114.31) GeV  
457 > (-91.3973 and 114.247) GeV  
458 > (-91.3473 and 114.184) GeV  
459 > (-91.2974 and 114.122) GeV  
460 > (-91.2476 and 114.06) GeV  
461 > (-91.198 and 113.998) GeV  
462 > (-91.1485 and 113.936) GeV  
463 > (-91.0991 and 113.874) GeV  
464 > (-91.0499 and 113.813) GeV  
465 > (-91.0008 and 113.751) GeV  
466 > (-90.9518 and 113.69) GeV  
467 > (-90.903 and 113.629) GeV  
468 > (-90.8543 and 113.568) GeV  
469 > (-90.8057 and 113.507) GeV  
470 > (-90.7573 and 113.447) GeV  
471 > (-90.709 and 113.386) GeV  
472 > (-90.6608 and 113.326) GeV  
473 > (-90.6128 and 113.266) GeV  
474 > (-90.5648 and 113.206) GeV  
475 > (-90.517 and 113.146) GeV  
476 > (-90.4694 and 113.087) GeV  
477 > (-90.4218 and 113.027) GeV  
478 > (-90.3744 and 112.968) GeV  
479 > (-90.3271 and 112.909) GeV  
480 > (-90.2799 and 112.85) GeV  
481 > (-90.2329 and 112.791) GeV  
482 > (-90.1859 and 112.733) GeV  
483 > (-90.1391 and 112.674) GeV  
484 > (-90.0924 and 112.616) GeV  
485 > (-90.0459 and 112.558) GeV  
486 > (-89.9994 and 112.499) GeV  
487 > (-89.9531 and 112.442) GeV  
488 > (-89.9069 and 112.384) GeV  
489 > (-89.8608 and 112.326) GeV  
490 > (-89.8148 and 112.269) GeV  
491 > (-89.7689 and 112.211) GeV  
492 > (-89.7232 and 112.154) GeV  
493 > (-89.6776 and 112.097) GeV  
494 > (-89.6321 and 112.04) GeV  
495 > (-89.5867 and 111.984) GeV  
496 > (-89.5414 and 111.927) GeV  
497 > (-89.4962 and 111.87) GeV  
498 > (-89.4512 and 111.814) GeV  
499 > (-89.4063 and 111.758) GeV  
500 > (-89.3614 and 111.702) GeV

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501 > (-89.3167 and 111.646) GeV  
502 > (-89.2721 and 111.59) GeV  
503 > (-89.2276 and 111.535) GeV  
504 > (-89.1833 and 111.479) GeV  
505 > (-89.139 and 111.424) GeV  
506 > (-89.0948 and 111.369) GeV  
507 > (-89.0508 and 111.314) GeV  
508 > (-89.0068 and 111.259) GeV  
509 > (-88.963 and 111.204) GeV  
510 > (-88.9193 and 111.149) GeV  
511 > (-88.8757 and 111.095) GeV  
512 > (-88.8322 and 111.04) GeV  
513 > (-88.7888 and 110.986) GeV  
514 > (-88.7455 and 110.932) GeV  
515 > (-88.7023 and 110.878) GeV  
516 > (-88.6592 and 110.824) GeV  
517 > (-88.6162 and 110.77) GeV  
518 > (-88.5733 and 110.717) GeV  
519 > (-88.5305 and 110.663) GeV  
520 > (-88.4879 and 110.61) GeV  
521 > (-88.4453 and 110.557) GeV  
522 > (-88.4028 and 110.504) GeV  
523 > (-88.3605 and 110.451) GeV  
524 > (-88.3182 and 110.398) GeV  
525 > (-88.276 and 110.345) GeV  
526 > (-88.234 and 110.293) GeV  
527 > (-88.192 and 110.24) GeV  
528 > (-88.1501 and 110.188) GeV  
529 > (-88.1084 and 110.136) GeV  
530 > (-88.0667 and 110.084) GeV  
531 > (-88.0251 and 110.032) GeV  
532 > (-87.9837 and 109.98) GeV  
533 > (-87.9423 and 109.928) GeV  
534 > (-87.901 and 109.876) GeV  
535 > (-87.8599 and 109.825) GeV  
536 > (-87.8188 and 109.774) GeV  
537 > (-87.7778 and 109.722) GeV  
538 > (-87.7369 and 109.671) GeV  
539 > (-87.6961 and 109.62) GeV  
540 > (-87.6554 and 109.569) GeV  
541 > (-87.6148 and 109.519) GeV  
542 > (-87.5743 and 109.468) GeV  
543 > (-87.5339 and 109.417) GeV  
544 > (-87.4935 and 109.367) GeV  
545 > (-87.4533 and 109.317) GeV  
546 > (-87.4132 and 109.267) GeV  
547 > (-87.3731 and 109.217) GeV  
548 > (-87.3331 and 109.167) GeV  
549 > (-87.2933 and 109.117) GeV  
550 > (-87.2535 and 109.067) GeV  
551 > (-87.2138 and 109.017) GeV  
552 > (-87.1742 and 108.968) GeV  
553 > (-87.1347 and 108.919) GeV  
554 > (-87.0953 and 108.869) GeV  
555 > (-87.056 and 108.82) GeV  
556 > (-87.0167 and 108.771) GeV  
557 > (-86.9776 and 108.722) GeV  
558 > (-86.9385 and 108.673) GeV

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559 > (-86.8995 and 108.625) GeV  
560 > (-86.8607 and 108.576) GeV  
561 > (-86.8219 and 108.527) GeV  
562 > (-86.7831 and 108.479) GeV  
563 > (-86.7445 and 108.431) GeV  
564 > (-86.706 and 108.383) GeV  
565 > (-86.6675 and 108.335) GeV  
566 > (-86.6291 and 108.287) GeV  
567 > (-86.5909 and 108.239) GeV  
568 > (-86.5527 and 108.191) GeV  
569 > (-86.5145 and 108.143) GeV  
570 > (-86.4765 and 108.096) GeV  
571 > (-86.4386 and 108.048) GeV  
572 > (-86.4007 and 108.001) GeV  
573 > (-86.3629 and 107.954) GeV  
574 > (-86.3252 and 107.907) GeV  
575 > (-86.2876 and 107.86) GeV  
576 > (-86.25 and 107.813) GeV  
577 > (-86.2126 and 107.766) GeV  
578 > (-86.1752 and 107.719) GeV  
579 > (-86.1379 and 107.673) GeV  
580 > (-86.1007 and 107.626) GeV  
581 > (-86.0636 and 107.58) GeV  
582 > (-86.0265 and 107.533) GeV  
583 > (-85.9895 and 107.487) GeV  
584 > (-85.9526 and 107.441) GeV  
585 > (-85.9158 and 107.395) GeV  
586 > (-85.8791 and 107.349) GeV  
587 > (-85.8424 and 107.303) GeV  
588 > (-85.8058 and 107.257) GeV  
589 > (-85.7693 and 107.212) GeV  
590 > (-85.7329 and 107.166) GeV  
591 > (-85.6966 and 107.121) GeV  
592 > (-85.6603 and 107.075) GeV  
593 > (-85.6241 and 107.03) GeV  
594 > (-85.588 and 106.985) GeV  
595 > (-85.5519 and 106.94) GeV  
596 > (-85.516 and 106.895) GeV  
597 > (-85.4801 and 106.85) GeV  
598 > (-85.4443 and 106.805) GeV  
599 > (-85.4085 and 106.761) GeV  
600 > (-85.3728 and 106.716) GeV  
601 > (-85.3373 and 106.672) GeV  
602 > (-85.3017 and 106.627) GeV  
603 > (-85.2663 and 106.583) GeV  
604 > (-85.2309 and 106.539) GeV  
605 > (-85.1956 and 106.495) GeV  
606 > (-85.1604 and 106.451) GeV  
607 > (-85.1252 and 106.407) GeV  
608 > (-85.0902 and 106.363) GeV  
609 > (-85.0552 and 106.319) GeV  
610 > (-85.0202 and 106.275) GeV  
611 > (-84.9854 and 106.232) GeV  
612 > (-84.9506 and 106.188) GeV  
613 > (-84.9158 and 106.145) GeV  
614 > (-84.8812 and 106.102) GeV  
615 > (-84.8466 and 106.058) GeV  
616 > (-84.8121 and 106.015) GeV

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617 > (-84.7777 and 105.972) GeV  
618 > (-84.7433 and 105.929) GeV  
619 > (-84.709 and 105.886) GeV  
620 > (-84.6748 and 105.844) GeV  
621 > (-84.6406 and 105.801) GeV  
622 > (-84.6065 and 105.758) GeV  
623 > (-84.5725 and 105.716) GeV  
624 > (-84.5385 and 105.673) GeV  
625 > (-84.5046 and 105.631) GeV  
626 > (-84.4708 and 105.589) GeV  
627 > (-84.4371 and 105.546) GeV  
628 > (-84.4034 and 105.504) GeV  
629 > (-84.3698 and 105.462) GeV  
630 > (-84.3362 and 105.42) GeV  
631 > (-84.3027 and 105.379) GeV  
632 > (-84.2693 and 105.337) GeV  
633 > (-84.236 and 105.295) GeV  
634 > (-84.2027 and 105.253) GeV  
635 > (-84.1694 and 105.212) GeV  
636 > (-84.1363 and 105.17) GeV  
637 > (-84.1032 and 105.129) GeV  
638 > (-84.0702 and 105.088) GeV  
639 > (-84.0372 and 105.047) GeV  
640 > (-84.0043 and 105.005) GeV  
641 > (-83.9715 and 104.964) GeV  
642 > (-83.9387 and 104.923) GeV  
643 > (-83.906 and 104.883) GeV  
644 > (-83.8734 and 104.842) GeV  
645 > (-83.8408 and 104.801) GeV  
646 > (-83.8083 and 104.76) GeV  
647 > (-83.7758 and 104.72) GeV  
648 > (-83.7434 and 104.679) GeV  
649 > (-83.7111 and 104.639) GeV  
650 > (-83.6789 and 104.599) GeV  
651 > (-83.6466 and 104.558) GeV  
652 > (-83.6145 and 104.518) GeV  
653 > (-83.5824 and 104.478) GeV  
654 > (-83.5504 and 104.438) GeV  
655 > (-83.5185 and 104.398) GeV  
656 > (-83.4866 and 104.358) GeV  
657 > (-83.4547 and 104.319) GeV  
658 > (-83.423 and 104.279) GeV  
659 > (-83.3912 and 104.239) GeV  
660 > (-83.3596 and 104.2) GeV  
661 > (-83.328 and 104.16) GeV  
662 > (-83.2965 and 104.121) GeV  
663 > (-83.265 and 104.081) GeV  
664 > (-83.2336 and 104.042) GeV  
665 > (-83.2022 and 104.003) GeV  
666 > (-83.1709 and 103.964) GeV  
667 > (-83.1397 and 103.925) GeV  
668 > (-83.1085 and 103.886) GeV  
669 > (-83.0774 and 103.847) GeV  
670 > (-83.0463 and 103.808) GeV  
671 > (-83.0153 and 103.769) GeV  
672 > (-82.9844 and 103.731) GeV  
673 > (-82.9535 and 103.692) GeV  
674 > (-82.9227 and 103.653) GeV

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675 > (-82.8919 and 103.615) GeV  
676 > (-82.8612 and 103.577) GeV  
677 > (-82.8305 and 103.538) GeV  
678 > (-82.7999 and 103.5) GeV  
679 > (-82.7694 and 103.462) GeV  
680 > (-82.7389 and 103.424) GeV  
681 > (-82.7084 and 103.386) GeV  
682 > (-82.6781 and 103.348) GeV  
683 > (-82.6477 and 103.31) GeV  
684 > (-82.6175 and 103.272) GeV  
685 > (-82.5873 and 103.234) GeV  
686 > (-82.5571 and 103.196) GeV  
687 > (-82.527 and 103.159) GeV  
688 > (-82.497 and 103.121) GeV  
689 > (-82.467 and 103.084) GeV  
690 > (-82.437 and 103.046) GeV  
691 > (-82.4071 and 103.009) GeV  
692 > (-82.3773 and 102.972) GeV  
693 > (-82.3475 and 102.935) GeV  
694 > (-82.3178 and 102.897) GeV  
695 > (-82.2881 and 102.86) GeV  
696 > (-82.2585 and 102.823) GeV  
697 > (-82.229 and 102.786) GeV  
698 > (-82.1995 and 102.749) GeV  
699 > (-82.17 and 102.713) GeV  
700 > (-82.1406 and 102.676) GeV  
701 > (-82.1113 and 102.639) GeV  
702 > (-82.082 and 102.603) GeV  
703 > (-82.0527 and 102.566) GeV  
704 > (-82.0235 and 102.529) GeV  
705 > (-81.9944 and 102.493) GeV  
706 > (-81.9653 and 102.457) GeV  
707 > (-81.9362 and 102.42) GeV  
708 > (-81.9073 and 102.384) GeV  
709 > (-81.8783 and 102.348) GeV  
710 > (-81.8494 and 102.312) GeV  
711 > (-81.8206 and 102.276) GeV  
712 > (-81.7918 and 102.24) GeV  
713 > (-81.7631 and 102.204) GeV  
714 > (-81.7344 and 102.168) GeV  
715 > (-81.7058 and 102.132) GeV  
716 > (-81.6772 and 102.097) GeV  
717 > (-81.6487 and 102.061) GeV  
718 > (-81.6202 and 102.025) GeV  
719 > (-81.5917 and 101.99) GeV  
720 > (-81.5634 and 101.954) GeV  
721 > (-81.535 and 101.919) GeV  
722 > (-81.5067 and 101.883) GeV  
723 > (-81.4785 and 101.848) GeV  
724 > (-81.4503 and 101.813) GeV  
725 > (-81.4222 and 101.778) GeV  
726 > (-81.3941 and 101.743) GeV  
727 > (-81.366 and 101.708) GeV  
728 > (-81.338 and 101.673) GeV  
729 > (-81.3101 and 101.638) GeV  
730 > (-81.2822 and 101.603) GeV  
731 > (-81.2544 and 101.568) GeV  
732 > (-81.2266 and 101.533) GeV

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733 > (-81.1988 and 101.499) GeV  
734 > (-81.1711 and 101.464) GeV  
735 > (-81.1434 and 101.429) GeV  
736 > (-81.1158 and 101.395) GeV  
737 > (-81.0883 and 101.36) GeV  
738 > (-81.0607 and 101.326) GeV  
739 > (-81.0333 and 101.292) GeV  
740 > (-81.0058 and 101.257) GeV  
741 > (-80.9785 and 101.223) GeV  
742 > (-80.9511 and 101.189) GeV  
743 > (-80.9238 and 101.155) GeV  
744 > (-80.8966 and 101.121) GeV  
745 > (-80.8694 and 101.087) GeV  
746 > (-80.8422 and 101.053) GeV  
747 > (-80.8151 and 101.019) GeV  
748 > (-80.7881 and 100.985) GeV  
749 > (-80.7611 and 100.951) GeV  
750 > (-80.7341 and 100.918) GeV  
751 > (-80.7072 and 100.884) GeV  
752 > (-80.6803 and 100.85) GeV  
753 > (-80.6535 and 100.817) GeV  
754 > (-80.6267 and 100.783) GeV  
755 > (-80.5999 and 100.75) GeV  
756 > (-80.5732 and 100.717) GeV  
757 > (-80.5466 and 100.683) GeV  
758 > (-80.52 and 100.65) GeV  
759 > (-80.4934 and 100.617) GeV  
760 > (-80.4669 and 100.584) GeV  
761 > (-80.4404 and 100.551) GeV  
762 > (-80.4139 and 100.517) GeV  
763 > (-80.3875 and 100.484) GeV  
764 > (-80.3612 and 100.452) GeV  
765 > (-80.3349 and 100.419) GeV  
766 > (-80.3086 and 100.386) GeV  
767 > (-80.2824 and 100.353) GeV  
768 > (-80.2562 and 100.32) GeV  
769 > (-80.2301 and 100.288) GeV  
770 > (-80.204 and 100.255) GeV  
771 > (-80.1779 and 100.222) GeV  
772 > (-80.1519 and 100.19) GeV  
773 > (-80.126 and 100.158) GeV  
774 > (-80.1 and 100.125) GeV  
775 > (-80.0741 and 100.093) GeV  
776 > (-80.0483 and 100.06) GeV  
777 > (-80.0225 and 100.028) GeV  
778 > (-79.9967 and 99.996) GeV  
779 > (-79.971 and 99.9638) GeV  
780 > (-79.9454 and 99.9318) GeV  
781 > (-79.9197 and 99.8997) GeV  
782 > (-79.8941 and 99.8677) GeV  
783 > (-79.8686 and 99.8358) GeV  
784 > (-79.8431 and 99.8039) GeV  
785 > (-79.8176 and 99.772) GeV  
786 > (-79.7922 and 99.7403) GeV  
787 > (-79.7668 and 99.7085) GeV  
788 > (-79.7414 and 99.6768) GeV  
789 > (-79.7161 and 99.6452) GeV  
790 > (-79.6908 and 99.6136) GeV

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791 > (-79.6656 and 99.5821) GeV  
792 > (-79.6404 and 99.5506) GeV  
793 > (-79.6153 and 99.5191) GeV  
794 > (-79.5902 and 99.4878) GeV  
795 > (-79.5651 and 99.4564) GeV  
796 > (-79.5401 and 99.4251) GeV  
797 > (-79.5151 and 99.3939) GeV  
798 > (-79.4901 and 99.3627) GeV  
799 > (-79.4652 and 99.3316) GeV  
800 > (-79.4403 and 99.3005) GeV  
801 > (-79.4155 and 99.2694) GeV  
802 > (-79.3907 and 99.2384) GeV  
803 > (-79.3659 and 99.2075) GeV  
804 > (-79.3412 and 99.1766) GeV  
805 > (-79.3165 and 99.1457) GeV  
806 > (-79.2919 and 99.1149) GeV  
807 > (-79.2673 and 99.0842) GeV  
808 > (-79.2427 and 99.0534) GeV  
809 > (-79.2182 and 99.0228) GeV  
810 > (-79.1937 and 98.9922) GeV  
811 > (-79.1692 and 98.9616) GeV  
812 > (-79.1448 and 98.9311) GeV  
813 > (-79.1204 and 98.9006) GeV  
814 > (-79.0961 and 98.8702) GeV  
815 > (-79.0718 and 98.8398) GeV  
816 > (-79.0475 and 98.8095) GeV  
817 > (-79.0233 and 98.7792) GeV  
818 > (-78.9991 and 98.7489) GeV  
819 > (-78.975 and 98.7188) GeV  
820 > (-78.9508 and 98.6886) GeV  
821 > (-78.9268 and 98.6585) GeV  
822 > (-78.9027 and 98.6285) GeV  
823 > (-78.8787 and 98.5984) GeV  
824 > (-78.8547 and 98.5685) GeV  
825 > (-78.8308 and 98.5386) GeV  
826 > (-78.8069 and 98.5087) GeV  
827 > (-78.783 and 98.4789) GeV  
828 > (-78.7592 and 98.4491) GeV  
829 > (-78.7354 and 98.4193) GeV  
830 > (-78.7117 and 98.3896) GeV  
831 > (-78.688 and 98.36) GeV  
832 > (-78.6643 and 98.3304) GeV  
833 > (-78.6406 and 98.3008) GeV  
834 > (-78.617 and 98.2713) GeV  
835 > (-78.5934 and 98.2418) GeV  
836 > (-78.5699 and 98.2124) GeV  
837 > (-78.5464 and 98.183) GeV  
838 > (-78.5229 and 98.1537) GeV  
839 > (-78.4995 and 98.1244) GeV  
840 > (-78.4761 and 98.0952) GeV  
841 > (-78.4527 and 98.0659) GeV  
842 > (-78.4294 and 98.0368) GeV  
843 > (-78.4061 and 98.0077) GeV  
844 > (-78.3828 and 97.9786) GeV  
845 > (-78.3596 and 97.9496) GeV  
846 > (-78.3364 and 97.9206) GeV  
847 > (-78.3132 and 97.8916) GeV  
848 > (-78.2901 and 97.8627) GeV

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849 > (-78.267 and 97.8338) GeV  
850 > (-78.244 and 97.805) GeV  
851 > (-78.221 and 97.7762) GeV  
852 > (-78.198 and 97.7475) GeV  
853 > (-78.175 and 97.7188) GeV  
854 > (-78.1521 and 97.6902) GeV  
855 > (-78.1292 and 97.6616) GeV  
856 > (-78.1063 and 97.633) GeV  
857 > (-78.0835 and 97.6045) GeV  
858 > (-78.0607 and 97.576) GeV  
859 > (-78.038 and 97.5475) GeV  
860 > (-78.0153 and 97.5191) GeV  
861 > (-77.9926 and 97.4908) GeV  
862 > (-77.9699 and 97.4625) GeV  
863 > (-77.9473 and 97.4342) GeV  
864 > (-77.9247 and 97.4059) GeV  
865 > (-77.9021 and 97.3777) GeV  
866 > (-77.8796 and 97.3496) GeV  
867 > (-77.8571 and 97.3215) GeV  
868 > (-77.8347 and 97.2934) GeV  
869 > (-77.8122 and 97.2654) GeV  
870 > (-77.7899 and 97.2374) GeV  
871 > (-77.7675 and 97.2094) GeV  
872 > (-77.7452 and 97.1815) GeV  
873 > (-77.7229 and 97.1536) GeV  
874 > (-77.7006 and 97.1258) GeV  
875 > (-77.6784 and 97.098) GeV  
876 > (-77.6562 and 97.0702) GeV  
877 > (-77.634 and 97.0425) GeV  
878 > (-77.6118 and 97.0149) GeV  
879 > (-77.5897 and 96.9872) GeV  
880 > (-77.5677 and 96.9596) GeV  
881 > (-77.5456 and 96.9321) GeV  
882 > (-77.5236 and 96.9046) GeV  
883 > (-77.5016 and 96.8771) GeV  
884 > (-77.4797 and 96.8496) GeV  
885 > (-77.4577 and 96.8222) GeV  
886 > (-77.4359 and 96.7949) GeV  
887 > (-77.414 and 96.7675) GeV  
888 > (-77.3922 and 96.7403) GeV  
889 > (-77.3704 and 96.713) GeV  
890 > (-77.3486 and 96.6858) GeV  
891 > (-77.3269 and 96.6586) GeV  
892 > (-77.3052 and 96.6315) GeV  
893 > (-77.2835 and 96.6044) GeV  
894 > (-77.2618 and 96.5774) GeV  
895 > (-77.2402 and 96.5503) GeV  
896 > (-77.2187 and 96.5234) GeV  
897 > (-77.1971 and 96.4964) GeV  
898 > (-77.1756 and 96.4695) GeV  
899 > (-77.1541 and 96.4426) GeV  
900 > (-77.1326 and 96.4158) GeV  
901 > (-77.1112 and 96.389) GeV  
902 > (-77.0898 and 96.3623) GeV  
903 > (-77.0684 and 96.3355) GeV  
904 > (-77.0471 and 96.3089) GeV  
905 > (-77.0257 and 96.2822) GeV  
906 > (-77.0045 and 96.2556) GeV

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907 > (-76.9832 and 96.229) GeV  
908 > (-76.962 and 96.2025) GeV  
909 > (-76.9408 and 96.176) GeV  
910 > (-76.9196 and 96.1495) GeV  
911 > (-76.8985 and 96.1231) GeV  
912 > (-76.8774 and 96.0967) GeV  
913 > (-76.8563 and 96.0704) GeV  
914 > (-76.8352 and 96.0441) GeV  
915 > (-76.8142 and 96.0178) GeV  
916 > (-76.7932 and 95.9915) GeV  
917 > (-76.7722 and 95.9653) GeV  
918 > (-76.7513 and 95.9392) GeV  
919 > (-76.7304 and 95.913) GeV  
920 > (-76.7095 and 95.8869) GeV  
921 > (-76.6886 and 95.8609) GeV  
922 > (-76.6678 and 95.8348) GeV  
923 > (-76.647 and 95.8088) GeV  
924 > (-76.6263 and 95.7829) GeV  
925 > (-76.6055 and 95.7569) GeV  
926 > (-76.5848 and 95.7311) GeV  
927 > (-76.5641 and 95.7052) GeV  
928 > (-76.5435 and 95.6794) GeV  
929 > (-76.5228 and 95.6536) GeV  
930 > (-76.5022 and 95.6278) GeV  
931 > (-76.4817 and 95.6021) GeV  
932 > (-76.4611 and 95.5764) GeV  
933 > (-76.4406 and 95.5508) GeV  
934 > (-76.4201 and 95.5252) GeV  
935 > (-76.3996 and 95.4996) GeV  
936 > (-76.3792 and 95.4741) GeV  
937 > (-76.3588 and 95.4485) GeV  
938 > (-76.3384 and 95.4231) GeV  
939 > (-76.3181 and 95.3976) GeV  
940 > (-76.2977 and 95.3722) GeV  
941 > (-76.2774 and 95.3468) GeV  
942 > (-76.2572 and 95.3215) GeV  
943 > (-76.2369 and 95.2962) GeV  
944 > (-76.2167 and 95.2709) GeV  
945 > (-76.1965 and 95.2457) GeV  
946 > (-76.1763 and 95.2205) GeV  
947 > (-76.1562 and 95.1953) GeV  
948 > (-76.1361 and 95.1702) GeV  
949 > (-76.116 and 95.1451) GeV  
950 > (-76.096 and 95.12) GeV  
951 > (-76.0759 and 95.0949) GeV  
952 > (-76.0559 and 95.0699) GeV  
953 > (-76.0359 and 95.045) GeV  
954 > (-76.016 and 95.02) GeV  
955 > (-75.996 and 94.9951) GeV  
956 > (-75.9761 and 94.9702) GeV  
957 > (-75.9563 and 94.9454) GeV  
958 > (-75.9364 and 94.9206) GeV  
959 > (-75.9166 and 94.8958) GeV  
960 > (-75.8968 and 94.871) GeV  
961 > (-75.877 and 94.8463) GeV  
962 > (-75.8573 and 94.8216) GeV  
963 > (-75.8376 and 94.797) GeV  
964 > (-75.8179 and 94.7724) GeV

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965 > (-75.7982 and 94.7478) GeV
966 > (-75.7786 and 94.7232) GeV
967 > (-75.7589 and 94.6987) GeV
968 > (-75.7393 and 94.6742) GeV
969 > (-75.7198 and 94.6498) GeV
970 > (-75.7002 and 94.6253) GeV
971 > (-75.6807 and 94.6009) GeV
972 > (-75.6612 and 94.5766) GeV
973 > (-75.6418 and 94.5522) GeV
974 > (-75.6223 and 94.5279) GeV
975 > (-75.6029 and 94.5037) GeV
976 > (-75.5835 and 94.4794) GeV
977 > (-75.5641 and 94.4552) GeV
978 > (-75.5448 and 94.431) GeV
979 > (-75.5255 and 94.4069) GeV
980 > (-75.5062 and 94.3828) GeV
981 > (-75.4869 and 94.3587) GeV
982 > (-75.4677 and 94.3346) GeV
983 > (-75.4484 and 94.3106) GeV
984 > (-75.4293 and 94.2866) GeV
985 > (-75.4101 and 94.2626) GeV
986 > (-75.3909 and 94.2387) GeV
987 > (-75.3718 and 94.2148) GeV
988 > (-75.3527 and 94.1909) GeV
989 > (-75.3336 and 94.1671) GeV
990 > (-75.3146 and 94.1433) GeV
991 > (-75.2956 and 94.1195) GeV
992 > (-75.2766 and 94.0957) GeV
993 > (-75.2576 and 94.072) GeV
994 > (-75.2386 and 94.0483) GeV
995 > (-75.2197 and 94.0247) GeV
996 > (-75.2008 and 94.001) GeV
997 > (-75.1819 and 93.9774) GeV
998 > (-75.1631 and 93.9539) GeV
999 > (-75.1442 and 93.9303) GeV
```

[Program finished]

Or

```
from math import sqrt, floor
t = 1000
dP1 = [0]*(t+1)
dP2 = [0]*(t+1)
dE = [0]*(t+1)
S = [0]*(t+1)
gM = sqrt(1393.6328858707575005182839547884)
```

for k3 in range(-t, t + 1):

if k3 != 0 and k3 != -1 and k3 != -2:

```
dP1[k3]=-((2**((11/4)*gM*k3**2+2**((19/4)*gM*k3+2**((15/4)*gM)*sqrt(abs(k3))*abs(2*k3+2)**(3/4)))/((k3**3+4*k3**2+4*k3)*sqrt(abs(k3+1))))
```

```
dP2[k3]=((5*2**((3/4)*gM*k3**3+25*2**((3/4)*gM*k3**2+2**((23/4)*gM*k3+3*2**((11/4)*gM)*abs(k3)**(3/2)*abs(2*k3+2)**(3/4)))/((k3**4+4*k3**3+4*k3**2)*abs(k3+1)**(3/2)))
```

```
dE[k3] = (2**((7/4)*gM*sqrt(abs(k3+1)))/(sqrt(abs(k3))*abs(2*k3+2)**(1/4)))
```

---

```

if k3 == t:
    N = floor(dE[1]/dE[t])

for l1 in range(1, t - 1 + 1):
    print(l1, '> (' , dP1[l1], ' and ', dP2[l1], ') GeV')

for l2 in range(N, l1 - 1 + 1, -1):
    for q1 in range(1, N + 1):
        for q2 in range(1, N + 1):

            if (dP1[l1] + dP2[l1]) - (q1 * dP1[l2] + q2 * dP2[l2]) > 0 and (dP1[l1] + dP2[l1]) - (q1 * dP1[l2] + q2 * dP2[l2]) < (dP1[l1] + dP2[l1]) - (dP1[l1+1] + dP2[l1+1]):
                print(l1, '> ~ {' , q1, '+', q2, '}', l2, '>')
                S[l1] = S[l1]+q1+q2
            elif l2 == l1-1 and q1 == N and q2 == N:
                print(S[l1])

→ 1 > (-390.6539386225637 and 516.2212760369592) GeV
2 > (-343.91613120922744 and 442.17788298329236) GeV
3 > (-317.26442383699344 and 403.4775824883504) GeV
4 > (-298.2415168443712 and 377.18780071494) GeV
5 > (-283.55268636279027 and 357.45737589351734) GeV
6 > (-271.7000873961953 and 341.8162389823102) GeV
7 > (-261.84526624588773 and 328.9638313279034) GeV
8 > (-253.46668643498933 and 318.126555423507) GeV
9 > (-246.21783835474818 and 308.8068266760182) GeV
10 > (-239.85744399004764 and 300.66637345231317) GeV
11 > (-234.21133699219496 and 293.4654027881245) GeV
12 > (-229.15010016387234 and 287.0282182465) GeV
13 > (-224.57523121688487 and 281.22257092966413) GeV
14 > (-220.4102189703796 and 275.9466520967744) GeV
15 > (-216.5945865514654 and 271.120575674613) GeV
16 > (-213.07979892902634 and 266.6806179142783) GeV
17 > (-209.8263809454959 and 262.5752134812368) GeV
18 > (-206.80184366062977 and 258.7621058869186) GeV
19 > (-203.9791637597128 and 255.20627720961787) GeV
20 > (-201.3356495824613 and 251.87841638635706) GeV
21 > (-198.85208262036286 and 248.7537674904634) GeV
22 > (-196.5120586669301 and 245.81125108511458) GeV
23 > (-194.3014759183959 and 243.0327850873355) GeV
24 > (-192.20813275710222 and 240.40275358195424) GeV
25 > (-190.22140845177665 and 237.9075868428857) GeV
26 > (-188.3320072770243 and 235.53542598072866) GeV
27 > (-186.53175166310086 and 233.27585272051078) GeV
28 > (-184.81341362942356 and 231.11966982833255) GeV
29 > (-183.17057638646466 and 229.0587213049716) GeV
30 > (-181.5975199145539 and 227.08574408101748) GeV
31 > (-180.08912575073177 and 225.19424487275262) GeV
32 > (-178.6407972778022 and 223.37839728931408) GeV
33 > (-177.2483926118093 and 221.63295535699862) GeV
34 > (-175.9081677949133 and 219.9531804421713) GeV
35 > (-174.61672846968085 and 218.33477917834816) GeV
36 > (-173.37098857393224 and 216.77385048460457) GeV
37 > (-172.168134878535 and 215.26684013697005) GeV
38 > (-171.005596413066 and 213.81050164787598) GeV
39 > (-169.88101800026317 and 212.4018624401741) GeV
40 > (-168.7922372602816 and 211.03819448603875) GeV
41 > (-167.73726455795207 and 209.71698872791055) GeV

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42 > (-166.71426545658895 and 208.43593271666595) GeV  
43 > (-165.7215453150557 and 207.19289099758015) GeV  
44 > (-164.7575357243483 and 205.9858878521535) GeV  
45 > (-163.82078252866498 and 204.81309206715846) GeV  
46 > (-162.90993521596522 and 203.67280345419104) GeV  
47 > (-162.02373749606568 and 202.563440885817) GeV  
48 > (-161.16101891171968 and 201.4835316498401) GeV  
49 > (-160.32068735093415 and 200.4317019526828) GeV  
50 > (-159.50172234783844 and 199.40666842746043) GeV  
51 > (-158.70316907541124 and 198.40723052293794) GeV  
52 > (-157.92413294683206 and 197.4322636668871) GeV  
53 > (-157.16377475359766 and 196.4807131119861) GeV  
54 > (-156.4213062781863 and 195.55158838479062) GeV  
55 > (-155.69598632724694 and 194.64395826882574) GeV  
56 > (-154.9871171382882 and 193.75694626181598) GeV  
57 > (-154.29404111881922 and 192.88972645473538) GeV  
58 > (-153.61613788203184 and 192.04151978693136) GeV  
59 > (-152.95282154752664 and 191.21159063722453) GeV  
60 > (-152.3035382793957 and 190.39924371575674) GeV  
61 > (-151.66776403726902 and 189.6038212255676) GeV  
62 > (-151.0450025187881 and 188.82470026652598) GeV  
63 > (-150.43478327445217 and 188.06129045741213) GeV  
64 > (-149.83665997794483 and 187.31303175469765) GeV  
65 > (-149.25020883693637 and 186.5793924489827) GeV  
66 > (-148.67502713100927 and 185.85986732214872) GeV  
67 > (-148.11073186480164 and 185.15397595013044) GeV  
68 > (-147.55695852573666 and 184.46126113782879) GeV  
69 > (-147.01335993682545 and 183.78128747411156) GeV  
70 > (-146.4796051960183 and 183.11363999610313) GeV  
71 > (-145.9553786944528 and 182.45792295307572) GeV  
72 > (-145.44037920672045 and 181.81375866123273) GeV  
73 > (-144.93431904695726 and 181.18078644154795) GeV  
74 > (-144.4369232851736 and 180.558661633596) GeV  
75 > (-143.94792901878006 and 179.9470546789938) GeV  
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77 > (-142.99414947827856 and 178.7541465488803) GeV  
78 > (-142.52889266422613 and 178.17225438081903) GeV  
79 > (-142.0710931278913 and 177.59969665023058) GeV  
80 > (-141.620538812079 and 177.03620762241883) GeV  
81 > (-141.17702624761685 and 176.48153233952303) GeV  
82 > (-140.7403601047686 and 175.93542605668404) GeV  
83 > (-140.31035277320356 and 175.39765371416965) GeV  
84 > (-139.88682396838757 and 174.86798944276526) GeV  
85 > (-139.46960036244215 and 174.34621609996438) GeV  
86 > (-139.0585152376834 and 173.83212483470675) GeV  
87 > (-138.6534081612047 and 173.32551467859645) GeV  
88 > (-138.25412467899852 and 172.82619216170679) GeV  
89 > (-137.8605160282396 and 172.33397095123306) GeV  
90 > (-137.47243886646046 and 171.84867151139431) GeV  
91 > (-137.08975501645344 and 171.37012078311542) GeV  
92 > (-136.71233122582447 and 170.89815188213487) GeV  
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96 > (-135.25273162807156 and 169.0729574809147) GeV  
97 > (-134.89976653284984 and 168.63159150959393) GeV  
98 > (-134.55135355076263 and 168.19592085191354) GeV  
99 > (-134.20738821149135 and 167.76581470294693) GeV

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100 > (-133.86776946918437 and 167.34114654949082) GeV  
101 > (-133.53239955727736 and 166.9217939879164) GeV  
102 > (-133.20118385083526 and 166.5076385514695) GeV  
103 > (-132.87403073595598 and 166.0985655464412) GeV  
104 > (-132.55085148580895 and 165.69446389667215) GeV  
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149 > (-121.07954000110709 and 151.35208037091763) GeV  
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157 > (-119.49762245742116 and 149.37439164672907) GeV

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158 > (-119.30701631651833 and 149.13610079287258) GeV  
159 > (-119.11791989589105 and 148.89969775789763) GeV  
160 > (-118.93031181730156 and 148.66515580149928) GeV  
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163 > (-118.3762102979543 and 147.9724370672469) GeV  
164 > (-118.19435032204842 and 147.74508267918685) GeV  
165 > (-118.01387808820115 and 147.51946354022036) GeV  
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167 > (-117.65702146965246 and 147.07333673099512) GeV  
168 > (-117.4806003141249 and 146.85278306966342) GeV  
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175 > (-116.28149179065502 and 145.35372066917378) GeV  
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177 > (-115.94991528387204 and 144.93920361692346) GeV  
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182 > (-115.1411598935846 and 143.92815042171426) GeV  
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184 > (-114.82543279829227 and 143.5334506127234) GeV  
185 > (-114.66918085209392 and 143.3381157422537) GeV  
186 > (-114.51398586488536 and 143.1441024146598) GeV  
187 > (-114.35983504107762 and 142.95139462772855) GeV  
188 > (-114.20671580755638 and 142.75997665755347) GeV  
189 > (-114.05461580865261 and 142.5698330522411) GeV  
190 > (-113.90352290125253 and 142.38094862579115) GeV  
191 > (-113.7534251500424 and 142.19330845214674) GeV  
192 > (-113.60431082288436 and 142.00689785940767) GeV  
193 > (-113.45616838631857 and 141.821702424202) GeV  
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200 > (-112.44545521065604 and 140.55819695380347) GeV  
201 > (-112.30469514469006 and 140.3822316203952) GeV  
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203 > (-112.02579427989622 and 140.03357576035123) GeV  
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205 > (-111.75032142380304 and 139.68920584213188) GeV  
206 > (-111.61384694335489 and 139.518598654772) GeV  
207 > (-111.4782014959011 and 139.3490279774051) GeV  
208 > (-111.34337606304865 and 139.18048253261898) GeV  
209 > (-111.20936176738815 and 139.01295121934064) GeV  
210 > (-111.07614986962584 and 138.84642310924838) GeV  
211 > (-110.94373176578826 and 138.68088744327434) GeV  
212 > (-110.81209898449553 and 138.51633362819314) GeV  
213 > (-110.6812431843028 and 138.35275123329572) GeV  
214 > (-110.55115615110704 and 138.1901299871449) GeV  
215 > (-110.42182979561719 and 138.02845977441078) GeV

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216 > (-110.29325615088653 and 137.86773063278298) GeV  
217 > (-110.16542736990472 and 137.7079327499585) GeV  
218 > (-110.03833572324818 and 137.54905646070227) GeV  
219 > (-109.91197359678706 and 137.3910922439782) GeV  
220 > (-109.78633348944717 and 137.2340307201496) GeV  
221 > (-109.66140801102537 and 137.077862648246) GeV  
222 > (-109.53718988005677 and 136.92257892329496) GeV  
223 > (-109.41367192173254 and 136.76817057371733) GeV  
224 > (-109.29084706586637 and 136.61462875878345) GeV  
225 > (-109.16870834490913 and 136.4619447661292) GeV  
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227 > (-108.9264619391194 and 136.15911602553106) GeV  
228 > (-108.80634081514425 and 136.00895447313292) GeV  
229 > (-108.6868789441345 and 135.85961712952945) GeV  
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240 > (-107.41451846823695 and 134.2690651861335) GeV  
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242 > (-107.1910372966184 and 133.98969687136338) GeV  
243 > (-107.08016380649292 and 133.85109675088395) GeV  
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248 > (-106.53425581574747 and 133.1686720710045) GeV  
249 > (-106.42673019174538 and 133.034257409678) GeV  
250 > (-106.31974489961927 and 132.90051826150324) GeV  
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253 > (-106.00198266015246 and 132.50329343663316) GeV  
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255 > (-105.79275526190956 and 132.24174496732337) GeV  
256 > (-105.68891192720518 and 132.11193382228976) GeV  
257 > (-105.58557614405716 and 131.98275720414858) GeV  
258 > (-105.48274346540367 and 131.85420955264473) GeV  
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260 > (-105.27856991267606 and 131.59897925785003) GeV  
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262 > (-105.07635679714694 and 131.3461998372004) GeV  
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268 > (-104.48114799698891 and 130.60215162184997) GeV  
269 > (-104.38357135800536 and 130.48017487964663) GeV  
270 > (-104.28644858044865 and 130.35876553516712) GeV  
271 > (-104.1897758791809 and 130.2379188558855) GeV  
272 > (-104.093549514485 and 130.11763016607367) GeV  
273 > (-103.99776579135535 and 129.99789484591295) GeV

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274 > (-103.90242105880098 and 129.87870833062345) GeV  
275 > (-103.80751170916284 and 129.76006610960965) GeV  
276 > (-103.71303417744349 and 129.64196372562273) GeV  
277 > (-103.61898494065044 and 129.52439677393826) GeV  
278 > (-103.52536051715069 and 129.4073609015502) GeV  
279 > (-103.43215746603883 and 129.2908518063797) GeV  
280 > (-103.33937238651585 and 129.1748652364985) GeV  
281 > (-103.24700191728039 and 129.0593969893678) GeV  
282 > (-103.15504273593095 and 128.94444291109045) GeV  
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284 > (-102.97234513827577 and 128.71606088432802) GeV  
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933 > (-76.44059896934144 and 95.55079243084168) GeV  
934 > (-76.42010867641612 and 95.52517945962356) GeV  
935 > (-76.39964581627136 and 95.49960077974544) GeV  
936 > (-76.37921032286945 and 95.4740563086586) GeV  
937 > (-76.35880213040205 and 95.44854596410083) GeV  
938 > (-76.33842117328915 and 95.42306966409555) GeV  
939 > (-76.31806738617797 and 95.39762732695021) GeV  
940 > (-76.2977407039421 and 95.37221887125509) GeV  
941 > (-76.27744106168028 and 95.34684421588211) GeV  
942 > (-76.25716839471559 and 95.32150327998347) GeV  
943 > (-76.23692263859422 and 95.29619598299031) GeV  
944 > (-76.2167037290846 and 95.27092224461164) GeV  
945 > (-76.19651160217643 and 95.24568198483294) GeV  
946 > (-76.17634619407954 and 95.22047512391504) GeV  
947 > (-76.15620744122306 and 95.19530158239267) GeV  
948 > (-76.13609528025427 and 95.17016128107352) GeV  
949 > (-76.1160096480378 and 95.14505414103674) GeV  
950 > (-76.09595048165451 and 95.11998008363193) GeV  
951 > (-76.07591771840063 and 95.09493903047783) GeV  
952 > (-76.05591129578669 and 95.06993090346116) GeV  
953 > (-76.03593115153666 and 95.04495562473527) GeV  
954 > (-76.01597722358694 and 95.02001311671928) GeV  
955 > (-75.99604945008545 and 94.99510330209655) GeV  
956 > (-75.97614776939066 and 94.97022610381369) GeV  
957 > (-75.95627212007066 and 94.94538144507936) GeV  
958 > (-75.93642244090223 and 94.92056924936308) GeV  
959 > (-75.91659867086997 and 94.89578944039407) GeV  
960 > (-75.89680074916522 and 94.87104194216013) GeV  
961 > (-75.87702861518532 and 94.84632667890654) GeV  
962 > (-75.85728220853264 and 94.82164357513473) GeV  
963 > (-75.83756146901362 and 94.79699255560142) GeV  
964 > (-75.81786633663796 and 94.77237354531725) GeV  
965 > (-75.7981967516176 and 94.7477864695458) GeV  
966 > (-75.778552654366 and 94.72323125380247) GeV  
967 > (-75.75893398549705 and 94.69870782385323) GeV  
968 > (-75.7393406858244 and 94.67421610571374) GeV  
969 > (-75.71977269636041 and 94.64975602564813) GeV

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```
970 > (-75.70022995831538 and 94.62532751016782) GeV
971 > (-75.68071241309664 and 94.60093048603068) GeV
972 > (-75.6612200023077 and 94.57656488023977) GeV
973 > (-75.64175266774738 and 94.55223062004217) GeV
974 > (-75.62231035140894 and 94.52792763292823) GeV
975 > (-75.60289299547932 and 94.50365584663015) GeV
976 > (-75.58350054233819 and 94.47941518912135) GeV
977 > (-75.5641329345572 and 94.45520558861494) GeV
978 > (-75.54479011489896 and 94.43102697356301) GeV
979 > (-75.52547202631652 and 94.40687927265546) GeV
980 > (-75.5061786119523 and 94.38276241481903) GeV
981 > (-75.4869098151373 and 94.35867632921621) GeV
982 > (-75.46766557939038 and 94.33462094524431) GeV
983 > (-75.44844584841732 and 94.31059619253425) GeV
984 > (-75.42925056611021 and 94.28660200094988) GeV
985 > (-75.41007967654635 and 94.26263830058656) GeV
986 > (-75.39093312398775 and 94.23870502177051) GeV
987 > (-75.37181085288009 and 94.21480209505765) GeV
988 > (-75.35271280785213 and 94.19092945123262) GeV
989 > (-75.33363893371474 and 94.16708702130788) GeV
990 > (-75.31458917546036 and 94.1432747365226) GeV
991 > (-75.29556347826184 and 94.11949252834175) GeV
992 > (-75.27656178747213 and 94.09574032845522) GeV
993 > (-75.25758404862309 and 94.07201806877669) GeV
994 > (-75.23863020742502 and 94.04832568144276) GeV
995 > (-75.21970020976572 and 94.02466309881203) GeV
996 > (-75.20079400170984 and 94.0010302534641) GeV
997 > (-75.18191152949801 and 93.9774270781986) GeV
998 > (-75.16305273954622 and 93.95385350603433) GeV
999 > (-75.14421757844504 and 93.93030947020827) GeV
```

[Program finished]

Or

Instead of :

```
from math import*
t = 1000
dP1 = [0]*(t+1)
dP2 = [0]*(t+1)
dP3 = [0]*(t+1)
dP4 = [0]*(t+1)
dP5 = [0]*(t+1)
dE = [0]*(t+1)
S = [0]*(t+1)
gM = sqrt(1393.6328858707575005182839547884)
for k3 in range(-t,t + 1):
```

```
#if[k3!= -1, k3!= -2, k3!= 0]
if k3!= 0 and k3!= -1 and k3!= -2:
```

```
dP1[k3]=-(2**((11/4)*gM*k3**3+5*2**((11/4)*gM*k3**2+3*2**((15/4)*gM*k3+2**((15/4)*gM*abs(k3)**(3/2)*abs(2
*k3+2)**(3/4))/((k 3**4+4*k3**3+4*k3**2)*abs(k3+1)**(3/2)))
```

```
#imdp1[k3]=0
dP2[k3]=((2**((27/4)*gM*k3+2**((27/4)*gM)*sqrt(abs(k3))*abs(2*k3+2)**(3/4))/((k3**4+8*k3**3+24*k3**2+32
*k3+16)*sqrt(abs(k3+1))))
```

---

```

#imdP2[k3] = 0
dP3[k3] = -((5*2**((11/4)*gM*k3**5+45*2**((11/4)*gM*k3**4+71*2**((15/4)*gM*k3**3+95*2**((15/4)*gM*k3**2+7*2**((27/4)*gM*k3+3*2**((23/4)*gM)*abs(k3)**(3/2)*abs(2*k3+2)**(3/4)))/(k3**6+8*k3**5+24*k3**4+32*k3**3+16*k3**2)*abs(k3+1)**(3/2)))

#imdP3[k3] = 0
dP4[k3] = -((5*2**((11/4)*gM*k3**5+45*2**((11/4)*gM*k3**4+71*2**((15/4)*gM*k3**3+95*2**((15/4)*gM*k3**2+7*2**((27/4)*gM*k3+3*2**((23/4)*gM)*abs(k3)**(3/2)*abs(2*k3+2)**(3/4)))/(k3**6+8*k3**5+24*k3**4+32*k3**3+16*k3**2)*abs(k3+1)**(3/2)))

#imdP4[k3] = 0
dP5[k3] = (k3**2*(45*gM*k3**4+315*gM*k3**3+594*gM*k3**2+444*gM*k3+120*gM)*sqrt(abs(k3))*abs(2*k3+2)**(7/4))/(k3+1)**2*(2**((1/4)*k3**6+3*2**((5/4)*k3**5+3*2**((9/4)*k3**4+2**((13/4)*k3**3)*sqrt(abs(k3+1)))))

#imdP5[k3] = 0
#imdE[k3] = 0
dE[k3] = (2**((7/4)*gM*sqrt(abs(k3+1)))/(sqrt(abs(k3))*abs(2*k3+2)**(1/4)))
if k3 == t:
    N = floor(dE[1]/dE[t])
for l1 in range(1,t-1+1):
    print(l1,>('dP1[l1]', 'and ', 'dP2[l1]',) GeV)
for l2 in range(N,l1-1+1,-1):
    for q1 in range(1,N+1):
        for q2 in range(1,N+1):
            for q3 in range(1,N+1):
                for q4 in range(1,N+1):
                    for q5 in range(1,N+1):
                        if(dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(q1*dP1[l2]+q2*dP2[l2]+q3*dP3[l2]+q4*dP4[l2]+q5*dP5[l2])>0 and (dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(q1*dP1[l2]+q2*dP2[l2]+q3*dP3[l2]+q4*dP4[l2]+q5*dP5[l2])<(dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(dP1[l1+1]+dP2[l1+1]+dP3[l1+1]+dP4[l1+1]+dP5[l1+1]):
                            print(l1,>~{'q1','+',q2,'+',q3,'+',q4,'+',q5,'.'},l2,>')

S[l1] = S[l1]+q1+q2+q3+q4+q5
elif l2==l1-1 and q1==N and q2==N and q3==N and q4==N and q5==N:
    print(S[l1])
→ ...
Then in C++ :
#include <iostream>
#include <cmath>
using namespace std;

int main()
{
    const int t = 1000;
    double dP1[t+1]={}, dP2[t+1]={}, dP3[t+1]={}, dP4[t+1]={}, dP5[t+1]={}, dE[t+1]={}, S[t+1]={};
    double gM = sqrt(1393.6328858707575005182839547884);
    int k3 = 1;
    int l1 = 1;
    int q1 = 1;
    int q2 = 1;
    int q3 = 1;
    int q4 = 1;
    int q5 = 1;

    for(int k3 = -t; k3 <= t; k3++)
    {
        if(k3!= 0 && k3!= -1 && k3!= -2)

```

```

dP1[k3]=-((pow(2,11.0/4)*gM*pow(k3,3)+5*pow(2,11.0/4)*gM*pow(k3,2)+3*pow(2,15.0/4)*gM*k3+pow(2,15.0/4)*gM)*pow(abs(k3),3.0/2)*pow(abs(2*k3+2),3.0/4))/((pow(k3,4)+4*pow(k3,3)+4*pow(k3,2))*pow(abs(k3+1),3.0/2));

dP2[k3]=((pow(2,27.0/4)*gM*k3+pow(2,27.0/4)*gM)*sqrt(abs(k3))*pow(abs(2*k3+2),3.0/4))/((pow(k3,4)+8*pow(k3,3)+24*pow(k3,2)+32*k3+16)*sqrt(abs(k3+1)));

dP3[k3]=-((5*pow(2,11.0/4)*gM*pow(k3,5)+45*pow(2,11.0/4)*gM*pow(k3,4)+71*pow(2,15.0/4)*gM*pow(k3,3)+95*pow(2,15.0/4)*gM*po w(k3,2)+7*pow(2,27.0/4)*gM*k3+3*pow(2,23.0/4)*gM)*pow(abs(k3),3.0/2)*pow(abs(2*k3+2),3.0/4))/((pow(k3,6)+8*pow(k3,5)+24*pow(k3,4)+32*pow(k3,3)+16*pow(k3,2))*pow(abs(k3+1),3.0/2));

dP4[k3]=-((5*pow(2,11.0/4)*gM*pow(k3,5)+45*pow(2,11.0/4)*gM*pow(k3,4)+71*pow(2,15.0/4)*gM*pow(k3,3)+95*pow(2,15.0/4)*gM*pow(k3,2)+7*pow(2,27.0/4)*gM*k3+3*pow(2,23.0/4)*gM)*pow(abs(k3),3.0/2)*pow(abs(2*k3+2),3.0/4))/((pow(k3,6)+8*pow(k3,5)+24*pow(k3,4)+32*pow(k3,3)+16*pow(k3,2))*pow(abs(k3+1),3.0/2));

dE[k3]=(pow(2,7.0/4)*gM*sqrt(abs(k3+1)))/(sqrt(abs(k3))*pow(abs(2*k3+2),1.0/4));
}

}

int N = 0;
for(int l1 = 1; l1 <= t-1; l1++)
{
    cout<<l1<<"> ("<<dP1[l1]<<" and "<<dP2[l1]<<") GeV"<<endl;
}
if(k3 == t)
{
    N = floor(dE[1]/dE[t]);
}
for(int l2 = N; l2 >= l1-1; l2--)
{
    for(int q1 = 1; q1 <= N; q1++)
    {
        for(int q2 = 1; q2 <= N; q2++)
        {
            for(int q3 = 1; q3 <= N; q3++)
            {
                for(int q4 = 1; q4 <= N; q4++)
                {
                    for(int q5 = 1; q5 <= N; q5++)
                    {
                        if((dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(q1*dP1[l2]+q2*dP2[l2]+q3*dP3[l2]+q 4*dP4[l2]+q5*dP5[l2]) > 0
&& (dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(q1*dP1[l2]+q2*dP2[l2]+q3*dP3[l2]+q4*dP4[l2]+q5*dP5[l2]) <(dP1[l1]+dP2[l1]+dP3[l1]+dP4[l1]+dP5[l1])-(dP1[l1+1]+dP2[l1+1]+dP3[l1+1]+dP4[l1+1]+dP5[l1+1]))
{
                            cout<<l1<<"> ~ {"<<q1<<"+<<q2<<"+<<q3<<"+<<q4<<"+<<q5<<"}."<<l2
<<"><<endl;
                            S[l1] = S[l1] + q1 + q2 + q3 + q4 + q5;
}
}
}
}
}
}
}
if(l2 == l1-1 && q1 == N && q2 == N && q3 == N && q4 == N && q5 == N)
{
    cout<<S[l1]<<endl;
}
}
return 0;
}

```

---

→ 1 > (-390.654 and 198.427) GeV  
2 > (-343.916 and 147.393) GeV  
3 > (-317.264 and 105.939) GeV  
4 > (-298.242 and 77.9716) GeV  
5 > (-283.553 and 59.0991) GeV  
6 > (-271.7 and 46.0137) GeV  
7 > (-261.845 and 36.6641) GeV  
8 > (-253.467 and 29.7953) GeV  
9 > (-246.218 and 24.6235) GeV  
10 > (-239.857 and 20.645) GeV  
11 > (-234.211 and 17.5266) GeV  
12 > (-229.15 and 15.042) GeV  
13 > (-224.575 and 13.0336) GeV  
14 > (-220.41 and 11.3893) GeV  
15 > (-216.595 and 10.0276) GeV  
16 > (-213.08 and 8.88854) GeV  
17 > (-209.826 and 7.92684) GeV  
18 > (-206.802 and 7.10816) GeV  
19 > (-203.979 and 6.40599) GeV  
20 > (-201.336 and 5.79959) GeV  
21 > (-198.852 and 5.27261) GeV  
22 > (-196.512 and 4.812) GeV  
23 > (-194.301 and 4.40724) GeV  
24 > (-192.208 and 4.04983) GeV  
25 > (-190.221 and 3.73277) GeV  
26 > (-188.332 and 3.45031) GeV  
27 > (-186.532 and 3.19769) GeV  
28 > (-184.813 and 2.97092) GeV  
29 > (-183.171 and 2.76664) GeV  
30 > (-181.598 and 2.58203) GeV  
31 > (-180.089 and 2.41469) GeV  
32 > (-178.641 and 2.26256) GeV  
33 > (-177.248 and 2.12389) GeV  
34 > (-175.908 and 1.99716) GeV  
35 > (-174.617 and 1.88107) GeV  
36 > (-173.371 and 1.77447) GeV  
37 > (-172.168 and 1.67637) GeV  
38 > (-171.006 and 1.58592) GeV  
39 > (-169.881 and 1.50235) GeV  
40 > (-168.792 and 1.42499) GeV  
41 > (-167.737 and 1.35325) GeV  
42 > (-166.714 and 1.28662) GeV  
43 > (-165.722 and 1.22461) GeV  
44 > (-164.758 and 1.16684) GeV  
45 > (-163.821 and 1.11291) GeV  
46 > (-162.91 and 1.06252) GeV  
47 > (-162.024 and 1.01535) GeV  
48 > (-161.161 and 0.971147) GeV  
49 > (-160.321 and 0.92967) GeV  
50 > (-159.502 and 0.890704) GeV  
51 > (-158.703 and 0.854053) GeV  
52 > (-157.924 and 0.819541) GeV  
53 > (-157.164 and 0.787007) GeV  
54 > (-156.421 and 0.756306) GeV  
55 > (-155.696 and 0.727304) GeV  
56 > (-154.987 and 0.699882) GeV  
57 > (-154.294 and 0.673928) GeV  
58 > (-153.616 and 0.649342) GeV

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59 > (-152.953 and 0.62603) GeV  
60 > (-152.304 and 0.603907) GeV  
61 > (-151.668 and 0.582897) GeV  
62 > (-151.045 and 0.562925) GeV  
63 > (-150.435 and 0.543927) GeV  
64 > (-149.837 and 0.525842) GeV  
65 > (-149.25 and 0.508612) GeV  
66 > (-148.675 and 0.492186) GeV  
67 > (-148.111 and 0.476515) GeV  
68 > (-147.557 and 0.461554) GeV  
69 > (-147.013 and 0.447263) GeV  
70 > (-146.48 and 0.433602) GeV  
71 > (-145.955 and 0.420535) GeV  
72 > (-145.44 and 0.40803) GeV  
73 > (-144.934 and 0.396055) GeV  
74 > (-144.437 and 0.38458) GeV  
75 > (-143.948 and 0.37358) GeV  
76 > (-143.467 and 0.363029) GeV  
77 > (-142.994 and 0.352902) GeV  
78 > (-142.529 and 0.343179) GeV  
79 > (-142.071 and 0.333837) GeV  
80 > (-141.621 and 0.324859) GeV  
81 > (-141.177 and 0.316225) GeV  
82 > (-140.74 and 0.307919) GeV  
83 > (-140.31 and 0.299924) GeV  
84 > (-139.887 and 0.292226) GeV  
85 > (-139.47 and 0.28481) GeV  
86 > (-139.059 and 0.277662) GeV  
87 > (-138.653 and 0.270771) GeV  
88 > (-138.254 and 0.264124) GeV  
89 > (-137.861 and 0.25771) GeV  
90 > (-137.472 and 0.251519) GeV  
91 > (-137.09 and 0.24554) GeV  
92 > (-136.712 and 0.239765) GeV  
93 > (-136.34 and 0.234183) GeV  
94 > (-135.973 and 0.228788) GeV  
95 > (-135.61 and 0.22357) GeV  
96 > (-135.253 and 0.218522) GeV  
97 > (-134.9 and 0.213637) GeV  
98 > (-134.551 and 0.208909) GeV  
99 > (-134.207 and 0.20433) GeV  
100 > (-133.868 and 0.199894) GeV  
101 > (-133.532 and 0.195597) GeV  
102 > (-133.201 and 0.191431) GeV  
103 > (-132.874 and 0.187393) GeV  
104 > (-132.551 and 0.183476) GeV  
105 > (-132.232 and 0.179676) GeV  
106 > (-131.916 and 0.17599) GeV  
107 > (-131.604 and 0.172411) GeV  
108 > (-131.296 and 0.168936) GeV  
109 > (-130.992 and 0.165562) GeV  
110 > (-130.691 and 0.162285) GeV  
111 > (-130.393 and 0.1591) GeV  
112 > (-130.099 and 0.156004) GeV  
113 > (-129.808 and 0.152995) GeV  
114 > (-129.52 and 0.150069) GeV  
115 > (-129.235 and 0.147223) GeV  
116 > (-128.954 and 0.144455) GeV

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117 > (-128.675 and 0.141761) GeV  
118 > (-128.4 and 0.139139) GeV  
119 > (-128.127 and 0.136586) GeV  
120 > (-127.858 and 0.134101) GeV  
121 > (-127.591 and 0.13168) GeV  
122 > (-127.327 and 0.129322) GeV  
123 > (-127.065 and 0.127025) GeV  
124 > (-126.806 and 0.124786) GeV  
125 > (-126.55 and 0.122603) GeV  
126 > (-126.297 and 0.120476) GeV  
127 > (-126.046 and 0.118401) GeV  
128 > (-125.797 and 0.116377) GeV  
129 > (-125.551 and 0.114403) GeV  
130 > (-125.307 and 0.112477) GeV  
131 > (-125.066 and 0.110598) GeV  
132 > (-124.826 and 0.108763) GeV  
133 > (-124.59 and 0.106972) GeV  
134 > (-124.355 and 0.105224) GeV  
135 > (-124.123 and 0.103516) GeV  
136 > (-123.892 and 0.101848) GeV  
137 > (-123.664 and 0.100219) GeV  
138 > (-123.438 and 0.0986268) GeV  
139 > (-123.214 and 0.0970711) GeV  
140 > (-122.992 and 0.0955507) GeV  
141 > (-122.772 and 0.0940643) GeV  
142 > (-122.554 and 0.0926112) GeV  
143 > (-122.338 and 0.0911902) GeV  
144 > (-122.123 and 0.0898005) GeV  
145 > (-121.911 and 0.0884413) GeV  
146 > (-121.701 and 0.0871115) GeV  
147 > (-121.492 and 0.0858104) GeV  
148 > (-121.285 and 0.0845372) GeV  
149 > (-121.08 and 0.0832911) GeV  
150 > (-120.876 and 0.0820714) GeV  
151 > (-120.674 and 0.0808773) GeV  
152 > (-120.474 and 0.0797081) GeV  
153 > (-120.276 and 0.0785632) GeV  
154 > (-120.079 and 0.0774419) GeV  
155 > (-119.883 and 0.0763435) GeV  
156 > (-119.69 and 0.0752675) GeV  
157 > (-119.498 and 0.0742133) GeV  
158 > (-119.307 and 0.0731803) GeV  
159 > (-119.118 and 0.0721679) GeV  
160 > (-118.93 and 0.0711756) GeV  
161 > (-118.744 and 0.070203) GeV  
162 > (-118.559 and 0.0692494) GeV  
163 > (-118.376 and 0.0683144) GeV  
164 > (-118.194 and 0.0673975) GeV  
165 > (-118.014 and 0.0664983) GeV  
166 > (-117.835 and 0.0656163) GeV  
167 > (-117.657 and 0.0647511) GeV  
168 > (-117.481 and 0.0639023) GeV  
169 > (-117.305 and 0.0630695) GeV  
170 > (-117.132 and 0.0622522) GeV  
171 > (-116.959 and 0.0614502) GeV  
172 > (-116.788 and 0.060663) GeV  
173 > (-116.618 and 0.0598903) GeV  
174 > (-116.449 and 0.0591317) GeV

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175 > (-116.281 and 0.058387) GeV  
176 > (-116.115 and 0.0576557) GeV  
177 > (-115.95 and 0.0569375) GeV  
178 > (-115.786 and 0.0562322) GeV  
179 > (-115.623 and 0.0555395) GeV  
180 > (-115.461 and 0.054859) GeV  
181 > (-115.301 and 0.0541905) GeV  
182 > (-115.141 and 0.0535337) GeV  
183 > (-114.983 and 0.0528884) GeV  
184 > (-114.825 and 0.0522542) GeV  
185 > (-114.669 and 0.0516309) GeV  
186 > (-114.514 and 0.0510183) GeV  
187 > (-114.36 and 0.0504162) GeV  
188 > (-114.207 and 0.0498243) GeV  
189 > (-114.055 and 0.0492423) GeV  
190 > (-113.904 and 0.0486702) GeV  
191 > (-113.753 and 0.0481075) GeV  
192 > (-113.604 and 0.0475543) GeV  
193 > (-113.456 and 0.0470101) GeV  
194 > (-113.309 and 0.046475) GeV  
195 > (-113.163 and 0.0459485) GeV  
196 > (-113.017 and 0.0454307) GeV  
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198 > (-112.73 and 0.04442) GeV  
199 > (-112.587 and 0.0439267) GeV  
200 > (-112.445 and 0.0434414) GeV  
201 > (-112.305 and 0.0429638) GeV  
202 > (-112.165 and 0.0424937) GeV  
203 > (-112.026 and 0.042031) GeV  
204 > (-111.888 and 0.0415755) GeV  
205 > (-111.75 and 0.0411272) GeV  
206 > (-111.614 and 0.0406858) GeV  
207 > (-111.478 and 0.0402512) GeV  
208 > (-111.343 and 0.0398232) GeV  
209 > (-111.209 and 0.0394018) GeV  
210 > (-111.076 and 0.0389869) GeV  
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213 > (-110.681 and 0.0377792) GeV  
214 > (-110.551 and 0.0373886) GeV  
215 > (-110.422 and 0.0370038) GeV  
216 > (-110.293 and 0.0366248) GeV  
217 > (-110.165 and 0.0362513) GeV  
218 > (-110.038 and 0.0358833) GeV  
219 > (-109.912 and 0.0355206) GeV  
220 > (-109.786 and 0.0351632) GeV  
221 > (-109.661 and 0.034811) GeV  
222 > (-109.537 and 0.0344639) GeV  
223 > (-109.414 and 0.0341218) GeV  
224 > (-109.291 and 0.0337845) GeV  
225 > (-109.169 and 0.033452) GeV  
226 > (-109.047 and 0.0331243) GeV  
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228 > (-108.806 and 0.0324825) GeV  
229 > (-108.687 and 0.0321683) GeV  
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231 > (-108.45 and 0.0315531) GeV  
232 > (-108.332 and 0.0312518) GeV

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233 > (-108.215 and 0.0309546) GeV  
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290 > (-102.434 and 0.0190254) GeV

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649 > (-83.7111 and 0.00314586) GeV  
650 > (-83.6789 and 0.00313503) GeV  
651 > (-83.6466 and 0.00312425) GeV  
652 > (-83.6145 and 0.00311353) GeV  
653 > (-83.5824 and 0.00310286) GeV  
654 > (-83.5504 and 0.00309225) GeV  
655 > (-83.5185 and 0.00308168) GeV  
656 > (-83.4866 and 0.00307117) GeV  
657 > (-83.4547 and 0.00306071) GeV  
658 > (-83.423 and 0.0030503) GeV  
659 > (-83.3912 and 0.00303995) GeV  
660 > (-83.3596 and 0.00302964) GeV  
661 > (-83.328 and 0.00301938) GeV  
662 > (-83.2965 and 0.00300918) GeV  
663 > (-83.265 and 0.00299902) GeV  
664 > (-83.2336 and 0.00298891) GeV  
665 > (-83.2022 and 0.00297886) GeV  
666 > (-83.1709 and 0.00296885) GeV  
667 > (-83.1397 and 0.00295889) GeV  
668 > (-83.1085 and 0.00294897) GeV  
669 > (-83.0774 and 0.00293911) GeV  
670 > (-83.0463 and 0.00292929) GeV  
671 > (-83.0153 and 0.00291952) GeV  
672 > (-82.9844 and 0.0029098) GeV  
673 > (-82.9535 and 0.00290012) GeV  
674 > (-82.9227 and 0.00289049) GeV  
675 > (-82.8919 and 0.00288091) GeV  
676 > (-82.8612 and 0.00287137) GeV  
677 > (-82.8305 and 0.00286188) GeV  
678 > (-82.7999 and 0.00285243) GeV  
679 > (-82.7694 and 0.00284303) GeV  
680 > (-82.7389 and 0.00283367) GeV  
681 > (-82.7084 and 0.00282436) GeV  
682 > (-82.6781 and 0.00281509) GeV  
683 > (-82.6477 and 0.00280587) GeV  
684 > (-82.6175 and 0.00279669) GeV  
685 > (-82.5873 and 0.00278755) GeV  
686 > (-82.5571 and 0.00277846) GeV  
687 > (-82.527 and 0.0027694) GeV  
688 > (-82.497 and 0.00276039) GeV  
689 > (-82.467 and 0.00275143) GeV  
690 > (-82.437 and 0.0027425) GeV  
691 > (-82.4071 and 0.00273362) GeV  
692 > (-82.3773 and 0.00272478) GeV  
693 > (-82.3475 and 0.00271598) GeV  
694 > (-82.3178 and 0.00270722) GeV  
695 > (-82.2881 and 0.0026985) GeV  
696 > (-82.2585 and 0.00268982) GeV

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697 > (-82.229 and 0.00268118) GeV  
698 > (-82.1995 and 0.00267258) GeV  
699 > (-82.17 and 0.00266402) GeV  
700 > (-82.1406 and 0.00265551) GeV  
701 > (-82.1113 and 0.00264703) GeV  
702 > (-82.082 and 0.00263859) GeV  
703 > (-82.0527 and 0.00263018) GeV  
704 > (-82.0235 and 0.00262182) GeV  
705 > (-81.9944 and 0.0026135) GeV  
706 > (-81.9653 and 0.00260521) GeV  
707 > (-81.9362 and 0.00259696) GeV  
708 > (-81.9073 and 0.00258875) GeV  
709 > (-81.8783 and 0.00258058) GeV  
710 > (-81.8494 and 0.00257244) GeV  
711 > (-81.8206 and 0.00256434) GeV  
712 > (-81.7918 and 0.00255628) GeV  
713 > (-81.7631 and 0.00254825) GeV  
714 > (-81.7344 and 0.00254026) GeV  
715 > (-81.7058 and 0.00253231) GeV  
716 > (-81.6772 and 0.00252439) GeV  
717 > (-81.6487 and 0.00251651) GeV  
718 > (-81.6202 and 0.00250866) GeV  
719 > (-81.5917 and 0.00250085) GeV  
720 > (-81.5634 and 0.00249308) GeV  
721 > (-81.535 and 0.00248534) GeV  
722 > (-81.5067 and 0.00247763) GeV  
723 > (-81.4785 and 0.00246996) GeV  
724 > (-81.4503 and 0.00246232) GeV  
725 > (-81.4222 and 0.00245472) GeV  
726 > (-81.3941 and 0.00244715) GeV  
727 > (-81.366 and 0.00243961) GeV  
728 > (-81.338 and 0.00243211) GeV  
729 > (-81.3101 and 0.00242464) GeV  
730 > (-81.2822 and 0.0024172) GeV  
731 > (-81.2544 and 0.0024098) GeV  
732 > (-81.2266 and 0.00240243) GeV  
733 > (-81.1988 and 0.00239509) GeV  
734 > (-81.1711 and 0.00238778) GeV  
735 > (-81.1434 and 0.00238051) GeV  
736 > (-81.1158 and 0.00237327) GeV  
737 > (-81.0883 and 0.00236606) GeV  
738 > (-81.0607 and 0.00235888) GeV  
739 > (-81.0333 and 0.00235173) GeV  
740 > (-81.0058 and 0.00234462) GeV  
741 > (-80.9785 and 0.00233753) GeV  
742 > (-80.9511 and 0.00233048) GeV  
743 > (-80.9238 and 0.00232346) GeV  
744 > (-80.8966 and 0.00231646) GeV  
745 > (-80.8694 and 0.0023095) GeV  
746 > (-80.8422 and 0.00230257) GeV  
747 > (-80.8151 and 0.00229567) GeV  
748 > (-80.7881 and 0.0022888) GeV  
749 > (-80.7611 and 0.00228195) GeV  
750 > (-80.7341 and 0.00227514) GeV  
751 > (-80.7072 and 0.00226836) GeV  
752 > (-80.6803 and 0.0022616) GeV  
753 > (-80.6535 and 0.00225488) GeV  
754 > (-80.6267 and 0.00224818) GeV

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755 > (-80.5999 and 0.00224151) GeV  
756 > (-80.5732 and 0.00223487) GeV  
757 > (-80.5466 and 0.00222826) GeV  
758 > (-80.52 and 0.00222168) GeV  
759 > (-80.4934 and 0.00221513) GeV  
760 > (-80.4669 and 0.0022086) GeV  
761 > (-80.4404 and 0.0022021) GeV  
762 > (-80.4139 and 0.00219563) GeV  
763 > (-80.3875 and 0.00218918) GeV  
764 > (-80.3612 and 0.00218277) GeV  
765 > (-80.3349 and 0.00217638) GeV  
766 > (-80.3086 and 0.00217002) GeV  
767 > (-80.2824 and 0.00216368) GeV  
768 > (-80.2562 and 0.00215737) GeV  
769 > (-80.2301 and 0.00215109) GeV  
770 > (-80.204 and 0.00214483) GeV  
771 > (-80.1779 and 0.0021386) GeV  
772 > (-80.1519 and 0.0021324) GeV  
773 > (-80.126 and 0.00212622) GeV  
774 > (-80.1 and 0.00212007) GeV  
775 > (-80.0741 and 0.00211394) GeV  
776 > (-80.0483 and 0.00210784) GeV  
777 > (-80.0225 and 0.00210177) GeV  
778 > (-79.9967 and 0.00209572) GeV  
779 > (-79.971 and 0.00208969) GeV  
780 > (-79.9454 and 0.00208369) GeV  
781 > (-79.9197 and 0.00207772) GeV  
782 > (-79.8941 and 0.00207176) GeV  
783 > (-79.8686 and 0.00206584) GeV  
784 > (-79.8431 and 0.00205994) GeV  
785 > (-79.8176 and 0.00205406) GeV  
786 > (-79.7922 and 0.00204821) GeV  
787 > (-79.7668 and 0.00204238) GeV  
788 > (-79.7414 and 0.00203657) GeV  
789 > (-79.7161 and 0.00203079) GeV  
790 > (-79.6908 and 0.00202504) GeV  
791 > (-79.6656 and 0.0020193) GeV  
792 > (-79.6404 and 0.00201359) GeV  
793 > (-79.6153 and 0.0020079) GeV  
794 > (-79.5902 and 0.00200224) GeV  
795 > (-79.5651 and 0.0019966) GeV  
796 > (-79.5401 and 0.00199098) GeV  
797 > (-79.5151 and 0.00198539) GeV  
798 > (-79.4901 and 0.00197981) GeV  
799 > (-79.4652 and 0.00197426) GeV  
800 > (-79.4403 and 0.00196874) GeV  
801 > (-79.4155 and 0.00196323) GeV  
802 > (-79.3907 and 0.00195775) GeV  
803 > (-79.3659 and 0.00195229) GeV  
804 > (-79.3412 and 0.00194685) GeV  
805 > (-79.3165 and 0.00194143) GeV  
806 > (-79.2919 and 0.00193603) GeV  
807 > (-79.2673 and 0.00193066) GeV  
808 > (-79.2427 and 0.00192531) GeV  
809 > (-79.2182 and 0.00191998) GeV  
810 > (-79.1937 and 0.00191467) GeV  
811 > (-79.1692 and 0.00190938) GeV  
812 > (-79.1448 and 0.00190411) GeV

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813 > (-79.1204 and 0.00189887) GeV  
814 > (-79.0961 and 0.00189364) GeV  
815 > (-79.0718 and 0.00188844) GeV  
816 > (-79.0475 and 0.00188325) GeV  
817 > (-79.0233 and 0.00187809) GeV  
818 > (-78.9991 and 0.00187295) GeV  
819 > (-78.975 and 0.00186782) GeV  
820 > (-78.9508 and 0.00186272) GeV  
821 > (-78.9268 and 0.00185764) GeV  
822 > (-78.9027 and 0.00185258) GeV  
823 > (-78.8787 and 0.00184753) GeV  
824 > (-78.8547 and 0.00184251) GeV  
825 > (-78.8308 and 0.00183751) GeV  
826 > (-78.8069 and 0.00183252) GeV  
827 > (-78.783 and 0.00182756) GeV  
828 > (-78.7592 and 0.00182262) GeV  
829 > (-78.7354 and 0.00181769) GeV  
830 > (-78.7117 and 0.00181278) GeV  
831 > (-78.688 and 0.0018079) GeV  
832 > (-78.6643 and 0.00180303) GeV  
833 > (-78.6406 and 0.00179818) GeV  
834 > (-78.617 and 0.00179335) GeV  
835 > (-78.5934 and 0.00178854) GeV  
836 > (-78.5699 and 0.00178375) GeV  
837 > (-78.5464 and 0.00177897) GeV  
838 > (-78.5229 and 0.00177422) GeV  
839 > (-78.4995 and 0.00176948) GeV  
840 > (-78.4761 and 0.00176476) GeV  
841 > (-78.4527 and 0.00176006) GeV  
842 > (-78.4294 and 0.00175537) GeV  
843 > (-78.4061 and 0.00175071) GeV  
844 > (-78.3828 and 0.00174606) GeV  
845 > (-78.3596 and 0.00174143) GeV  
846 > (-78.3364 and 0.00173682) GeV  
847 > (-78.3132 and 0.00173223) GeV  
848 > (-78.2901 and 0.00172765) GeV  
849 > (-78.267 and 0.00172309) GeV  
850 > (-78.244 and 0.00171855) GeV  
851 > (-78.221 and 0.00171403) GeV  
852 > (-78.198 and 0.00170952) GeV  
853 > (-78.175 and 0.00170503) GeV  
854 > (-78.1521 and 0.00170055) GeV  
855 > (-78.1292 and 0.0016961) GeV  
856 > (-78.1063 and 0.00169166) GeV  
857 > (-78.0835 and 0.00168724) GeV  
858 > (-78.0607 and 0.00168283) GeV  
859 > (-78.038 and 0.00167844) GeV  
860 > (-78.0153 and 0.00167407) GeV  
861 > (-77.9926 and 0.00166971) GeV  
862 > (-77.9699 and 0.00166537) GeV  
863 > (-77.9473 and 0.00166105) GeV  
864 > (-77.9247 and 0.00165674) GeV  
865 > (-77.9021 and 0.00165245) GeV  
866 > (-77.8796 and 0.00164817) GeV  
867 > (-77.8571 and 0.00164391) GeV  
868 > (-77.8347 and 0.00163967) GeV  
869 > (-77.8122 and 0.00163544) GeV  
870 > (-77.7899 and 0.00163123) GeV

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871 > (-77.7675 and 0.00162703) GeV  
872 > (-77.7452 and 0.00162285) GeV  
873 > (-77.7229 and 0.00161869) GeV  
874 > (-77.7006 and 0.00161454) GeV  
875 > (-77.6784 and 0.0016104) GeV  
876 > (-77.6562 and 0.00160629) GeV  
877 > (-77.634 and 0.00160218) GeV  
878 > (-77.6118 and 0.00159809) GeV  
879 > (-77.5897 and 0.00159402) GeV  
880 > (-77.5677 and 0.00158996) GeV  
881 > (-77.5456 and 0.00158592) GeV  
882 > (-77.5236 and 0.00158189) GeV  
883 > (-77.5016 and 0.00157787) GeV  
884 > (-77.4797 and 0.00157387) GeV  
885 > (-77.4577 and 0.00156989) GeV  
886 > (-77.4359 and 0.00156592) GeV  
887 > (-77.414 and 0.00156196) GeV  
888 > (-77.3922 and 0.00155802) GeV  
889 > (-77.3704 and 0.00155409) GeV  
890 > (-77.3486 and 0.00155018) GeV  
891 > (-77.3269 and 0.00154628) GeV  
892 > (-77.3052 and 0.0015424) GeV  
893 > (-77.2835 and 0.00153853) GeV  
894 > (-77.2618 and 0.00153467) GeV  
895 > (-77.2402 and 0.00153083) GeV  
896 > (-77.2187 and 0.001527) GeV  
897 > (-77.1971 and 0.00152318) GeV  
898 > (-77.1756 and 0.00151938) GeV  
899 > (-77.1541 and 0.00151559) GeV  
900 > (-77.1326 and 0.00151182) GeV  
901 > (-77.1112 and 0.00150806) GeV  
902 > (-77.0898 and 0.00150431) GeV  
903 > (-77.0684 and 0.00150058) GeV  
904 > (-77.0471 and 0.00149686) GeV  
905 > (-77.0257 and 0.00149315) GeV  
906 > (-77.0045 and 0.00148946) GeV  
907 > (-76.9832 and 0.00148578) GeV  
908 > (-76.962 and 0.00148211) GeV  
909 > (-76.9408 and 0.00147846) GeV  
910 > (-76.9196 and 0.00147482) GeV  
911 > (-76.8985 and 0.00147119) GeV  
912 > (-76.8774 and 0.00146757) GeV  
913 > (-76.8563 and 0.00146397) GeV  
914 > (-76.8352 and 0.00146038) GeV  
915 > (-76.8142 and 0.00145681) GeV  
916 > (-76.7932 and 0.00145324) GeV  
917 > (-76.7722 and 0.00144969) GeV  
918 > (-76.7513 and 0.00144615) GeV  
919 > (-76.7304 and 0.00144262) GeV  
920 > (-76.7095 and 0.00143911) GeV  
921 > (-76.6886 and 0.00143561) GeV  
922 > (-76.6678 and 0.00143212) GeV  
923 > (-76.647 and 0.00142864) GeV  
924 > (-76.6263 and 0.00142518) GeV  
925 > (-76.6055 and 0.00142172) GeV  
926 > (-76.5848 and 0.00141828) GeV  
927 > (-76.5641 and 0.00141485) GeV  
928 > (-76.5435 and 0.00141144) GeV

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929 > (-76.5228 and 0.00140803) GeV  
930 > (-76.5022 and 0.00140464) GeV  
931 > (-76.4817 and 0.00140126) GeV  
932 > (-76.4611 and 0.00139789) GeV  
933 > (-76.4406 and 0.00139453) GeV  
934 > (-76.4201 and 0.00139118) GeV  
935 > (-76.3996 and 0.00138785) GeV  
936 > (-76.3792 and 0.00138452) GeV  
937 > (-76.3588 and 0.00138121) GeV  
938 > (-76.3384 and 0.00137791) GeV  
939 > (-76.3181 and 0.00137462) GeV  
940 > (-76.2977 and 0.00137134) GeV  
941 > (-76.2774 and 0.00136808) GeV  
942 > (-76.2572 and 0.00136482) GeV  
943 > (-76.2369 and 0.00136158) GeV  
944 > (-76.2167 and 0.00135835) GeV  
945 > (-76.1965 and 0.00135512) GeV  
946 > (-76.1763 and 0.00135191) GeV  
947 > (-76.1562 and 0.00134871) GeV  
948 > (-76.1361 and 0.00134552) GeV  
949 > (-76.116 and 0.00134235) GeV  
950 > (-76.096 and 0.00133918) GeV  
951 > (-76.0759 and 0.00133602) GeV  
952 > (-76.0559 and 0.00133288) GeV  
953 > (-76.0359 and 0.00132974) GeV  
954 > (-76.016 and 0.00132662) GeV  
955 > (-75.996 and 0.0013235) GeV  
956 > (-75.9761 and 0.0013204) GeV  
957 > (-75.9563 and 0.00131731) GeV  
958 > (-75.9364 and 0.00131423) GeV  
959 > (-75.9166 and 0.00131115) GeV  
960 > (-75.8968 and 0.00130809) GeV  
961 > (-75.877 and 0.00130504) GeV  
962 > (-75.8573 and 0.001302) GeV  
963 > (-75.8376 and 0.00129897) GeV  
964 > (-75.8179 and 0.00129595) GeV  
965 > (-75.7982 and 0.00129294) GeV  
966 > (-75.7786 and 0.00128994) GeV  
967 > (-75.7589 and 0.00128695) GeV  
968 > (-75.7393 and 0.00128397) GeV  
969 > (-75.7198 and 0.001281) GeV  
970 > (-75.7002 and 0.00127804) GeV  
971 > (-75.6807 and 0.00127509) GeV  
972 > (-75.6612 and 0.00127215) GeV  
973 > (-75.6418 and 0.00126922) GeV  
974 > (-75.6223 and 0.0012663) GeV  
975 > (-75.6029 and 0.00126338) GeV  
976 > (-75.5835 and 0.00126048) GeV  
977 > (-75.5641 and 0.00125759) GeV  
978 > (-75.5448 and 0.00125471) GeV  
979 > (-75.5255 and 0.00125183) GeV  
980 > (-75.5062 and 0.00124897) GeV  
981 > (-75.4869 and 0.00124612) GeV  
982 > (-75.4677 and 0.00124327) GeV  
983 > (-75.4484 and 0.00124044) GeV  
984 > (-75.4293 and 0.00123761) GeV  
985 > (-75.4101 and 0.00123479) GeV  
986 > (-75.3909 and 0.00123199) GeV

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987 > (-75.3718 and 0.00122919) GeV  
 988 > (-75.3527 and 0.0012264) GeV  
 989 > (-75.3336 and 0.00122362) GeV  
 990 > (-75.3146 and 0.00122085) GeV  
 991 > (-75.2956 and 0.00121809) GeV  
 992 > (-75.2766 and 0.00121534) GeV  
 993 > (-75.2576 and 0.00121259) GeV  
 994 > (-75.2386 and 0.00120986) GeV  
 995 > (-75.2197 and 0.00120713) GeV  
 996 > (-75.2008 and 0.00120441) GeV  
 997 > (-75.1819 and 0.00120171) GeV  
 998 > (-75.1631 and 0.00119901) GeV  
 999 > (-75.1442 and 0.00119632) GeV

[Program finished]

4d origin of  $dE = 4\sqrt{(gM^2)/\sqrt{2}} \sim 125.5673374143954990316092809188$  GeV ( $(gM^2) = 1393.6328858707575005182839547884$  GeV $^2$ ) (conf) [6,7].

Possibility of obtaining any mass of massive boson-massive graviton and masses lower than those of neutrinos and which can come from fluctuations of energies of the quantum vacuum [8,9].

### 1.5. A Less and Less Spin 0 Particles

(4) Example 1 :  $dE = 4\sqrt{\frac{gM^2}{\sqrt{2}}} \sim 125.5673374143954990316092809188$  GeV ( $gM^2 = 1393.6328858707575005182839547884$  GeV $^2$ ) [10-14].

The particle at exactly some 125 GeV

And spin

$1+1+1-1 = 2$  (As a frequent Space-Time reflect)

or

$1-1+1-1 = 0$

Fusion of 4 identical particles that are to disappear spontaneously or after one wave length: A single 4d-String appearing and disappearing spontaneously ( $Dt \leq 0$ ) [10-12,14,15].

It si obtain a dark energy\massive gravitons that it is emitted to long distances because of higher values for  $\Delta k_3 = dk_{3d}$

Dark matter\massive gravitons that it is emitted to short distances because of lesser values for  $\Delta k_3 = dk_{3n}$

Algorithm to find  $\Delta k_3 = dk_{3d}$

We set  $dE = h*C/L$

$L \sim 2.5$  kpc =  $7.7142*10^{19}$  m

(1 pc =  $3.086*10^{13}$  kilomètres)

$h = 6.62607004*10^{(-34)}$  m $^2$ kg/s

$C = 299792458$  m/s

$dE = 6.62607004*10^{(-34)}*299792458/(7.7142*10^{19}) = 2.575050976344609*10^{(-45)}$  joules =  $1.607219735509044*10^{(-35)}$  GeV

```
block(dE: 1.607219735509044*10-35,
gM : sqrt(1393.6328858707575005182839547884),
find_root(dE = 2^(7/4)*gM*sqrt((k3+1)/(k3*sqrt(2*k3+2))),k3,10,10150)
→ k3 = 1.862840706286786*10147 (Obtaining of k3min for dark matter effect\massive graviton.)
```

Dark matter\massive gravitons that it is emitted to short distances because of lesser values for  $\Delta k_3 = dk_{3n} = k_3 = 1.862840706286786*10^{147}$

→ Dark energy\massive gravitons that it is emitted to long distances because of higher values for  $\Delta k_3 = dk_{3d}$

#### 1.5.1. Algorithm

from math import\*

---

#An algorithm giving sets of massive bosons-dark energy: {dE[k3] = 2^(7/4)\*gM\*sqrt((k3d+1)/(k3n\*sqrt(2\*k3d+2))), k3d = 1+n.  
dk3d}

#and sets of massive bosons-dark matter: {dE[k3] = 2^(7/4)\*gM\*sqrt((k3n+1)/(k3d\*sqrt(2\*k3n+2))), k3n = 1+n.dk3n}  
gM = sqrt(1393.6328858707575005182839547884)

for q in range (1,300 + 1):

Sidn = 0

Sidd = 0

tmax = 10\*\*10\*\*q

dk3n = 1.255314934818507\*10\*\*89

dk3d = 1.862840706286786\*10\*\*147

d0 = 1.862840706286786\*10\*\*147

for t0 in range(1,10000 + 1) :

if d0 > 10\*\*(-3)\*1.862840706286786\*10\*\*147 :

Sidn = 0

Sidd = 0

k3n = 1.862840706286786\*10\*\*147

k3d = 1.862840706286786\*10\*\*147

for t in range(1, tmax + 1) :

fiEk3n = 2\*\*^(7/4)\*sqrt((k3n+1)/(k3n\*sqrt(2\*k3n+2)))

fiEk3d = 2\*\*^(7/4)\*sqrt((k3d+1)/(k3d\*sqrt(2\*k3d+2)))

Sidn = fiEk3n\*dk3n + Sidn

Sidd = fiEk3d\*dk3d + Sidd

k3n = k3n+dk3n

k3d = k3d+dk3d

if t == tmax :

if (Sidd/Sidn >= 3 and Sidd/Sidn < 4):

k3n = k3n-dk3n

k3d = k3d-dk3d

dEd = 2\*\*^(7/4)\*gM\*sqrt((dk3d+1)/(dk3d\*sqrt(2\*dk3d+2)))

print("dk3n = ",dk3n, ", dk3d = ",dk3d, ", dEd = ",dEd," GeV")

dk3d = dk3d-d0

d0 = d0/10

elif Sidd/Sidn < 3:

k3n = k3n-dk3n

k3d = k3d-dk3d

dk3d = dk3d+d0

elif Sidd/Sidn >= 4:

k3n = k3n-dk3n

k3d = k3d-dk3d

dk3d : dk3d-d0/10

→ ... ....

((q = 1, dk3n = 1.255314934818507\*10\*\*89, dk3d = 1.255314934818507\*10\*\*89, d0 = 1.255314934818507\*10\*\*89 and d0 > 10\*\*(-3)\*1.255314934818507\*10\*\*89)

→ dk3n=1.255314934818507\*10^89, {dk3d=4.895728245792177\*10^89, dEd=1.6072197 35509 044\*10^(-35) GeV}

dk3n=1.255314934818507\*10^89, {dk3d=3.891476297937371\*10^89, dEd=1.60721973550904 4\*10^(-35) GeV}

dk3n=1.255314934818507\*10^89, {dk3d=3.778497953803705\*10^89, dEd=1.60721973550904 4\*10^(-35) GeV}

[Program finished]

Example with: {for dk in range (1,50 + 1):

tmax = 1000

for t0 in range(1,1000 + 1) :}

→ dk3n=1.0 dk3d=5.0

dk3n=1.0 dk3d=float(22/5)=4.4

---

```
dk3n=1.0 dk3d=float(433/100)=4.33
dk3n=2.0 dk3d=9.0
dk3n=2.0 dk3d=float(87/10)=8.7
dk3n=2.0 dk3d=float(863/100)=8.63
dk3n=3.0 dk3d=13.0
dk3n=3.0 dk3d=13.0
dk3n=3.0 dk3d=float(1293/100)=12.93
dk3n=4.0 dk3d=18.0
dk3n=4.0 dk3d=float(173/10)=17.3
dk3n=4.0 dk3d=float(1723/100)=17.23
dk3n=5.0 dk3d=22.0
dk3n=5.0 dk3d=float(108/5)=21.6
dk3n=5.0 dk3d=float(1077/50)=21.54
dk3n=6.0 dk3d=26.0
dk3n=6.0 dk3d=float(259/10)=25.9
dk3n=6.0 dk3d=float(646/25)=25.84
dk3n=7.0 dk3d=31.0
dk3n=7.0 dk3d=float(151/5)=30.2
dk3n=7.0 dk3d=float(1507/50)=30.14
dk3n=8.0 dk3d=35.0
dk3n=8.0 dk3d=float(69/2)=34.5
dk3n=8.0 dk3d=float(861/25)=34.44
dk3n=9.0 dk3d=39.0
dk3n=9.0 dk3d=float(194/5)=38.8
dk3n=9.0 dk3d=float(1937/50)=38.74
dk3n=10.0 dk3d=44.0
dk3n=10.0 dk3d=float(431/10)=43.1
dk3n=10.0 dk3d=float(1076/25)=43.04
dk3n=11.0 dk3d=48.0
dk3n=11.0 dk3d=float(237/5)=47.4
dk3n=11.0 dk3d=float(2367/50)=47.34
dk3n=12.0 dk3d=float(52)=52.0
dk3n=12.0 dk3d=float(517/10)=51.7
dk3n=12.0 dk3d=float(1291/25)=51.64
dk3n=13.0 dk3d=float(56)=56.0
dk3n=13.0 dk3d=float(56)=56.0
dk3n=13.0 dk3d=float(1119/20)=55.95
dk3n=14.0 dk3d=float(61)=61.0
dk3n=14.0 dk3d=float(603/10)=60.3
dk3n=14.0 dk3d=float(241/4)=60.25
dk3n=15.0 dk3d=float(65)=65.0
dk3n=15.0 dk3d=float(323/5)=64.6
dk3n=15.0 dk3d=float(1291/20)=64.55
dk3n=16.0 dk3d=float(69)=69.0
dk3n=16.0 dk3d=float(689/10)=68.9
dk3n=16.0 dk3d=float(1377/20)=68.85
dk3n=17.0 dk3d=float(74)=74.0
dk3n=17.0 dk3d=float(366/5)=73.2
dk3n=17.0 dk3d=float(1463/20)=73.15
dk3n=18.0 dk3d=float(78)=78.0
dk3n=18.0 dk3d=float(155/2)=77.5
dk3n=18.0 dk3d=float(1549/20)=77.45
dk3n=19.0 dk3d=float(82)=82.0
dk3n=19.0 dk3d=float(409/5)=81.8
dk3n=19.0 dk3d=float(327/4)=81.75
dk3n=20.0 dk3d=float(87)=87.0
dk3n=20.0 dk3d=float(861/10)=86.1
dk3n=20.0 dk3d=float(4303/50)=86.06
```

---

```
dk3n=21.0 dk3d=float(91)=91.0
dk3n=21.0 dk3d=float(452/5)=90.4
dk3n=21.0 dk3d=float(2259/25)=90.36
dk3n=22.0 dk3d=float(95)=95.0
dk3n=22.0 dk3d=float(947/10)=94.7
dk3n=22.0 dk3d=float(4733/50)=94.66
dk3n=23.0 dk3d=float(99)=99.0
dk3n=23.0 dk3d=float(99)=99.0
dk3n=23.0 dk3d=float(2474/25)=98.96
dk3n=24.0 dk3d=float(104)=104.0
dk3n=24.0 dk3d=float(1033/10)=103.3
dk3n=24.0 dk3d=float(5163/50)=103.26
dk3n=25.0 dk3d=float(108)=108.0
dk3n=25.0 dk3d=float(538/5)=107.6
dk3n=25.0 dk3d=float(2689/25)=107.56
dk3n=26.0 dk3d=float(112)=112.0
dk3n=26.0 dk3d=float(1119/10)=111.9
dk3n=26.0 dk3d=float(5593/50)=111.86
dk3n=27.0 dk3d=float(117)=117.0
dk3n=27.0 dk3d=float(581/5)=116.2
dk3n=27.0 dk3d=float(2904/25)=116.16
dk3n=28.0 dk3d=float(121)=121.0
dk3n=28.0 dk3d=float(2412)=120.5
dk3n=28.0 dk3d=float(12047/100)=120.47
dk3n=29.0 dk3d=float(125)=125.0
dk3n=29.0 dk3d=float(624/5)=124.8
dk3n=29.0 dk3d=float(12477/100)=124.77
dk3n=30.0 dk3d=float(130)=130.0
dk3n=30.0 dk3d=float(1291/10)=129.1
dk3n=30.0 dk3d=float(12907/100)=129.07
dk3n=31.0 dk3d=float(134)=134.0
dk3n=31.0 dk3d=float(667/5)=133.4
dk3n=31.0 dk3d=float(13337/100)=133.37
dk3n=32.0 dk3d=float(138)=138.0
dk3n=32.0 dk3d=float(1377/10)=137.7
dk3n=32.0 dk3d=float(13767/100)=137.67
dk3n=33.0 dk3d=float(142)=142.0
dk3n=33.0 dk3d=float(142)=142.0
dk3n=33.0 dk3d=float(14197/100)=141.97
dk3n=34.0 dk3d=float(147)=147.0
dk3n=34.0 dk3d=float(1463/10)=146.3
dk3n=34.0 dk3d=float(14627/100)=146.27
dk3n=35.0 dk3d=float(151)=151.0
dk3n=35.0 dk3d=float(753/5)=150.6
dk3n=35.0 dk3d=float(15057/100)=150.57
dk3n=36.0 dk3d=float(155)=155.0
dk3n=36.0 dk3d=float(1549/10)=154.9
dk3n=36.0 dk3d=float(3872/25)=154.88
dk3n=37.0 dk3d=float(160)=160.0
dk3n=37.0 dk3d=float(796/5)=159.2
dk3n=37.0 dk3d=float(7959/50)=159.18
dk3n=38.0 dk3d=float(164)=164.0
dk3n=38.0 dk3d=float(327/2)=163.5
dk3n=38.0 dk3d=float(4087/25)=163.48
dk3n=39.0 dk3d=float(168)=168.0
dk3n=39.0 dk3d=float(839/5)=167.8
dk3n=39.0 dk3d=float(8389/50)=167.78
dk3n=40.0 dk3d=float(173)=173.0
```

---

```

dk3n=40.0 dk3d=float(1721/10)=172.1
dk3n=40.0 dk3d=float(4302/25)=172.08
dk3n=41.0 dk3d=float(177)=177.0
dk3n=41.0 dk3d=float(88/25)=176.4
dk3n=41.0 dk3d=float(8819/50)=176.38
dk3n=42.0 dk3d=float(181)=181.0
dk3n=42.0 dk3d=float(1807/10)=180.7
dk3n=42.0 dk3d=float(4517/25)=180.68
dk3n=43.0 dk3d=float(185)=185.0
dk3n=43.0 dk3d=float(185)=185.0
dk3n=43.0 dk3d=float(18499/100)=184.99
dk3n=44.0 dk3d=float(190)=190.0
dk3n=44.0 dk3d=float(1893/10)=189.3
dk3n=44.0 dk3d=float(18929/100)=189.29
dk3n=45.0 dk3d=float(194)=194.0
dk3n=45.0 dk3d=float(968/5)=193.6
dk3n=45.0 dk3d=float(19359/100)=193.59
dk3n=46.0 dk3d=float(198)=198.0
dk3n=46.0 dk3d=float(1979/10)=197.9
dk3n=46.0 dk3d=float(19789/100)=197.89
dk3n=47.0 dk3d=float(203)=203.0
dk3n=47.0 dk3d=float(1011/5)=202.2
dk3n=47.0 dk3d=float(20219/100)=202.19
dk3n=48.0 dk3d=float(207)=207.0
dk3n=48.0 dk3d=float(413/2)=206.5
dk3n=48.0 dk3d=float(20649/100)=206.49
dk3n=49.0 dk3d=float(211)=211.0
dk3n=49.0 dk3d=float(1054/5)=210.8
dk3n=49.0 dk3d=float(21079/100)=210.79
dk3n=50.0 dk3d=float(216)=216.0
dk3n=50.0 dk3d=float(2151/10)=215.1
dk3n=50.0 dk3d=float(21509/100)=215.09

```

[Program finished]

## 1.6. Trend Variations

$$dE_{k3} = 4 \cdot \sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2 \cdot k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2}))} \quad (4dprocess)$$

(1 bis) 4d superstring;

$$dE[k3] = 2^{(7/4)} * \text{abs}(gM) * \sqrt{(k3+1) / (k3 * \sqrt{2 * k3 + 2})}$$

$$idE_{k3} = 4 \cdot \frac{\sqrt{gM^2} \cdot -i \cdot \frac{-\frac{2^3}{2+2 \cdot k3}^{\frac{1}{2}}}{-\frac{2^3}{2+2 \cdot k3} + 2^2}}{\sqrt{gM^2}} = 2^{\frac{7}{4}} \cdot \sqrt{\frac{(k3+1)}{k3 \cdot \sqrt{(2 \cdot k3 + 2)}}}$$

$$idE[k3] = 2^{(7/4)} * \sqrt{(k3+1) / (k3 * \sqrt{2 * k3 + 2})}$$

or

$$dE2[k3] = (2^{(7/2)} * gM^2 * k3 + 2^{(7/2)} * gM^2) / (k3 * \sqrt{2 * k3 + 2}),$$

$$idE2[k3] = (2^{(7/2)} * k3 + 2^{(7/2)}) / (k3 * \sqrt{2 * k3 + 2});$$

$$Example 1 : dE = 4 \cdot \sqrt{\frac{gM^2}{2}} \sim 125.5673374143954990316092809188 GeV \quad (gM^2 = 1393.6328858707575005182839547884 GeV^2)$$

### 1.6.1. Algorithm

```
from math import*
#An algorithm giving sets of massive bosons-dark energy: {dE[k3] = 2^(7/4)*gM*sqrt((k3n+1)/ (k3n*sqrt(2*k3n+2))), k3n = 1+n. dk3n}
#and sets of massive bosons-dark matter: {dE[k3] = 2^(7/4)*gM*sqrt((k3d+1)/(k3d*sqrt(2*k3d+2 ))), k3d = 1+n.dk3d}

for dk in range (1,100 + 1):
    Sidn = 0
    Sidd = 0
    tmax = 10000
    dk3n = dk
    dk3d = dk+1
    d0 = 1
    for t0 in range(1,10000 + 1):
        if d0 > 10**(-3) :
            Sidn = 0
            Sidd = 0
            k3n = 1
            k3d = 1

            for t in range(1, tmax + 1) :
                fiEk3n = 2**((7/4)*sqrt((k3n+1)/(k3n*sqrt(2*k3n+2))))
                fiEk3d = 2**((7/4)*sqrt((k3d+1)/(k3d*sqrt(2*k3d+2 ))))
                Sidn = fiEk3n*dk3n + Sidn
                Sidd = fiEk3d*dk3d + Sidd
                k3n = k3n+dk3n
                k3d = k3d+dk3d

            if t == tmax :
                if (Sidd/Sidn >= 3 and Sidd/Sidn < 4) :
                    k3n = k3n-dk3n
                    k3d = k3d-dk3d
                    print("dk3n = ",dk3n, "dk3d = ",dk3d)
                    dk3d = dk3d-d0
                    d0 = d0/10
                elif Sidd/Sidn < 3 :
                    k3n = k3n-dk3n
                    k3d = k3d-dk3d
                    dk3d = dk3d+d0
                elif Sidd/Sidn >= 4 :
                    k3n = k3n-dk3n
                    k3d = k3d-dk3d
                    dk3d : dk3d-d0/10
                → ... ....
Simple Variations to induce from bosons energy-bosons of approximately 10^(-47) kg (5.60958860892704*10^(-21) GeV).
```

$$\int dE_{k3} dk3 = \int 4.\sqrt{(gM^2 \cdot -i \cdot \frac{(-\frac{2^3}{(2+2.k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2})} dk3$$
$$(5) = 2^{\frac{11}{4}} \cdot gM \cdot \int \sqrt{\left(\frac{1}{\sqrt{(2.k3 + 2) \cdot (4 - 8/(2.k3 + 2))}}\right)} dk3$$

We obtain

$$k3min > 1.255314934818507.10^{89}$$

$$SdEmax = 5.60958860892704*10^{(-21)} \text{ GeV}$$

( $k3 = 1.255314934818507.10^{89}$  (From massive bosons-4d string energy generator)) [16]

# Resonant Combination

$dk$  is the number of identical massive bosons

$tx$  is the number of bosons groups

$k3i \geq k3min$  (to obtain some less massive bosons but traveling larger distances)

Example of result :  $k3i=10^{110}, dk=18, tx=251 \Leftrightarrow k3i=10^{105}, dk=1, tx=254$

## 1.6.2. Fusion of 4 Identical Particles that are to Disappear Spontaneously or After One Wave Length

A single 4d-String appearing and disappearing spontaneously ( $Dt \leq 0$ ) [10-12,14,15]

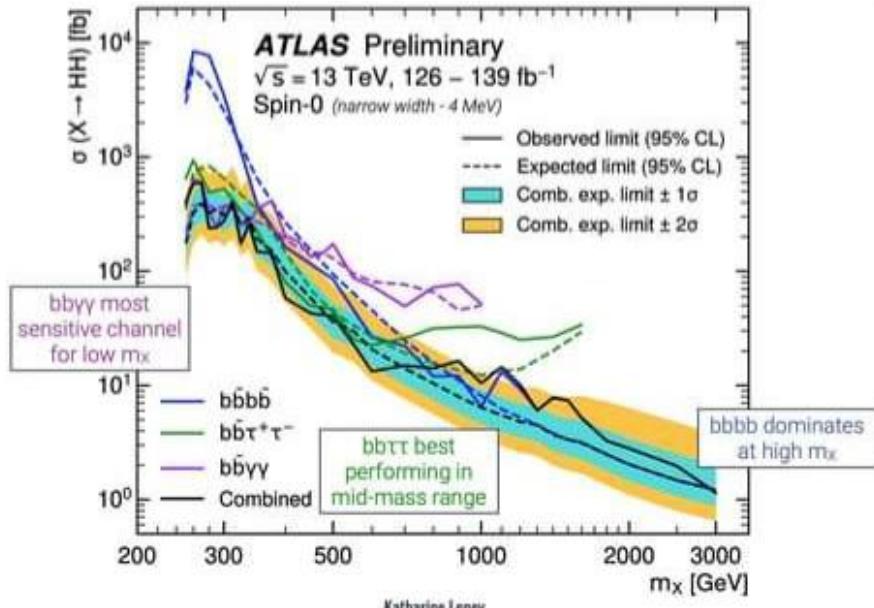


Figure 13: Observation of More than Spin 0 Events for Spin 2 Events

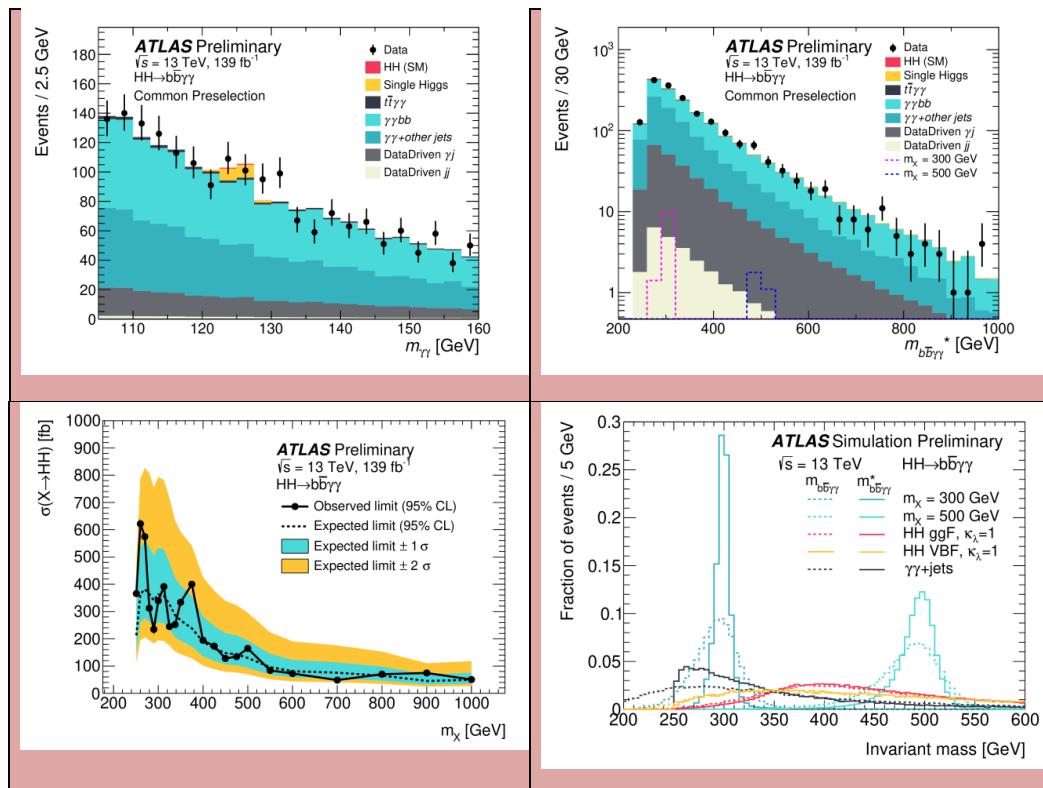


Figure 14: Decay Channel to Produce Spin 2 Events

As well as  $\{\pi^+, \pi^-\} \rightarrow \{\{\mu^+, \mu^-\}, v_\mu, \text{anti\_}v_\mu\}$ ;

The  $\pi^\pm$  mesons have a mass of 139.6 MeV/c<sup>2</sup> and a mean lifetime of  $2.6033 \times 10^{-8}$  s. They decay due to the weak interaction. The primary decay mode of a pion, with a branching of  $99.98770 \pm 0.00004$  %, is a leptonic decay into a muon and a muon neutrino:

$$\pi^+ \rightarrow \mu^+ + v_\mu$$

$$\pi^- \rightarrow \mu^- + \text{anti\_}v_\mu$$

The second most common decay mode of a pion, with a branching of 0.0123 %, is also a leptonic decay into an electron and the corresponding electron antineutrino. This "electronic mode" was discovered at CERN in 1958:

$$\pi^+ \rightarrow e^+ + v_e$$

$$\pi^- \rightarrow e^- + \text{anti\_}v_e$$

We have a  $\{\text{particle\_spin } +2, \text{particle\_spin-2}\} \rightarrow 2.\{\text{b,anti\_b}\}$

or

$\{\text{particle\_spin } +2, \text{particle\_spin-2}\} \rightarrow \{\{\text{b,anti\_b}\} + \{\tau, \text{anti\_}\tau\}\}$

### 1.7. Instead of Photons Generated

The  $\pi^0$  has a slightly smaller mass than the charged pions ( $134.9766 \pm 0.0006$  MeV / c<sup>2</sup>) and a much shorter lifetime of  $8.4 \pm 0.6 \times 10^{-17}$  s. At the end of this period, the  $\pi^0$  decays due to the electromagnetic interaction. The most common decay (98.798% of decays) gives two  $\gamma$  photons:

$$\pi^0 \rightarrow 2.\gamma$$

Or

In  $1.198 \pm 0.032$ % of cases, the decay products are a  $\gamma$  photon and an electron-positron pair:

$$\pi^0 \rightarrow \gamma + e^- + e^+$$

As

$2.\text{particle\_spin } 0 \rightarrow \{\text{b,anti\_b}, 2.\gamma\}$ .

#### 1.7.1. From 4d Superstring a Particle at Some 125 GeV

$$dE_{k3} = 4.\sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2.k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2}))} \quad (4dprocess)$$

4d superstring,

$$idE_{k3} = 4 \cdot \frac{\sqrt{gM^2} \cdot -i \cdot \frac{-\frac{2^3}{(2+2.k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2}}{\sqrt{gM^2}} = 2^{\frac{7}{4}} \cdot \sqrt{\frac{(k3+1)}{k3 \cdot \sqrt{(2.k3+2)}}}$$

or

$$dE_{2k3} = 16.gM^2 \cdot -i \cdot \frac{-\frac{2^3}{(2+2.k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2},$$

$$idE_{2k3} = 16 \cdot \frac{gM^2 \cdot -i \cdot \frac{-\frac{2^3}{(2+2.k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2}}{gM^2} = \frac{2^{\frac{7}{2}} \cdot k3 + 2^{\frac{7}{2}}}{k3 \cdot \sqrt{2.k3+2}};$$

Example 1 :  $dE = 4\sqrt{\frac{gM^2}{\sqrt{2}}} \sim 125.5673374143954990316092809188 \text{ GeV}$  ( $gM^2 = 1393.6328858707575005182839547884 \text{ GeV}^2$ )

[12-14]

The particle at exactly some 125 GeV

And spin

$1+1+1-1 = 2$  (As a frequent Space-Time reflect.)

or

$1-1+1-1 = 0$

With

$dE = \sqrt{dE^2}$  sets:

$$dE_{k3} = 4\sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2 \cdot k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2}))} \quad (4dprocess)$$

$$idE_{k3} = 4 \cdot \frac{\sqrt{gM^2} \cdot -i \cdot \frac{-\frac{2^3}{(2+2 \cdot k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2}}{\sqrt{gM^2}} = 2^{\frac{7}{4}} \cdot \sqrt{\frac{(k3+1)}{k3 \cdot \sqrt{(2 \cdot k3+2)}}}$$

or

$$dE_{2k3} = 16 \cdot gM^2 \cdot -i \cdot \frac{-\frac{2^3}{(2+2 \cdot k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2},$$

$$idE_{2k3} = 16 \cdot \frac{gM^2 \cdot -i \cdot \frac{-\frac{2^3}{(2+2 \cdot k3)}^{\frac{1}{2}}}{-\frac{2^3}{(2+2 \cdot k3)} + 2^2}}{gM^2} = \frac{2^{\frac{7}{2}} \cdot k3 + 2^{\frac{7}{2}}}{k3 \cdot \sqrt{2 \cdot k3 + 2}},$$

Example 1 :  $dE = 4\sqrt{\frac{gM^2}{\sqrt{2}}} \sim 125.5673374143954990316092809188 \text{ GeV}$  ( $gM^2 = 1393.6328858707575005182839547884 \text{ GeV}^2$ )

Examples: [11-14, 17-19]

$dE = 4 * \sqrt{((gM^2)^2 * |Val[1,2]|)}$ ,  $Val[1,2] = X/(X^2+Y^2)$  with  $k3=1$  and  $Y=2$  and  $[X=-\sqrt{2} * \%i, X=\sqrt{2} * \%i]$ ,  
 $Val[2,2] = X/(X^2+Y^2)$  with  $k3=2$  and  $Y=2$  and  $[X=-(2 * \%i)/\sqrt{3}, X=(2 * \%i)/\sqrt{3}] \rightarrow Val[2,2] = (\sqrt{3} * \%i)/4$   
 $\rightarrow dE = 98.26175177406498 \text{ GeV}$ ,

$Val[3,2] = X/(X^2+Y^2)$  with  $k3=3$  and  $Y=2$  and  $[X=-\%i, X=%oi] \rightarrow Val[3,2] = \%oi/3$   
 $\rightarrow dE = 86.21315865135692 \text{ GeV}$ ,

.....  
 $Val[4,2] = X/(X^2+Y^2)$  with  $k3=4$  and  $Y=2$  and  $[X=-(2 * \%i)/\sqrt{5}, X=(2 * \%i)/\sqrt{5}] \rightarrow Val[4,2] = (\sqrt{5} * \%i)/8$   
 $\rightarrow dE = 78.94628387056885 \text{ GeV}$ ,

$Val[5,2] = X/(X^2+Y^2)$  with  $k3=5$  and  $Y=2$  and  $[X=-(\sqrt{2} * \%i)/\sqrt{3}, X=(\sqrt{2} * \%i)/\sqrt{3}] \rightarrow Val[5,2] = (\sqrt{3} * \%i)/(5 * \sqrt{2})$   
 $\rightarrow dE = 73.90468953072723 \text{ GeV}$ ,

$Val[6,2] = X/(X^2+Y^2)$  with  $k3=6$  and  $Y=2$  and  $[X=-(2 * \%i)/\sqrt{7}, X=(2 * \%i)/\sqrt{7}] \rightarrow Val[6,2] = (\sqrt{7} * \%i)/12$   
 $\rightarrow dE = 70.11615158611494 \text{ GeV}$ ,

$Val[7,2] = X/(X^2+Y^2)$  with  $k3=7$  and  $Y=2$  and  $[X=-\%i/\sqrt{2}, X=%i/\sqrt{2}] \rightarrow Val[7,2] = (\sqrt{2} * \%i)/7$   
 $\rightarrow dE = 67.11856508201555,$

$Val[8,2] = X/(X^2+Y^2)$  with  $k3=8$  and  $Y=2$  and  $[X=-(2 * \%i)/3, X=(2 * \%i)/3] \rightarrow Val[8,2] = (3 * \%i)/16$   
 $\rightarrow dE = 64.6598689885177,$

$Val[9,2] = X/(X^2+Y^2)$  with  $k3=9$  and  $Y=2$  and  $[X=-(\sqrt{2} * \%i)/\sqrt{5}, X=(\sqrt{2} * \%i)/\sqrt{5}] \rightarrow Val[9,2] = (\sqrt{5} * \%i)/(9 * \sqrt{2})$   
 $\rightarrow dE = 62.58898832127002,$

$Val[10,2] = X/(X^2+Y^2)$  with  $k3=10$  and  $Y=2$  and  $[X=-(2 * \%i)/\sqrt{11}, X=(2 * \%i)/\sqrt{11}] \rightarrow Val[10,2] = (\sqrt{11} * \%i)/20$   
 $\rightarrow dE = 60.8089294622656,$

.....

Val[11,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 11 and Y = 2 and [X=-%i/sqrt(3),X=%i/sqrt(3)] → Val[11,2] = (sqrt(3)\*%i)/11  
→ dE = 59.25406579592956,

Val[12,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 12 and Y = 2 and [X=-(2\*%i)/sqrt(13),X=(2\*%i)/sqrt(13)] → Val[12,2] = (sqrt(13)\*%i)/24  
→ dE = 57.87811808262757,

Val[13,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 13 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(7),X=(sqrt(2)\*%i)/sqrt(7)] → Val[13,2] = (sqrt(7)\*%i)/(13\*sqrt(2))  
→ dE = 56.64733971277926,

Val[14,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 14 and Y = 2 and [X=-(2\*%i)/sqrt(15),X=(2\*%i)/sqrt(15)] → Val[14,2] = (sqrt(15)\*%i)/28  
→ dE = 55.53643312639486,

Val[15,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 15 and Y = 2 and [X=-%i/2,X=%i/2] → Val[15,2] = (2\*%i)/15  
→ dE = 54.52598912314765,

Val[16,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 16 and Y = 2 and [X=-(2\*%i)/sqrt(17),X=(2\*%i)/sqrt(17)] → Val[16,2] = (sqrt(17)\*%i)/32  
→ dE = 53.60081898525197,

Val[17,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 17 and Y = 2 and [X=-(sqrt(2)\*%i)/3,X=(sqrt(2)\*%i)/3] → Val[17,2] = (3\*%i)/(17\*sqrt(2))  
→ dE = 52.74883253574095,

.....

Val[18,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 18 and Y = 2 and [X=-(2\*%i)/sqrt(19),X=(2\*%i)/sqrt(19)] → Val[18,2] = (sqrt(19)\*%i)/36  
→ dE = 51.9602622262889,

Val[19,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 19 and Y = 2 and [X=-%i/sqrt(5),X=%i/sqrt(5)] → Val[19,2] = (sqrt(5)\*%i)/19  
→ dE = 51.2271134499051,

Val[20,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 20 and Y = 2 and [X=-(2\*%i)/sqrt(21),X=(2\*%i)/sqrt(21)] → Val[20,2] = (sqrt(21)\*%i)/40  
→ dE = 50.54276680389589 GeV,

Val[21,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 21 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(11),X=(sqrt(2)\*%i)/sqrt(11)] → Val[21,2] = (sqrt(11)\*%i)/(21\*sqrt(2))  
→ dE = 49.90168487010055 GeV,

Val[22,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 22 and Y = 2 and [X=-(2\*%i)/sqrt(23),X=(2\*%i)/sqrt(23)] → Val[22,2] = (sqrt(23)\*%i)/44  
→ dE = dE = 49.29919241818454 GeV,

Val[23,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 23 and Y = 2 and [X=-%i/sqrt(6),X=%i/sqrt(6)] → Val[23,2] = (sqrt(6)\*%i)/23  
→ dE = 48.73130916893959 GeV,

Val[24,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 24 and Y = 2 and [X=-(2\*%i)/5,X=(2\*%i)/5] → Val[24,2] = (5\*%i)/48  
→ dE = 48.19462082485205 GeV,

.....

Val[25,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 25 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(13),X=(sqrt(2)\*%i)/sqrt(13)] → Val[25,2] = (sqrt(13)\*%i)/(25\*sqrt(2))  
→ dE = 47.68617839110907 GeV,

Val[26,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 26 and Y = 2 and [X=-(2\*%i)/3^(3/2),X=(2\*%i)/3^(3/2)] → Val[26,2] = (3^(3/2)\*%i)/52  
→ dE = 47.20341870370431 GeV,

Val[27,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 27 and Y = 2 and [X=-%i/sqrt(7),X=%i/sqrt(7)] → Val[27,2] = (sqrt(7)\*%i)/27  
→ dE = 46.74410105740996 GeV,

Val[28,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 28 and Y = 2 and [X=-(2\*%i)/sqrt(29),X=(2\*%i)/sqrt(29)] → Val[28,2] = (sqrt(29)\*%i)/56  
→ dE = 46.30625619890902 GeV,

Val[29,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 29 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(15),X=(sqrt(2)\*%i)/sqrt(15)] → Val[29,2] = (sqrt(15)\*%i)/(29\*sqrt(2))  
→ dE = 45.88814491850693 GeV,

Val[30,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 30 and Y = 2 and [X=-(2\*%i)/sqrt(31),X=(2\*%i)/sqrt(31)] → Val[30,2] = (sqrt(31)\*%i)/60  
→ dE = 45.4882241664636 GeV,

Val[31,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 31 and Y = 2 and [X=-%i/2^(3/2),X=%i/2^(3/2)] → Val[31,2] = (2^(3/2)\*%i)/31  
→ dE = 45.10511912202092 GeV,

.....

Val[32,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 32 and Y = 2 and [X=-(2\*%i)/sqrt(33),X=(2\*%i)/sqrt(33)] → Val[32,2] = (sqrt(33)\*%i)/64  
→ dE = 44.73760001151199 GeV,

Val[33,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 33 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(17),X=(sqrt(2)\*%i)/sqrt(17)] → Val[33,2] = (sqrt(17)\*%i)/(33\*sqrt(2))  
→ dE = 44.38456274518938 GeV,

Val[34,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 34 and Y = 2 and [X=-(2\*%i)/sqrt(35),X=(2\*%i)/sqrt(35)] → Val[34,2] = (sqrt(5)\*sqrt(7)\*%i)/68  
→ dE = 44.04501264725804 GeV,

---

Val[35,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 35 and Y = 2 and [X=-%oi/3,X=%i/3] → Val[35,2] = (3\*%i)/35  
 → dE = 43.71805070866736 GeV,  
 Val[36,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 36 and Y = 2 and [X=-(2\*%i)/sqrt(37),X=(2\*%i)/sqrt(37)] → Val[36,2] = (sqrt(37)\*%i)/72  
 → dE = 43.40286191067236 GeV,  
 Val[37,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 37 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(19),X=(sqrt(2)\*%i)/sqrt(19)] → Val[37,2] = (sqrt(19)\*%i)/(37\*sqrt(2))  
 → dE = 43.09870525843511 GeV,  
 Val[38,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 38 and Y = 2 and [X=-(2\*%i)/sqrt(39),X=(2\*%i)/sqrt(39)] → Val[38,2] = (sqrt(39)\*%i)/76  
 → dE = 42.80490523481002 GeV,  
 ....  
 Val[39,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 39 and Y = 2 and [X=-%i/sqrt(10),X=%i/sqrt(10)] → Val[39,2] = (sqrt(10)\*%i)/39  
 → dE = 42.52084443991102 GeV,  
 Val[40,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 40 and Y = 2 and [X=-(2\*%i)/sqrt(41),X=(2\*%i)/sqrt(41)] → Val[40,2] = (sqrt(41)\*%i)/80  
 → dE = 42.2459572257572 GeV,  
 Val[41,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 41 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(21),X=(sqrt(2)\*%i)/sqrt(21)] → Val[41,2] = (sqrt(21)\*%i)/(41\*sqrt(2))  
 → dE = 41.9797241699585 GeV,  
 Val[42,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 42 and Y = 2 and [X=-(2\*%i)/sqrt(43),X=(2\*%i)/sqrt(43)] → Val[42,2] = (sqrt(43)\*%i)/84  
 → dE = 41.72166726007706 GeV,  
 Val[43,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 43 and Y = 2 and [X=-%i/sqrt(11),X=%i/sqrt(11)] → Val[43,2] = (sqrt(11)\*%i)/43  
 → dE = 41.47134568252444 GeV,  
 Val[44,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 44 and Y = 2 and [X=-(2\*%i)/(3\*sqrt(5)),X=(2\*%i)/(3\*sqrt(5))] → Val[44,2] = (3\*sqrt(5)\*%i)/88  
 → dE = 41.22835212780523 GeV,  
 Val[45,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 45 and Y = 2 and [X=-(sqrt(2)\*%i)/sqrt(23),X=(sqrt(2)\*%i)/sqrt(23)] → Val[45,2] = (sqrt(23)\*%i)/(45\*sqrt(2))  
 → dE = 40.99230953849354 GeV,  
 ....  
 Val[46,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 46 and Y = 2 and [X=-(2\*%i)/sqrt(47),X=(2\*%i)/sqrt(47)] → Val[46,2] = (sqrt(47)\*%i)/92  
 → dE = 40.76286823822587 GeV,  
 Val[47,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 47 and Y = 2 and [X=-%i/(2\*sqrt(3)),X=%i/(2\*sqrt(3))] → Val[47,2] = (2\*sqrt(3)\*%i)/47  
 → dE = 40.53970338975132 GeV,  
 Val[48,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 48 and Y = 2 and [X=-(2\*%i)/7,X=(2\*%i)/7] → Val[48,2] = (7\*%i)/96  
 → dE = 40.32251273812042 GeV,  
 Val[49,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 49 and Y = 2 and [X=-(sqrt(2)\*%i)/5,X=(sqrt(2)\*%i)/5] → Val[49,2] = (5\*%i)/(49\*sqrt(2))  
 → dE = 40.11101460174871 GeV,  
 Val[50,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 50 and Y = 2 and [X=-(2\*%i)/sqrt(51),X=(2\*%i)/sqrt(51)] → Val[50,2] = (sqrt(51)\*%i)/100  
 → dE = 39.90494607962204 GeV,  
 Val[51,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 51 and Y = 2 and [X=-%i/sqrt(13),X=%i/sqrt(13)] → Val[51,2] = (sqrt(13)\*%i)/51  
 → dE = 39.70406144752673 GeV,  
 Val[52,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 52 and Y = 2 and [X=-(2\*%i)/sqrt(53),X=(2\*%i)/sqrt(53)] → Val[52,2] = (sqrt(53)\*%i)/104  
 → dE = 39.5081307200551 GeV,  
 ....

Obtaining of bosons, each having a mass of approximately  $10^{-47}$  kg with k3 = 1.2553149348185 07.10<sup>89</sup> (From massive bosons-4d string energy generator) [16,18].

$$dE_{k3} = 4.\sqrt{(gM^2 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2.k3)})^{\frac{1}{2}}}{-\frac{2^3}{(2+2.k3)} + 2^2}))} \text{ (4d process);}$$

$$dE_{k3} = 4.\sqrt{(1393.6328858707575005182839547884 \cdot (-i \cdot \frac{(-\frac{2^3}{(2+2.k3)})^{\frac{1}{2}}}{-\frac{2^3}{2+2.k3} + 2^2}))}$$

→ import cmath  
 for k3 in range(1, 6):  
 $dE = 4 * \text{cmath.sqrt}(1393.6328858707575005182839547884 * (-1j * (-2 ** 3 / (2 + 2 * k3)) ** (1/2) / (-2 ** 3 / (2 + 2 * k3) + 2 ** 2)))$

---

```

print("dE =",dE," GeV")
dE=125.5673374143955 GeV (Exactly a Higgs boson mass)
dE=98.26175177406499 GeV
dE=86.21315865135692 GeV
dE=78.94628387056885 GeV
dE=73.90468953072724 GeV;

from math import *
for k3 in range(1,6):
    dEk3 = (2**((11/4)*(1393.6328858707575005182839547884)**(1/2)))/(abs(2*k3+2)**(1/4)*(a bs(8/(2*k3+2)- 4))**(1/2))
    print('dE[', k3, '] =', dEk3)
→ ...
Or

[dE[k3] = 4*sqrt(gM^2*(-%i*(-2^3/(2+2*k3))^(1/2)/(-2^3/(2+2*k3)+2^2))),[k3]; [(4*k3*sqrt(2*k3+2)*dE[k3]^2)^2
= ((2^(11/2)*gM^2)+2^(11/2)*gM^2*k3)^2],[k3];

[k3 = -1,
k3 = -(8*gM^2*sqrt(dE[k3]^4+16*gM^4)-32*gM^4)/dE[k3]^4,
k3 = (8*gM^2*sqrt(dE[k3]^4+16*gM^4)+32*gM^4)/dE[k3]^4]

--dE[k3] = 5.60958860892704*10^(-21) GeV → {k3 = - (8*(1393.6328858707575005182839547884)*sqrt((5.60958860892704*
10^(-21))^4+16*(1393.6328858707575005182839547884)^2)-
32*(1393.6328858707575005182839547884)^2)/(5.60958860892704*10^(-21))^4,
k3 = (8*(1393.6328858707575005182839547884)*sqrt((5.60958860892704*10^(-21))^4+16*(1393.63288587075750051828395
47884)^2)+32*(1393.6328858707575005182839547884)^2)/(5.60958860892704*10^(-21))^4};

{k3 = 0.0
k3 = 1.255314934818507*10^89}.

```

## 1.8. Introduction of Interactions with a 4d-String

### 1.8.1. Absorption of Massive Gravitons with an Open String

On N massive gravitons n will be instantly absorbed and  $(N!/(N-n)!n!)$  total absorptions (where massive gravitons are repeated) in  $(N!/(N-n)!n!)/n$  distinct time intervals will be necessary for the absorption of N massive gravitons.

We obtain two different possible energy values for n massive gravitons in N.

In  $q.(N!/(N-n)!n!).dt_0$  times with  $q \rightarrow \infty$  we have  $E = (1/2).q.(sE_a + sE_b)$ . (6)

But would explain heterogeneities with dark matter [20-23].

We obtain from result : An open string absorbing a massive graviton

$$H = \int d\sigma [X^2(\sigma)/2 + (\partial X / \partial \sigma)^2/2] = m^2 = E_A \cdot E_B / C^4 + \text{Potential Energy}^2 / C^4 \quad (7)$$

For values  $(k_{max}, |k_{min}|) \leq 100000$ , rich values of k3 and dEk3 are not obtained, but for values  $(k_{max}, |k_{min}|) \geq 100000$ , we look for real values  $|dEk3| \leq 4 \text{ GeV}$ .

With  $dE^2[k3] = \{2^{(7/2)} * gM^2 * k3 / (k3 * sqrt(2 * k3 + 2)) \rightarrow \text{Potential energy}$

$+ 2^{(7/2)} * gM^2 / (k3 * sqrt(2 * k3 + 2)) \rightarrow E_A \cdot E_B \text{ Kinematic energies}\}$  (8)

We calculate  $E_{\text{Potential energy}} = gM \cdot \sqrt{(2^{(7/2)} * k3 / (k3 * sqrt(2 * k3 + 2)))}$

And obtain  $E_{\text{Kinematic energy}} \neq E_A \text{ or } E_B$ ;  $E_{\text{Kinematic energy}} = dEk3 - E_{\text{Potential energy}}$

Interactions of two 4d string one of spin +2 and one of spin -2 with an open string. 4d string : Trefoil Knot [15].

With  $dE^2[k3] =$

$\{2^{(7/2)} * gM^2 * k3 / (k3 * sqrt(2 * k3 + 2)) \rightarrow \text{Potential energy}$

$+ 2^{(7/2)} * gM^2 / (k3 * sqrt(2 * k3 + 2)) \rightarrow E_A \cdot E_B \text{ Kinematic energies}\}$

We calculate  $E_{\text{Potential energy}} = gM \cdot \sqrt{(2^{(7/2)} * k3 / (k3 * sqrt(2 * k3 + 2)))}$  (8)

And obtain  $E_{\text{Kinematic energy}} \neq E_A \text{ or } E_B$ ;  $E_{\text{Kinematic energy}} = dEk3 - E_{\text{Potential energy}}$

$k3a \rightarrow 4\text{d massive graviton mass calculation.}$

---

k3b → a second 4d massive graviton mass calculation.

We obtain

$$\xi = (E_A \cdot E_B / C^4 + PEnergy^2 / C^4) / (E_A + PEnergy) \quad (9)$$

then

$$\xi = (PEnergy^2 + E_A \cdot E_B) / (C^4 \cdot PEnergy + C^4 \cdot E_A) \quad (10)$$

or

$$\xi = (E_A \cdot E_B / C^4 + PEnergy^2 / C^4) / (E_B + PEnergy) \quad (11)$$

then

$$\xi = (PEnergy^2 + E_A \cdot E_B) / (C^4 \cdot PEnergy + C^4 \cdot E_B) \quad (12)$$

with  $dE[k3] = 2^{(7/4)} * abs(gM) * sqrt((k3+1)/(k3 * sqrt(2*k3+2)))$

and

$$E_A \cdot E_B = dE_A[k3] \cdot dE_B[k3]$$

### 1.8.2. Algorithm in Python :

#### 1.8.2.1. Example 1:

```
#n = 5, N = 8
import random
import math

N = 8
kmax = 100
kmin = 1
t = 0
k3 = [0]*(N+1)
dE = [0]*(N+1)

while t <= N:
    k_3 = -random.randint(0, kmax) + 2 * kmax

    if k_3 > 0:
        t += 1
        k3[t-1] = k_3
        dE[t-1] = (1127186345 * math.sqrt((k_3 + 1)/(k_3 * math.sqrt(2*k_3+2))))/8976748
        print(k3[t-1],dE[t-1])

    l = 0
    sEa = 0
    for i1 in range(N):
        for i2 in range(i1 + 1, N):
            for i3 in range(i2 + 1, N):
                for i4 in range(i3 + 1, N):
                    for i5 in range(i4 + 1, N):
                        l += 1
                        print(l, ">")
                        print("k3[",i1,"] = ",k3[i1], ", dE[",i1,"] = ",dE[i1])
                        print("k3[",i2,"] = ",k3[i2], ", dE[",i2,"] = ",dE[i2])
                        print("k3[",i3,"] = ",k3[i3], ", dE[",i3,"] = ",dE[i3])
                        print("k3[",i4,"] = ",k3[i4], ", dE[",i4,"] = ",dE[i4])
                        print("k3[",i5,"] = ",k3[i5], ", dE[",i5,"] = ",dE[i5])
                        sEa += dE[i1] + dE[i2] + dE[i3] + dE[i4] + dE[i5]

    sEb = 0
    for i1 in range(N):
        for i2 in range(i1 + 1, N):
            for i3 in range(i2 + 1, N):
                sEb += dE[i1] + dE[i2] + dE[i3]
    print("sEa = ",sEa)
```

---

```

print("when")
print("sEb = ",sEb)

1.8.2.2. Example 2:
#n = 5, N = 8*4
import math
import random
import itertools

N = 8*4
kmax = 1000
kmin = 1
t = 0
k3 = [0]*(N+1)
dE = [0]*(N+1)
while t < N:
    k_3 = -random.randint(0, kmax) + 2*kmax
    if k_3 > 0:
        t += 1
        k3[t] = k_3
        dE[t] = (1127186345*math.sqrt((k_3+1)/(k_3*math.sqrt(2*k_3+2))))/8976748
        print("k3[", t, "] = ", k3[t], ", dE[", t, "] = ", dE[t], sep="")
    l = 0
    sEa = 0
    for indices in itertools.combinations(range(1, N+1), 5):
        l += 1
        print(l, ":")
        for i in indices:
            print("k3[", i, "] = ", k3[i], ", dE[", i, "] = ", dE[i], sep="")
            sEa += sum(dE[i] for i in indices)

    sEb = 0
    for indices in itertools.combinations(range(1, N+1), 27):
        sEb += sum(dE[i] for i in indices)
    print("Result for sEa:", sEa)
    print("when")
    print("Result for sEb:", sEb)

```

## **1.9. Algorithm in C++**

### **1.9.1. Example 1:**

```

//n = 5, N = 8
#include <iostream>
#include <cmath>
#include <cstdlib>
#include <ctime>
using namespace std;

int main() {
    srand(time(0));
    int N = 8;
    int kmax = 100;
    int kmin = 1;
    int t = 0;
    int k3[N+1];
    double dE[N+1];

    while (t <= N) {

```

```

int k_3 = -rand() % kmax + 2 * kmax;
if (k_3 > 0) {
    t++;
    k3[t] = k_3;
    dE[t] = (1127186345 * sqrt((k_3 + 1) / (k_3 * sqrt(2 * k_3 + 2)))) / 8976748;
    cout << "k3[" << t << "] = " << k3[t] << ", dE[" << t << "] = " << dE[t] << endl;
}
}

int l = 0;
double sEa = 0;

for (int i1 = 1; i1 <= N; i1++) {
    for (int i2 = 1; i2 <= N; i2++) {
        for (int i3 = 1; i3 <= N; i3++) {
            for (int i4 = 1; i4 <= N; i4++) {
                for (int i5 = 1; i5 <= N; i5++) {
                    if (i1 < i2 && i2 < i3 && i3 < i4 && i4 < i5) {
                        l++;
                        cout << l << ": " << endl;
                        cout << "k3[" << i1 << "] = " << k3[i1] << ", dE[" << i1 << "] = " << dE[i1] << endl;
                        cout << "k3[" << i2 << "] = " << k3[i2] << ", dE[" << i2 << "] = " << dE[i2] << endl;
                        cout << "k3[" << i3 << "] = " << k3[i3] << ", dE[" << i3 << "] = " << dE[i3] << endl;
                        cout << "k3[" << i4 << "] = " << k3[i4] << ", dE[" << i4 << "] = " << dE[i4] << endl;
                        cout << "k3[" << i5 << "] = " << k3[i5] << ", dE[" << i5 << "] = " << dE[i5] << endl;
                        sEa += dE[i1] + dE[i2] + dE[i3] + dE[i4] + dE[i5];
                    }
                }
            }
        }
    }
}

double sEb = 0;
for (int i1 = 1; i1 <= N; i1++) {
    for (int i2 = 1; i2 <= N; i2++) {
        for (int i3 = 1; i3 <= N; i3++) {
            if (i1 < i2 && i2 < i3) {
                sEb += dE[i1] + dE[i2] + dE[i3];
            }
        }
    }
}

cout << "Result for sEa: " << sEa << endl;
cout << "when" << endl;
cout << "Result for sEb: " << sEb << endl;

return 0;
}
→ k3[1] = 180, dE[1] = 28.8671
k3[2] = 129, dE[2] = 31.3914
k3[3] = 149, dE[3] = 30.2725
k3[4] = 152, dE[4] = 30.1211
k3[5] = 162, dE[5] = 29.6421
k3[6] = 190, dE[6] = 28.4774
k3[7] = 198, dE[7] = 28.1838
k3[8] = 170, dE[8] = 29.2849

```

---

k3[9] = 163, dE[9] = 29.5962

1:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

2:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[6] = 190, dE[6] = 28.4774

3:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[7] = 198, dE[7] = 28.1838

4:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

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k3[8] = 170, dE[8] = 29.2849

5:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

6:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[7] = 198, dE[7] = 28.1838

7:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[8] = 170, dE[8] = 29.2849

8:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[6] = 190, dE[6] = 28.4774

k3[7] = 198, dE[7] = 28.1838

9:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[6] = 190, dE[6] = 28.4774

k3[8] = 170, dE[8] = 29.2849

10:

k3[1] = 180, dE[1] = 28.8671

---

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[7] = 198, dE[7] = 28.1838

k3[8] = 170, dE[8] = 29.2849

11:

k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

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k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

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k3[2] = 129, dE[2] = 31.3914

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k3[7] = 198, dE[7] = 28.1838

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k3[2] = 129, dE[2] = 31.3914

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k3[5] = 162, dE[5] = 29.6421

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k3[8] = 170, dE[8] = 29.2849

16:

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k3[2] = 129, dE[2] = 31.3914

k3[4] = 152, dE[4] = 30.1211

k3[7] = 198, dE[7] = 28.1838

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k3[7] = 198, dE[7] = 28.1838

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k3[1] = 180, dE[1] = 28.8671

k3[2] = 129, dE[2] = 31.3914

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

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k3[1] = 180, dE[1] = 28.8671

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k3[2] = 129, dE[2] = 31.3914  
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28:  
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k3[3] = 149, dE[3] = 30.2725  
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k3[6] = 190, dE[6] = 28.4774

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31:

k3[1] = 180, dE[1] = 28.8671

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

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k3[7] = 198, dE[7] = 28.1838

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k3[1] = 180, dE[1] = 28.8671

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

k3[7] = 198, dE[7] = 28.1838

k3[8] = 170, dE[8] = 29.2849

36:

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

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k3[2] = 129, dE[2] = 31.3914

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k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

k3[7] = 198, dE[7] = 28.1838

38:

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

k3[8] = 170, dE[8] = 29.2849

39:

k3[2] = 129, dE[2] = 31.3914

---

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[6] = 190, dE[6] = 28.4774

k3[7] = 198, dE[7] = 28.1838

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k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[6] = 190, dE[6] = 28.4774

k3[8] = 170, dE[8] = 29.2849

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k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[4] = 152, dE[4] = 30.1211

k3[7] = 198, dE[7] = 28.1838

k3[8] = 170, dE[8] = 29.2849

42:

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

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43:

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[6] = 190, dE[6] = 28.4774

k3[8] = 170, dE[8] = 29.2849

44:

k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[5] = 162, dE[5] = 29.6421

k3[7] = 198, dE[7] = 28.1838

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k3[2] = 129, dE[2] = 31.3914

k3[3] = 149, dE[3] = 30.2725

k3[6] = 190, dE[6] = 28.4774

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46:

k3[2] = 129, dE[2] = 31.3914

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

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k3[2] = 129, dE[2] = 31.3914

k3[4] = 152, dE[4] = 30.1211

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48:

k3[2] = 129, dE[2] = 31.3914

k3[4] = 152, dE[4] = 30.1211

k3[5] = 162, dE[5] = 29.6421

k3[7] = 198, dE[7] = 28.1838

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---

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k3[2] = 129, dE[2] = 31.3914  
k3[4] = 152, dE[4] = 30.1211  
k3[6] = 190, dE[6] = 28.4774  
k3[7] = 198, dE[7] = 28.1838  
k3[8] = 170, dE[8] = 29.2849

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k3[2] = 129, dE[2] = 31.3914  
k3[5] = 162, dE[5] = 29.6421  
k3[6] = 190, dE[6] = 28.4774  
k3[7] = 198, dE[7] = 28.1838  
k3[8] = 170, dE[8] = 29.2849

51:  
k3[3] = 149, dE[3] = 30.2725  
k3[4] = 152, dE[4] = 30.1211  
k3[5] = 162, dE[5] = 29.6421  
k3[6] = 190, dE[6] = 28.4774  
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k3[3] = 149, dE[3] = 30.2725  
k3[4] = 152, dE[4] = 30.1211  
k3[5] = 162, dE[5] = 29.6421  
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k3[4] = 152, dE[4] = 30.1211  
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54:  
k3[3] = 149, dE[3] = 30.2725  
k3[4] = 152, dE[4] = 30.1211  
k3[6] = 190, dE[6] = 28.4774  
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56:  
k3[4] = 152, dE[4] = 30.1211  
k3[5] = 162, dE[5] = 29.6421  
k3[6] = 190, dE[6] = 28.4774  
k3[7] = 198, dE[7] = 28.1838  
k3[8] = 170, dE[8] = 29.2849

Result for sEa: 8268.41

when

Result for sEb: 4961.05

[Program finished]

Example 2 :

```
//n = 5, N = 8*4
#include <iostream>
#include <cmath>
#include <cstdlib>
```

```

#include <ctime>
using namespace std;
int main() {
    srand(time(0));
    int N = 8*4;
    int kmax = 1000;
    int kmin = 1;
    int t = 0;
    int k3[N+1];
    double dE[N+1];

    while (t <= N) {
        int k_3 = -rand() % kmax + 2 * kmax;
        if (k_3 > 0) {
            t++;
            k3[t] = k_3;
            dE[t] = (1127186345 * sqrt((k_3 + 1) / (k_3 * sqrt(2 * k_3 + 2)))) / 8976748;
            cout << "k3[" << t << "] = " << k3[t] << ", dE[" << t << "] = " << dE[t] << endl;
        }
    }

    int l = 0;
    double sEa = 0;

    for (int i1 = 1; i1 <= N; i1++) {
        for (int i2 = 1; i2 <= N; i2++) {
            for (int i3 = 1; i3 <= N; i3++) {
                for (int i4 = 1; i4 <= N; i4++) {
                    for (int i5 = 1; i5 <= N; i5++) {
                        if (i1 < i2 && i2 < i3 && i3 < i4 && i4 < i5) {
                            l++;
                            cout << l << ":" << endl;
                            cout << "k3[" << i1 << "] = " << k3[i1] << ", dE[" << i1 << "] = " << dE[i1] << endl;
                            cout << "k3[" << i2 << "] = " << k3[i2] << ", dE[" << i2 << "] = " << dE[i2] << endl;
                            cout << "k3[" << i3 << "] = " << k3[i3] << ", dE[" << i3 << "] = " << dE[i3] << endl;
                            cout << "k3[" << i4 << "] = " << k3[i4] << ", dE[" << i4 << "] = " << dE[i4] << endl;
                            cout << "k3[" << i5 << "] = " << k3[i5] << ", dE[" << i5 << "] = " << dE[i5] << endl;
                            sEa += dE[i1] + dE[i2] + dE[i3] + dE[i4] + dE[i5];
                        }
                    }
                }
            }
        }
    }

    double sEb = 0;
    for (int i1 = 1; i1 <= N; i1++) {
        for (int i2 = 1; i2 <= N; i2++) {
            for (int i3 = 1; i3 <= N; i3++) {
                for (int i4 = 1; i4 <= N; i4++) {
                    for (int i5 = 1; i5 <= N; i5++) {
                        for (int i6 = 1; i6 <= N; i6++) {
                            for (int i7 = 1; i7 <= N; i7++) {
                                for (int i8 = 1; i8 <= N; i8++) {
                                    for (int i9 = 1; i9 <= N; i9++) {
                                        for (int i10 = 1; i10 <= N; i10++) {
                                            for (int i11 = 1; i11 <= N; i11++) {
                                                for (int i12 = 1; i12 <= N; i12++) {

```

We have

An algorithm giving sets of massive bosons-dark energy:  $\{dE[k3] = 2^{(7/4)} * gM * \sqrt{(k3d+1)/(k3 d^* \sqrt{2*k3d+2})}, k3d = 1+n, dk3d\}$  and sets of massive bosons-dark matter:  $\{dE[k3] = 2^{(7/4)} * gM * \sqrt{(k3n+1)/(k3n * \sqrt{2*k3n+2})}, k3n = 1+n, dk3n\}$

gM = sqrt(1393.6328858707575005182839547884);

and

dk3n = 1.255314934818507.10<sup>89</sup>

dk3d = 1.862840706286786.10<sup>147</sup>

## 1.10. Search for dk3

dE<sup>2</sup>[k3] =

{2^(7/2)\*gM^2\*k3/(k3\*sqrt(2\*k3+2)) → Potential energy

+2^(7/2)\*gM^2/(k3\*sqrt(2\*k3+2)) → E\_A.E\_B Kinematic energies}

dE[k3] = 2^(7/4)\*abs(gM)\*sqrt((k3+1)/(k3\*sqrt(2\*k3+2)))

E\_A.E\_B=dE\_A[k3].dE\_B[k3]=(2^(7/4)\*abs(gM)\*sqrt((k3a+1)/(k3a\*sqrt(2\*k3a+2))))\*(2^(7/4)\*abs(gM)\*sqrt((k3b+1)/(k3b\*sqrt(2\*k3b+2))))=2^(7/2)\*gM^2\*sqrt((k3a+1)/(k3a\*sqrt(2\*k3a+2)))\*sqrt((k3b+1)/(k3b\*sqrt(2\*k3b+2)))

[2^(7/2)\*gM^2\*sqrt((k3a+1)/(k3a\*sqrt(2\*k3a+2)))\*sqrt((k3b+1)/(k3b\*sqrt(2\*k3b+2))) = 2^(7/2) \*gM^2/(k3\*sqrt(2\*k3+2))], [k3]

→[(2^(7/2)\*gM^2\*sqrt((k3a+1)/(k3a\*sqrt(2\*k3a+2)))\*sqrt((k3b+1)/(k3b\*sqrt(2\*k3b+2))))^2=(2^(7/2)\*gM^2/(k3\*sqrt(2\*k3+2)))^2], [k3]

→[k3=-(%i\*(3^(5/2)\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(2/3)-sqrt(3))

+9\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(2/3)+6\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)+1)/(18\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)),

k3=(%i\*(3^(5/2)\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(2/3)-6\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)-1)/(18\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)),

-9\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(2/3)-6\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)-1)/(18\*((2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(k3a\*k3b\*(k3b\*(k3a\*(27\*sqrt(2\*k3a+2)\*sqrt(2\*k3b+2)-8)-8\*k3a-8)))/(4\*3^(3/2)\*(k3a+1)\*(k3b+1))+(k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2))/(2\*(k3a\*(2\*k3b+2)+2\*k3b+2))-1/27)^(1/3)),

k3=(9\*(9\*(2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(27\*k3a^2\*sqrt(2\*k3a+2)\*k3b^2\*sqrt(2\*k3b+2)+(-8\*k3a^2)-8\*k3a)\*k3b^2+(-8\*k3a^2)-8\*k3a)\*k3b)+3^(7/2)\*k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2)+((-4\*sqrt(3)\*k3a)-4\*sqrt(3))\*k3b-4\*sqrt(3)\*k3a-4\*sqrt(3))^(2/3)-3\*((4\*3^(7/2)\*k3a+4\*3^(7/2))\*k3b+4\*3^(7/2)\*k3a+4\*3^(7/2))^(1/3)\*(9\*(2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(27\*k3a^2\*sqrt(2\*k3a+2)\*k3b^2\*sqrt(2\*k3b+2)+(-8\*k3a^2)-8\*k3a)\*k3b^2+(-8\*k3a^2)-8\*k3a)\*k3b+3^(7/2)\*k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2)+((-4\*sqrt(3)\*k3a)-4\*sqrt(3))\*k3b-4\*sqrt(3)\*k3a-4\*sqrt(3))^(1/3)+((4\*3^(7/2)\*k3a+4\*3^(7/2))\*k3b+4\*3^(7/2)\*k3a+4\*3^(7/2))^(2/3))/(9\*((4\*3^(7/2)\*k3a+4\*3^(7/2))\*k3b+4\*3^(7/2)\*k3a+4\*3^(7/2))^(1/3)\*(9\*(2\*k3a+2)^(1/4)\*(2\*k3b+2)^(1/4)\*sqrt(27\*k3a^2\*sqrt(2\*k3a+2)\*k3b^2\*sqrt(2\*k3b+2)+(-8\*k3a^2)-8\*k3a)\*k3b^2+(-8\*k3a^2)-8\*k3a)\*k3b+3^(7/2)\*k3a\*sqrt(2\*k3a+2)\*k3b\*sqrt(2\*k3b+2)+((-4\*sqrt(3)\*k3a)-4\*sqrt(3))\*k3b-4\*sqrt(3)\*k3a-4\*sqrt(3))^(1/3))]

Example 1/3:

import cmath

---

```

kmin = -10
kmax = 10
for k3a in range(kmin, kmax+1):
    for k3b in range(kmin, kmax+1):
        if k3a*k3b*(4**3***(3/2)*(k3a+1)*(k3b+1))*(2*(k3a*(2*k3b+2)+2*k3b+2)) != 0:
            if 18*((((2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(k3a*k3b*(k3b*(k3a*(27*cmath.sqrt(2*k3a+2)*cmath.sqrt(2*k3b+2)-8)-8*k3a-8))))/(4**3***(3/2)*(k3a+1)*(k3b+1))+(k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2))/((2*(k3a*(2*k3b+2)+2*k3b+2))-1/27)***(1/3)) != 0:
                k3 = -(cmath.sqrt(-1)*(3***(5/2)*(((2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(k3a*k3b*(k3b*(k3a*(27*cmath.sqrt(2*k3a+2)*cmath.sqrt(2*k3b+2)-8)-8*k3a-8))))/(4**3***(3/2)*(k3a+1)*(k3b+1))+(k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2))/((2*(k3a*(2*k3b+2)+2*k3b+2))-1/27)***(2/3)-cmath.sqrt(3))+9*((((2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(k3a*k3b*(k3b*(k3a*(27*cmath.sqrt(2*k3a+2)*cmath.sqrt(2*k3b+2)-8)-8*k3a-8))))/(4**3***(3/2)*(k3a+1)*(k3b+1))+(k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2))/((2*(k3a*(2*k3b+2)+2*k3b+2))-1/27)***(2/3)-cmath.sqrt(3))+9*((((2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(k3a*k3b*(k3b*(k3a*(27*cmath.sqrt(2*k3a+2)*cmath.sqrt(2*k3b+2)-8)-8*k3a-8))))/(4**3***(3/2)*(k3a+1)*(k3b+1))+(k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2))/((2*(k3a*(2*k3b+2)+2*k3b+2))-1/27)***(1/3)+1)/(18*((((2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(k3a*k3b*(k3b*(k3a*(27*cmath.sqrt(2*k3a+2)*cmath.sqrt(2*k3b+2)-8)-8*k3a-8))))/(4**3***(3/2)*(k3a+1)*(k3b+1))+(k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2))/((2*(k3a*(2*k3b+2)+2*k3b+2))-1/27)***(1/3)) != 0:
                    print("k3 =",k3, "k3a =",k3a, "k3b =",k3b)
→ ... ....

```

### Example 3/3

```

import cmath
kmin = -10
max = 10

```

```

for k3a in range(kmin, kmax+1):
    for k3b in range(kmin, kmax+1):
        if k3a*k3b != 0:
            if(4**3***(3/2)*(k3a+1)*(k3b+1))*(2*(k3a*(2*k3b+2)+2*k3b+2))*(9*((4**3***(7/2)*k3a+4**3***(7/2))*k3b+4**3***(7/2)*k3a+4**3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(2/3)-3*((4**3***(7/2)*k3a+4**3***(7/2))*k3b+4**3***(7/2)*k3a+4**3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3)) != 0:
                k3 = (9*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(2/3)-3*((4**3***(7/2)*k3a+4**3***(7/2))*k3b+4**3***(7/2)*k3a+4**3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3)+((4**3***(7/2)*k3a+4**3***(7/2))*k3b+4**3***(7/2)*k3a+4**3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3))
                    print("k3 =",k3, "k3a =",k3a, "k3b =",k3b)
→ ... ....

```

And

```

import cmath
import math
kmin = -100000
kmax = 100000

```

```

for k3a in range(kmin, kmax+1):
    for k3b in range(kmin, kmax+1):

```

---

```

if k3a*k3b != 0:
    if(4**3***3/2)*(k3a+1)*(k3b+1))*(2*(k3a*(2*k3b+2)+2*k3b+2))*(9*((4**3**7/2)*k3a+4**3**7/2)*k3b+4**3**7/2)*k3a+4**3**7/2))**1/3)*(9*(2*k3a+2)**1/4)*(2*k3b+2)**1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3**7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))**1/3)!= 0:
        k3=(9*(9*(2*k3a+2)**1/4)*(2*k3b+2)**1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3**7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))**1/3)-3*((4**3**7/2)*k3a+4**3**7/2))**1/3)*(9*(2*k3a+2)**1/4)*(2*k3b+2)**1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3**7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))**1/3))/((4**3**7/2)*k3a+4**3**7/2))**1/3)/(9*((4**3**7/2)*k3a+4**3**7/2)*k3b+4**3**7/2)*k3a+4**3**7/2))**1/3)*(9*(2*k3a+2)**1/4)*(2*k3b+2)**1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3**7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))**1/3)
        if (abs(math.floor(abs(k3))-abs(k3)) <= 0.00000001) or (abs(math.ceil(abs(k3))-abs(k3)) <= 0.00000001):
            print("k3 = ",k3, "k3a = ",k3a, "k3b = ",k3b)
→ ...
k3 = (4.000000004358974+0j) k3a = 1 k3b = 12801
k3 = (5.00000000435709+0j) k3a = 1 k3b = 45001
k3 = (5.000000003098156+0j) k3a = 2 k3b = 16876
k3 = (6.00000000462856+0j) k3a = 2 k3b = 47629
k3 = (6.000000001318018+0j) k3a = 3 k3b = 28225
k3 = (6.000000002665895+0j) k3a = 4 k3b = 19846
k3 = (7.000000000527919+0j) k3a = 4 k3b = 48021
k3 = (8.000000000332687+0j) k3a = 6 k3b = 64513
k3 = (7.000000001934029+0j) k3a = 7 k3b = 25089
k3 = (7.0000000026068765+0j) k3a = 8 k3b = 21610
k3 = (8.00000000636057+0j) k3a = 8 k3b = 46657
k3 = (8.000000000825255+0j) k3a = 9 k3b = 40961
k3 = (9.0000000002365+0j) k3a = 9 k3b = 81001
k3 = (9.000000000297902+0j) k3a = 10 k3b = 72172
k3 = (8.000000001543293+0j) k3a = 12 k3b = 29953
k3 = (9.000000000712818+0j) k3a = 15 k3b = 46657
k3 = (8.000000002852211+0j) k3a = 16 k3b = 22033
k3 = (8.00000000365744+0j) k3a = 18 k3b = 19457
k3 = (9.000000001048175+0j) k3a = 18 k3b = 38476
k3 = (10.00000000425901+0j) k3a = 20 k3b = 63526
k3 = (10.000000000519831+0j) k3a = 22 k3b = 57501
k3 = (10.000000000678323+0j) k3a = 25 k3b = 50337
k3 = (9.000000002443311+0j) k3a = 27 k3b = 25201
k3 = (9.000000003038068+0j) k3a = 30 k3b = 22600
k3 = (11.000000000435202+0j) k3a = 33 k3b = 65825
k3 = (12.000000000241666+0j) k3a = 39 k3b = 92161
k3 = (10.000000002172683+0j) k3a = 44 k3b = 28126
k3 = (11.000000000785192+0j) k3a = 44 k3b = 49006
.....
k3 = (18.00000000223377+0j) k3a = 1026 k3b = 36973
k3 = (17.999999990966415+0j) k3a = 1028 k3b = 36901
k3 = (20.0000000007486+0j) k3a = 1050 k3b = 67265
k3 = (21.000000000465235+0j) k3a = 1078 k3b = 87400
k3 = (16.00000000895825+0j) k3a = 1088 k3b = 17425
k3 = (16.000000000566697+0j) k3a = 1090 k3b = 17393
k3 = (14.99999999213551+0j) k3a = 1092 k3b = 11880
k3 = (20.00000000097798+0j) k3a = 1200 k3b = 58850
k3 = (19.999999993160305+0j) k3a = 1202 k3b = 58752
.....

```

4d origin of dE = 4.Sqrt{(gM^2)/sqrt(2)} ~ 125.5673374143954990316092809188 GeV ((gM^2) = 1393.6328858707575005182 839547884 GeV<sup>2</sup>)

### 1.11. Initially

{dE : 1.607219735509044\*10^(-35),

gM : sqrt(1393.6328858707575005182839547884),

root(dE = 2^(7/4)\*gM\*sqrt((k3+1)/(k3\*sqrt(2\*k3+2))),k3,10,10^150)}

→ k3 = 1.862840706286786\*10<sup>147</sup> (Obtaining of k3min for dark matter effect\massive graviton.)

With

dE[k3] = 2^(7/4)\*abs(gM)\*sqrt((k3+1)/(k3\*sqrt(2\*k3+2)))

idE[k3] = 2^(7/4)\*sqrt((k3+1)/(k3\*sqrt(2\*k3+2)))

or

dE<sup>2</sup>[k3] = (2^(7/2)\*gM^2\*k3+2^(7/2)\*gM^2)/(k3\*sqrt(2\*k3+2)),

idE<sup>2</sup>[k3] = (2^(7/2)\*k3+2^(7/2))/(k3\*sqrt(2\*k3+2));

dE = 4\*sqrt((gM^2)\*|Val[1,2]|), Val[1,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3=1 and Y=2 and [X=-sqrt(2)\*%i, X=sqrt(2)\*%i]; dE = 4.Sqrt{(gM^2)}/sqrt(2) ~ 125.5673374143954990316092809188 GeV

Val[2,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 2 and Y = 2 and [X=-(2\*%i)/sqrt(3),X=(2\*%i)/sqrt(3)] → Val[2,2] = (sqrt(3)\*%i)/4

→ dE = 98.26175177406498 GeV,

Val[3,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 3 and Y = 2 and [X=-%i,X=%i] → Val[3,2] = %i/3

→ dE = 86.21315865135692 GeV,

.....

Val[4,2] = X/(X<sup>2</sup>+Y<sup>2</sup>) with k3 = 4 and Y = 2 and [X=-(2\*%i)/sqrt(5),X=(2\*%i)/sqrt(5)] → Val[4,2] = (sqrt(5)\*%i)/8

→ dE = 78.94628387056885 GeV,

.....

We obtain from result : An open string absorbing a massive graviton

H = ∫dσ [X<sup>2</sup>(σ)/2 + (∂X/∂σ)<sup>2</sup>/2] = m<sup>2</sup> = E\_A.E\_B/C<sup>4</sup> + Potential Energy<sup>2</sup>/C<sup>4</sup>

Thanks to the resolution of the Riemann hypothesis with the result-consequence a = ½ for n≡∞ :

{∫(1/(n+k)<sup>a</sup>,n) = (n+k)<sup>(1-a)</sup>/(1-a)

= -n<sup>(1-a)</sup>/(1-a);

n+k = (-1)<sup>(1/(1-a))</sup>\*n;

{n+k = (-1)<sup>(1/(1-a))</sup>\*n,

k=-1}

→ [n = -1/((-1)<sup>(1/(1-a))</sup>-1)]

--a = ½ → [n = -1/((-1)<sup>(1/(1-(1/2)))</sup>-1) = +∞].}, we introduce:

k3 variations and melting sign for b values:

sn1 = s2 = sin(log(2)\*b)

Eq1 :

Function: [0 = (8\*s2^6-24\*s2^4+24\*s2^2-8)^(2/3)\*(24\*k3^2\*s2^6-72\*k3^2\*s2^4-24\*k3^2)+4\*s2^4],

Eq2:

[0 = 64\*k3^4\*(k3^2\*((-27\*2^(2\*a+2)\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(4/3))-9\*2^(4\*a+3)\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(2/3)+2^(6\*a+4))+81\*2^(6\*a+6)\*k3^6\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(4/3)-9\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(4/3)-9\*2^(6\*a+6)\*k3^4\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(2/3)-3\*2^(2\*a+1)\*(8\*s2^6-24\*s2^4+24\*s2^2-8)^(2/3)].]

Examples :

k3 = -5,

Root (0 = (8\*s2^6-24\*s2^4+24\*s2^2-8)^(2/3)\*(24\*(-5)^2\*s2^6-72\*(-5)^2\*s2^4-24\*(-5)^2)+4\*s2^4, {s2, -1, 1})

{s2->-0.98828435414}

{s2->0.98828435413},

{s2->-0.98828435414}

[log(2)\*b+2\*k\*%pi = asin(-0.98828435414)]

#include <iostream>

#include <cmath>

---

```

int main() {
    for (int k = -10; k <= 10; k++) {
        if (k != 0) {
            float b = (asin(-0.98828435414) - 2 * k * M_PI) / log(2);
            std::cout << "b = " << b << std::endl;
        }
    }
    return 0;
}
→ b=88.60207635515901
b=79.53735607150462
b=70.47263578785024
b=61.40791550419585
b=52.34319522054146
b=43.27847493688707
b=34.21375465323268
b=25.1490343695783 (near ± 25.010857580145688763...)
b=16.08431408592391
b=7.019593802269521
b=-11.10984676503925
b=-20.17456704869364
b=-29.23928733234803
b=-38.30400761600242
b=-47.3687278996568
b=-56.43344818331119
b=-65.49816846696557
b=-74.56288875061996
b=-83.62760903427434
b=-92.69232931792874

```

Going further :

k Partie imaginaire de  $\rho_k$

$1 \pm 14.134\ 725\ 141\ 734\ 693\ 790\dots$

$2 \pm 21.022\ 039\ 638\ 771\ 554\ 993\dots$

$3 \pm 25.010\ 857\ 580\ 145\ 688\ 763\dots$

$4 \pm 30.424\ 876\ 125\ 859\ 513\ 210\dots$

Interactions of two 4d string one of spin +2 and one of spin -2 with an open string. 4d string : Trefoil Knot [15]. For values  $(k_{max}, |k_{min}|) \ll 100000$ , rich values of  $k_3$  and  $dE_{k3}$  are not obtained, but for values  $(k_{max}, |k_{min}|) \geq 100000$ , we look for  $|\text{real}(\text{values } dE_{k3})| \leq 4 \text{ GeV}$ .

With  $dE^2[k3] =$

$\{2^{(7/2)} * gM^2 * k3 / (k3 * \sqrt{2 * k3 + 2})\} \rightarrow \text{Potential energy}$

$\{2^{(7/2)} * gM^2 / (k3 * \sqrt{2 * k3 + 2})\} \rightarrow E_A, E_B \text{ Kinematic energies}\}$

We calculate  $E_{\text{Potential energy}} = gM \cdot \sqrt{(2^{(7/2)} * k3 / (k3 * \sqrt{2 * k3 + 2}))}$

And obtain  $E_{\text{Kinematic energy}} \neq E_A \text{ or } E_B$ ;  $E_{\text{Kinematic energy}} = dE_{k3} - E_{\text{Potential energy}}$

The energy of an open string is with

$E_{\text{correction}} = \text{real}(\zeta(\frac{1}{2} + i.b)) > 0 = \text{real1}(\zeta(\frac{1}{2} + i.b))$

With

$\zeta(s) = 1^{-s} + 2^{-s} + 3^{-s} + 4^{-s} + \dots$

Then

$\Delta E(k) = E_{\text{correction}} * \hbar * \omega(k)$

$\Delta E(k) = \text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \omega(k)$

With

$\text{real1}(\zeta(\frac{1}{2} + i.b)) / \text{real}(iE_p + iE_k) = \text{image1}(\zeta(\frac{1}{2} + i.b)) / \text{image}(iE_p + iE_k)$

Potential energy =  $2^{(7/4)} * gM * \sqrt{k3 / (k3 * \sqrt{2 * k3 + 2}))}$

Kinematic energy in the Way that :

---

$$\Delta E(k) = \text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \omega(k)$$

With

$$\text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \omega(k) / \text{real}(iE_p + iE_k) = \text{image1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \omega(k) / \text{image}(iE_p + iE_k);$$

$$\text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{real}(iE_p + iE_k) = \text{image1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{image}(iE_p + iE_k);$$

$$\text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{real}(iE_p + iE_k) = \text{image1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{image}(iE_p + iE_k)$$

with

$$\omega(k) = \sqrt{k/m} * \sin(k\lambda/2)$$

$$m = idE_k3 = 2^{(7/4)*\sqrt{(k^3+1)/(k^3*\sqrt{2*k^3+2})}}$$

$$Ek = idE_k3.gM - Ep = 2^{(7/4)*gM*\sqrt{(k^3+1)/(k^3*\sqrt{2*k^3+2})}} - Ep,$$

$$\text{real1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{real}(idE_k3) = \text{image1}(\zeta(\frac{1}{2} + i.b)) * \hbar * \sqrt{k/m} * \sin(k\lambda/2) / \text{image}(idE_k3)$$

Where k is the wave vector associated with the vibration and  $\lambda$  is the wavelength of the vibration.

If the wave vector k is close to zero, it means that the wavelength is very long and the atoms will vibrate together as if they were a single atom. The corresponding angular frequency will then be close to zero and the associated energy variation will be small.

### 1.11.1. Algorithm

```
import cmath
import math
import sys

def main():
    h = 6.626070e-34 # J s
    Lmin = 1
    Lmax = 1000
    k_i = 1
    k_f = 1000
    kmin = -100000
    kmax = 100000
    i0 = 0
    i1 = 0
    s2 = [0] * 101
    Ns = sys.maxsize
    for t in range(-100, -1+1):
        s2[-100] = -0.99941091795
        s2[-99] = -0.99940496942
        s2[-98] = -0.9993988995
        s2[-97] = -0.99939270444
        s2[-96] = -0.99938638046
        s2[-95] = -0.9993799232
        s2[-94] = -0.99937332878
        s2[-93] = -0.99936659252
        s2[-92] = -0.99935970985
        s2[-91] = -0.99935267598
        s2[-90] = -0.99934548584
        s2[-89] = -0.99933813417
        s2[-88] = -0.99933061549
        s2[-87] = -0.99932292402
        s2[-86] = -0.99931505375
        s2[-85] = -0.99930699836
        s2[-84] = -0.99929869643
        s2[-83] = -0.99929030539
        s2[-82] = -0.99928165377
        s2[-81] = -0.9992727885
        s2[-80] = -0.99926370171
        s2[-79] = -0.9992543849
        s2[-78] = -0.99924482941
```

---

s2[-77] = -0.99923502576  
s2[-76] = -0.99922496418  
s2[-75] = -0.99921463444  
s2[-74] = -0.99920402561  
s2[-73] = -0.99919312627  
s2[-72] = -0.99918192428  
s2[-71] = -0.99917040687  
s2[-70] = -0.99915856056  
s2[-69] = -0.99914635017  
s2[-68] = -0.99913382302  
s2[-67] = -0.99912090071  
s2[-66] = -0.99910758696  
s2[-65] = -0.99909386377  
s2[-64] = -0.9990797119  
s2[-63] = -0.999065111  
s2[-62] = -0.99905003931  
s2[-61] = -0.99903447372  
s2[-60] = -0.99901838949  
s2[-59] = -0.99900176035  
s2[-58] = -0.99898455808  
s2[-57] = -0.9989667525  
s2[-56] = -0.99894831137  
s2[-55] = -0.99892920002  
s2[-54] = -0.99890938121  
s2[-53] = -0.99888881494  
s2[-52] = -0.99886745811  
s2[-51] = -0.99884526425  
s2[-50] = -0.99882218315  
s2[-49] = -0.99879816055  
s2[-48] = -0.99877313759  
s2[-47] = -0.99874705052  
s2[-46] = -0.99871982993  
s2[-45] = -0.99869140034  
s2[-44] = -0.99866167938  
s2[-43] = -0.99863057697  
s2[-42] = -0.99859799455  
s2[-41] = -0.99856382388  
s2[-40] = -0.99852794595  
s2[-39] = -0.99849022951  
s2[-38] = -0.99845048535  
s2[-37] = -0.99840868533  
s2[-36] = -0.99836451834  
s2[-35] = -0.99831782967  
s2[-34] = -0.99826839698  
s2[-33] = -0.99821597105  
s2[-32] = -0.99816027152  
s2[-31] = -0.99810098191  
s2[-30] = -0.99803774353  
s2[-29] = -0.99797014832  
s2[-28] = -0.99789768542  
s2[-27] = -0.99781993386  
s2[-26] = -0.99773619296  
s2[-25] = -0.99764575523  
s2[-24] = -0.99754778226  
s2[-23] = -0.99744130083  
s2[-22] = -0.9973251523  
s2[-21] = -0.99719795755  
s2[-20] = -0.99705806211

---

```

s2[-19] = -0.99690346375
s2[-18] = -0.996731716
s2[-17] = -0.99653979777
s2[-16] = -0.99632393409
s2[-15] = -0.99607934533
s2[-14] = -0.99579988915
s2[-13] = -0.99547753758
s2[-12] = -0.99510159327
s2[-11] = -0.99465747946
s2[-10] = -0.99412479292
s2[-9] = -0.99347415065
s2[-8] = -0.9926614346
s2[-7] = -0.99161749897
s2[-6] = -0.9902273088
s2[-5] = -0.98828435414
s2[-4] = -0.98537717072
s2[-3] = -0.98055121855
s2[-2] = -0.97097209774
s2[-1] = -0.94282328841

for k_0 in range(-10, 10):
    if k_0 != 0:
        b = (math.asin(s2[t]) - 2 * k_0 * math.pi) / math.log(2)
        ReS = 1
        ImS = 0
        for l in range(2, Ns + 1):
            s0 = 1/l***(1/2+b*cmath.sqrt(-1))
            if s0.real > 0:
                ReS += s0.real
                ImS += s0.imag
            if l >= Ns:
                print("b = ", b)
        print("ReS+i.ImS = ", ReS, "+i.", ImS)
    print()

for x in range(kmin, kmax+1):
    for y in range(kmin, kmax+1):
        if x*y != 0:
            eq1 = (4*3***((3/2)*(x+1)*(y+1)))
            eq2 = (2*(x*(2*y+2)+2*y+2))
            eq3 = (9*((4*3***((7/2)*x+4*3***((7/2)*y+4*3***((7/2)*x+4*3***((7/2))))***((1/3)*(9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x-2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3)*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((2/3)-3*((4*3***((7/2)*x+4*3***((7/2)*y+4*3***((7/2)*x+4*3***((7/2))))***((1/3)*(9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((1/3)+((4*3***((7/2)*x+4*3***((7/2)*y+4*3***((7/2)*x+4*3***((7/2))))***((1/3)*(9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((1/3))) if eq1 * eq2 * eq3 != 0:
                k3 = (9*((9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((2/3))-3*((4*3***((7/2)*x+4*3***((7/2)*y+4*3***((7/2)*x+4*3***((7/2))))***((1/3)*(9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((1/3)+((4*3***((7/2)*x+4*3***((7/2)*y+4*3***((7/2)*x+4*3***((7/2))))***((1/3)*(9*(2*x+2))))***((1/4)*(2*y+2))))***((1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+((-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3***((7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))***((1/3))) if (abs(math.floor(abs(k3))) - abs(k3)) <= 0.00000001) or (abs(math.ceil(abs(k3))) - abs(k3)) <= 0.00000001):
        i0 += 1
        gM = cmath.sqrt(1393.6328858707575005182839547884)
        dEk3 = 2**((7/4)*gM*cmath.sqrt((k3+1)/(k3*cmath.sqrt(2*k3+2))))

```

---

```

E_A = 2**((7/4)*gM*cmath.sqrt((x+1)/(x*cmath.sqrt(2*x+2))) # x = k3a
E_B = 2**((7/4)*gM*cmath.sqrt((y+1)/(y*cmath.sqrt(2*y+2))) # y = k3b
idEk3 = 2**((7/4)*cmath.sqrt((k3+1)/(k3*cmath.sqrt(2*k3+2))))
```

for Lambda in range(Lmin, Lmax + 1):  
 for k in range(k\_i, k\_f + 1):  
 # m = idEk3  
 Sx=(ReS+cmath.sqrt(-1)\*ImS)\*(h/(2\*math.pi))\*cmath.sqrt(k/idEk3)\*math.sin(k\*Lambd a/2)

if (Sx.real/idEk3.real)/(Sx.imag/idEk3.imag) < 1.2 and  
(Sx.real/idEk3.real)/(Sx.imag/idEk3.imag) > 1/1.2 or (abs(dEk3.real) <= 4 or abs(abs(dEk3.real) - E\_A.real) <= 0.01 or abs(abs(dEk3.real) - E\_B.real) <= 0.01):  
 i1 += 1  
 print("Case ", i1, "/", i0, ":")  
 print("k3 = ", k3, "k3a = ", x, "k3b = ", y)  
 rk3 = cmath.sqrt(k3.real\*\*2 + k3.imag\*\*2)  
 print("rk3 = ", rk3)  
 dErk3 = 2\*\*((7/4)\*gM\*cmath.sqrt((rk3.real+1)/(rk3.real\*cmath.sqrt(2\*rk3.real+2))))  
 rdEk3 = cmath.sqrt(dEk3.real\*\*2 + dEk3.imag\*\*2)  
 E\_potential = gM\*cmath.sqrt(2\*\*((7/2)\*k3/(k3\*cmath.sqrt(2\*k3+2))))  
 E\_kinematic = dEk3 - E\_potential  
 print("dEk3 = ", dEk3, " GeV")  
 print("rdEk3 = ", rdEk3)  
 print("dErk3 = ", dErk3, " GeV")  
 print("E\_potential = ", E\_potential, " GeV")  
 print("E\_kinematic = ", E\_kinematic, " GeV")  
 print()  
 if abs(abs(dEk3.real) - E\_A.real) <= 0.01 or abs(abs(dEk3.real) - E\_B.real) <= 0.01:  
 print("E\_A = ", E\_A, " GeV")  
 print("E\_B = ", E\_B, " GeV")  
 print("real(dEk3) = ", dEk3.real, " GeV")  
 print()  
 if (Sx.real/idEk3.real)/(Sx.imag/idEk3.imag) < 1.2 and (Sx.real/idEk3.real)/(Sx.imag/idEk3.imag) > 1/1.2:  
 print("k = ", k)  
 print("λ = ", Lambda)  
 print()  
if \_\_name\_\_ == "\_\_main\_\_":
 main()

A better algorithm  $\zeta(\frac{1}{2} + i.b)$  generator is :

```

import cmath
import math
import sys
def main():
    s2 = [0] * 101
    Ns = sys.maxsize
    for t in range(-100, -1+1):
        s2[-100] = -0.99941091795
        s2[-99] = -0.99940496942
        s2[-98] = -0.9993988995
        s2[-97] = -0.99939270444
        s2[-96] = -0.99938638046
        s2[-95] = -0.9993799232
        s2[-94] = -0.99937332878
        s2[-93] = -0.99936659252
        s2[-92] = -0.99935970985
        s2[-91] = -0.99935267598
        s2[-90] = -0.99934548584

```

---

s2[-89] = -0.99933813417  
s2[-88] = -0.99933061549  
s2[-87] = -0.99932292402  
s2[-86] = -0.99931505375  
s2[-85] = -0.99930699836  
s2[-84] = -0.99929869643  
s2[-83] = -0.99929030539  
s2[-82] = -0.99928165377  
s2[-81] = -0.9992727885  
s2[-80] = -0.99926370171  
s2[-79] = -0.9992543849  
s2[-78] = -0.99924482941  
s2[-77] = -0.99923502576  
s2[-76] = -0.99922496418  
s2[-75] = -0.99921463444  
s2[-74] = -0.99920402561  
s2[-73] = -0.99919312627  
s2[-72] = -0.99918192428  
s2[-71] = -0.99917040687  
s2[-70] = -0.99915856056  
s2[-69] = -0.99914635017  
s2[-68] = -0.99913382302  
s2[-67] = -0.99912090071  
s2[-66] = -0.99910758696  
s2[-65] = -0.99909386377  
s2[-64] = -0.9990797119  
s2[-63] = -0.999065111  
s2[-62] = -0.99905003931  
s2[-61] = -0.99903447372  
s2[-60] = -0.99901838949  
s2[-59] = -0.99900176035  
s2[-58] = -0.99898455808  
s2[-57] = -0.9989667525  
s2[-56] = -0.99894831137  
s2[-55] = -0.99892920002  
s2[-54] = -0.99890938121  
s2[-53] = -0.99888881494  
s2[-52] = -0.99886745811  
s2[-51] = -0.99884526425  
s2[-50] = -0.99882218315  
s2[-49] = -0.99879816055  
s2[-48] = -0.99877313759  
s2[-47] = -0.99874705052  
s2[-46] = -0.99871982993  
s2[-45] = -0.99869140034  
s2[-44] = -0.99866167938  
s2[-43] = -0.99863057697  
s2[-42] = -0.99859799455  
s2[-41] = -0.99856382388  
s2[-40] = -0.99852794595  
s2[-39] = -0.99849022951  
s2[-38] = -0.99845048535  
s2[-37] = -0.99840868533  
s2[-36] = -0.99836451834  
s2[-35] = -0.99831782967  
s2[-34] = -0.99826839698  
s2[-33] = -0.99821597105  
s2[-32] = -0.99816027152

---

```
s2[-31] = -0.99810098191
s2[-30] = -0.99803774353
s2[-29] = -0.99797014832
s2[-28] = -0.99789768542
s2[-27] = -0.99781993386
s2[-26] = -0.99773619296
s2[-25] = -0.99764575523
s2[-24] = -0.99754778226
s2[-23] = -0.99744130083
s2[-22] = -0.9973251523
s2[-21] = -0.99719795755
s2[-20] = -0.99705806211
s2[-19] = -0.99690346375
s2[-18] = -0.996731716
s2[-17] = -0.99653979777
s2[-16] = -0.99632393409
s2[-15] = -0.99607934533
s2[-14] = -0.99579988915
s2[-13] = -0.99547753758
s2[-12] = -0.99510159327
s2[-11] = -0.99465747946
s2[-10] = -0.99412479292
s2[-9] = -0.99347415065
s2[-8] = -0.9926614346
s2[-7] = -0.99161749897
s2[-6] = -0.9902273088
s2[-5] = -0.98828435414
s2[-4] = -0.98537717072
s2[-3] = -0.98055121855
s2[-2] = -0.97097209774
s2[-1] = -0.94282328841
```

```
for k_0 in range(-10, 10):
    if k_0 != 0:
        b = (math.asin(s2[t]) - 2 * k_0 * math.pi) / math.log(2)
        ReS = 1
        ImS = 0
        for l in range(2, Ns + 1):
            s0 = 1/l***(1/2+b*cmath.sqrt(-1))
            if s0.real > 0:
                ReS += s0.real
                ImS += s0.imag
            if l >= Ns:
                print("b = ",b)
            print("ReS+i.ImS = ", ReS, "+i.", ImS)
            print()
if __name__ == "__main__":
    main()
```

We obtain results similar to :

```
import cmath
import math
def main():
    s2 = [0] * 6
    Ns = 1000000000
    for t in range(-5, -1+1):
        s2[-5] = -0.98828435414
        s2[-4] = -0.98537717072
```

---

```

s2[-3] = -0.98055121855
s2[-2] = -0.97097209774
s2[-1] = -0.94282328841
for k_0 in range(-10, 10):
    if k_0 != 0:
        b = (math.asin(s2[t]) - 2 * k_0 * math.pi) / math.log(2)
        ReS = 1
        ImS = 0
        for l in range(2, Ns + 1):
            s0 = 1/l***(1/2+b*cmath.sqrt(-1))
            if s0.real > 0:
                ReS += s0.real
                ImS += s0.imag
            if l >= Ns:
                print("b = ",b)
        print("ReS+i.ImS = ", ReS, "+i.", ImS)
        print()

if __name__ == "__main__":
    main()
→ b = 88.60207635515901
ReS+i.ImS = 6307.844896030516 +i. -28.94938165387543
b = 79.53735607150463
ReS+i.ImS = 6434.37737066339 +i. 11.242220705893391
ReS+i.ImS = 6335.630982820043 +i. -44.06143464461285
b = 61.40791550419585
ReS+i.ImS = 6388.238302501553 +i. 108.25945207135854
ReS+i.ImS = 6382.172075003123 +i. -61.24789663387373
b = 43.27847493688707
ReS+i.ImS = 6265.140783718337 +i. 97.21067855763751
ReS+i.ImS = 6478.890842451481 +i. -93.52071152141292
ReS+i.ImS = 6181.543372422819 +i. -122.22486115007362
b = 16.08431408592391
ReS+i.ImS = 6692.738286329365 +i. 142.35970324080344
ReS+i.ImS = 6099.5141308650045 +i. -433.9284953584362
ReS+i.ImS = 6221.895473340011 +i. 280.61671644842875
b = -20.174567048693643
ReS+i.ImS = 6618.610594190466 +i. -134.43579349798716
ReS+i.ImS = 6213.541197470559 +i. 107.90232364995555
ReS+i.ImS = 6471.434206720912 +i. 84.35606321963408
b = -47.3687278996568
ReS+i.ImS = 6268.873089628677 +i. -80.16737814175987
ReS+i.ImS = 6383.614914697005 +i. 56.515709447766845
b = -65.49816846696558
ReS+i.ImS = 6382.085124104104 +i. -101.30322907646526
ReS+i.ImS = 6339.58171487993 +i. 44.51747397056369
b = -83.62760903427434
ReS+i.ImS = 6431.167438821539 +i. -15.818420310540942
b = 88.62804490801527
ReS+i.ImS = 6306.284430038629 +i. 22.223163074471593
ReS+i.ImS = 6425.97239428184 +i. -39.483157160381566
... ...
From
b = 88.60207635515901
b = 79.53735607150463
b = 70.47263578785024
b = 61.40791550419585
b = 52.34319522054147

```

---

b = 43.27847493688707  
b = 34.213754653232684  
b = 25.149034369578295  
b = 16.08431408592391  
b = 7.0195938022695215  
b = -11.109846765039254  
b = -20.174567048693643  
b = -29.239287332348027  
b = -38.304007616002416  
b = -47.3687278996568  
b = -56.433448183311185  
b = -65.49816846696558  
b = -74.56288875061996  
b = -83.62760903427434  
b = 88.62804490801527  
b = 79.56332462436087  
b = 70.49860434070649  
b = 61.433884057052104  
b = 52.369163773397716  
b = 43.30444348974333  
b = 34.23972320608894  
b = 25.175002922434555  
b = 16.11028263878017  
b = 7.045562355125782  
b = -11.083878212182993  
b = -20.14859849583738  
b = -29.21331877949177  
b = -38.27803906314616  
b = -47.34275934680055  
b = -56.40747963045494  
b = -65.47219991410932  
b = -74.5369201977637  
b = -83.6016404814181  
b = 88.66602097606453  
b = 79.60130069241013  
b = 70.53658040875575  
b = 61.47186012510136  
b = 52.40713984144697  
b = 43.34241955779259  
b = 34.2776992741382  
b = 25.21297899048381  
b = 16.14825870682942  
b = 7.083538423175033  
b = -11.045902144133743  
b = -20.11062242778813  
b = -29.175342711442514  
b = -38.240062995096906  
b = -47.30478327875129  
b = -56.369503562405676  
b = -65.43422384606006  
b = -74.49894412971446  
b = -83.56366441336884  
b = 88.72948326417199  
b = 79.66476298051761  
b = 70.60004269686323  
b = 61.53532241320883  
b = 52.47060212955444  
b = 43.405881845900055

b = 34.34116156224567  
b = 25.27644127859128  
b = 16.211720994936893  
b = 7.147000711282508  
b = -10.982439856026266  
b = -20.047160139680656  
b = -29.111880423335045  
b = -38.17660070698943  
b = -47.24132099064382  
b = -56.30604127429821  
b = -65.37076155795259  
b = -74.43548184160699  
b = -83.50020212526137  
b = 88.87124212439919  
b = 79.8065218407448  
b = 70.74180155709041  
b = 61.67708127343602  
b = 52.612360989781635  
b = 43.54764070612725  
b = 34.482920422472866  
b = 25.418200138818474  
b = 16.353479855164085  
b = 7.2887595715097  
b = -10.840680995799076  
b = -19.905401279453464  
b = -28.970121563107853  
b = -38.03484184676224  
b = -47.09956213041663  
b = -56.16428241407101  
b = -65.2290026977254  
b = -74.29372298137979  
b = -83.35844326503418

11

The function used to calculate k3 gives either false integers or real integers.

For a definition of 1.0e-5, as in the command line: if ( $\text{abs}(\text{math.floor}(\text{abs}(k3)) - \text{abs}(k3)) \leq 0.00001$ ) or ( $\text{abs}(\text{math.ceil}(\text{abs}(k3)) - \text{abs}(k3)) \leq 0.00001$ )

Many of the k3s obtained are false integers.

For a definition of 1.0e-8, as in the command line: if ( $\text{abs}(\text{math.floor}(\text{abs}(k3)) - \text{abs}(k3)) \leq 0.00000001$ ) or ( $\text{abs}(\text{math.ceil}(\text{abs}(k3)) - \text{abs}(k3)) \leq 0.00000001$ )

The  $k_3$  obtained are much less likely to be false integers.

With a definition increased from  $1.0e-5$  to  $1.0e-8$  and ever more increased with the calculation definition always proportionally increased, we will have more and more exact k3 values over a wider margin [kmin, kmax].

These obtained k3 will help in the calculation of massive gravitons for dark matter (dark matter effect), initially obtained with a calculated variation of  $\Delta k_{3n} = 1.255314934818507 \times 10^{89}$

And massive gravitons for dark energy, initially obtained with a calculated variation of  $dk3d = 1.862840706286786 \times 10^{147}$  ( $dk3 \neq 1$  leads to a quantum entanglement process.).

And  $3 = \sum EnergieDarkEnergy / \sum EnergieDarkMatter$ .

We have

We have

$$k3 = \frac{9 \cdot (9 \cdot (2 \cdot k3a + 2)^{1/4} \cdot (2 \cdot k3b + 2)^{1/4}) \cdot \sqrt{27 \cdot k3a^2 \cdot \sqrt{2 \cdot \sqrt{2 \cdot k3a + 2} \cdot k3b^2 \cdot \sqrt{2 \cdot k3b + 2} + (-8 \cdot k3a^2) - 8 \cdot k3a} \cdot k3b^2 + (-8 \cdot k3a^2) - 8 \cdot k3a) \cdot k3b + 3^{7/2} \cdot k3a \cdot \sqrt{2 \cdot k3a + 2} \cdot k3b \cdot \sqrt{2 \cdot k3b + 2} + (-4 \cdot \sqrt{3} \cdot k3a) - 4 \cdot \sqrt{3} \cdot k3b - 4 \cdot \sqrt{3} \cdot k3a - 4 \cdot \sqrt{3}}^{(2/3)} - 3 \cdot ((4 \cdot 3^{7/2} \cdot k3a + 4 \cdot 3^{7/2}) \cdot k3b + 4 \cdot 3^{7/2} \cdot k3a + 4 \cdot 3^{7/2})^{1/3} \cdot (9 \cdot (2 \cdot k3a + 2)^{1/4} \cdot (2 \cdot k3b + 2)^{1/4} \cdot \sqrt{27 \cdot k3a^2 \cdot \sqrt{2 \cdot \sqrt{2 \cdot k3a + 2} \cdot k3b^2 \cdot \sqrt{2 \cdot k3b + 2} + (-8 \cdot k3a^2) - 8 \cdot k3a} \cdot k3b^2 + (-8 \cdot k3a^2) - 8 \cdot k3a) \cdot k3b + 3^{7/2} \cdot k3a \cdot \sqrt{2 \cdot k3a + 2} \cdot k3b \cdot \sqrt{2 \cdot k3b + 2} + (-4 \cdot \sqrt{3} \cdot k3a) - 4 \cdot \sqrt{3} \cdot k3b - 4 \cdot \sqrt{3} \cdot k3a - 4 \cdot \sqrt{3}}^{(2/3)} + (4 \cdot 3^{7/2})^{1/3})}{\dots}$$

---

$7/2)*k3a+4*3^(7/2))*k3b+4*3^(7/2)*k3a+4*3^(7/2))^(2/3))/(9*((4*3^(7/2)*k3a+4*3^(7/2))*k3b+4*3^(7/2)*k3a+4*3^(7/2)))^(1/3)*(9*(2*k3a+2)^(1/4)*(2*k3b+2)^(1/4)*sqrt(27*k3a^2*sqrt(2*k3a+2)*k3b^2*sqrt(2*k3b+2)+(-8*k3a^2)-8*k3a)*k3b^2+((-8*k3a^2)-8*k3a)*k3b)+3^(7/2)*k3a*sqrt(2*k3a+2)*k3b*sqrt(2*k3b+2)+((-4*sqrt(3)*k3a)-4*sqrt(3))*k3b-4*sqrt(3)*k3a-4*sqrt(3))^(1/3))$

$k3a \rightarrow 4d$  massive graviton mass calculation.

$k3b \rightarrow$  a second 4d massive graviton mass calculation.

Algorithm :

```

import cmath
import math
kmin = -100000
kmax = 100000
i0 = 0
i1 = 0

```

for  $x$  in range(kmin, kmax+1):

    for  $y$  in range(kmin, kmax+1):

        if  $x*y != 0$ :

            eq1 =  $(4*3^{**}(3/2)*(x+1)*(y+1))$

            eq2 =  $(2*(x*(2*y+2)+2*y+2))$

            eq3 =  $(9*((4*3^{**}(7/2)*x+4*3^{**}(7/2))*y+4*3^{**}(7/2)*x+4*3^{**}(7/2)))^{**}(1/3)*(9*(2*x+2)^{**}(1/4)*(2*y+2)^{**}(1/4)*cmath.$

            sqrt(27\*x\*\*2\*cmath.sqrt(2\*x+2)\*y\*\*2\*cmath.sqrt(2\*y+2)+(-8\*x\*\*2)-8\*x)\*y\*\*2+((-8\*x\*\*2)-8\*x)\*y)+3^{\*\*}(7/2)\*x\*cmath.sqrt(2\*x+2)\*y\*cmath.sqrt(2\*y+2)+((-4\*cmath.sqrt(3)\*x)-4\*cmath.sqrt(3))\*y-4\*cmath.sqrt(3)\*x-4\*cmath.sqrt(3))^{\*\*}(1/3))

        if eq1 \* eq2 \* eq3 != 0:

            k3 =  $(9*(9*(2*x+2)^{**}(1/4)*(2*y+2)^{**}(1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+(-8*x**2)-8*x)*y**2+((-8*x**2)-8*x)*y)+3^{**}(7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))^{**}(2/3)-3*((4*3^{**}(7/2)*x+4*3^{**}(7/2))*y+4*3^{**}(7/2)*x+4*3^{**}(7/2))^{**}(1/3)*(9*(2*x+2)^{**}(1/4)*(2*y+2)^{**}(1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+(-8*x**2)-8*x)*y)+3^{**}(7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3)*x-4*cmath.sqrt(3))^{**}(1/3)+((4*3^{**}(7/2)*x+4*3^{**}(7/2))*y+4*3^{**}(7/2)*x+4*3^{**}(7/2))^{**}(1/3)*(9*(2*x+2)^{**}(1/4)*(2*y+2)^{**}(1/4)*cmath.sqrt(27*x**2*cmath.sqrt(2*x+2)*y**2*cmath.sqrt(2*y+2)+(-8*x**2)-8*x)*y)+3^{**}(7/2)*x*cmath.sqrt(2*x+2)*y*cmath.sqrt(2*y+2)+((-4*cmath.sqrt(3)*x)-4*cmath.sqrt(3))*y-4*cmath.sqrt(3))^{**}(1/3))$

            if (abs(math.floor(abs(k3)) - abs(k3)) <= 0.00000001) or (abs(math.ceil(abs(k3)) - abs(k3)) <= 0.00000001):

                i0 += 1

                gM = cmath.sqrt(1393.6328858707575005182839547884)

                dEk3 =  $2^{**}(7/4)*gM*cmath.sqrt((k3+1)/(k3*cmath.sqrt(2*k3+2)))$

                E\_A =  $2^{**}(7/4)*gM*cmath.sqrt((x+1)/(x*cmath.sqrt(2*x+2)))#x = k3a$

                E\_B =  $2^{**}(7/4)*gM*cmath.sqrt((y+1)/(y*cmath.sqrt(2*y+2)))#y = k3b$

                if abs(dEk3.real) <= 4 or abs(abs(dEk3.real) - E\_A.real) <= 0.01 or abs(abs(dEk3.real) - E\_B.real) <= 0.01:

                    i1 += 1

                    print("Case ", i1, "/", i0, ":")

                    print("k3 = ", k3, "k3a = ", x, "k3b = ", y)

                    rk3 = cmath.sqrt(k3.real\*\*2 + k3.imag\*\*2)

                    print("rk3 = ", rk3)

dErk3 =  $2^{**}(7/4)*gM*cmath.sqrt((rk3.real+1)/(rk3.real*cmath.sqrt(2*rk3.real+2)))$

rdEk3 = cmath.sqrt(dEk3.real\*\*2 + dEk3.imag\*\*2)

E\_potential =  $gM*cmath.sqrt(2^{**}(7/2)*k3/(k3*cmath.sqrt(2*k3+2)))$

E\_kinematic = dEk3 - E\_potential

print("dEk3 = ", dEk3, " GeV")

print("rdEk3 = ", rdEk3)

print("dErk3 = ", dErk3, " GeV")

print("E\_potential = ", E\_potential, " GeV")

print("E\_kinematic = ", E\_kinematic, " GeV")

```

print()
if abs(abs(dEk3.real) - E_A.real) <= 0.01 or abs(abs(dEk3.real) - E_B.real) <= 0.01:
    print("E_A = ", E_A, " GeV")
    print("E_B = ", E_B, " GeV")
    print("real(dEk3) = ", dEk3.real, " GeV")
    print()

```

We obtain from result : An open string absorbing a massive graviton

$$H = \int d\sigma [X^2(\sigma)/2 + (\partial X/\partial \sigma)^2/2] = m^2 = E_A \cdot E_B / C^4 + \text{Potential Energy}^2 / C^4$$

For values  $(k_{\max}, |k_{\min}|) \ll 1000000$ , rich values of  $k_3$  and  $dEk3$  are not obtained, but for values  $(k_{\max}, |k_{\min}|) \geq 1000000$ , we look for  $|real(\text{values } dEk3)| \leq 4 \text{ GeV}$ .

With  $dE^2[k3] =$

$$\{2^{(7/2)} * gM^2 * k3 / (k3 * sqrt(2 * k3 + 2)) \rightarrow \text{Potential energy}$$

$$+ 2^{(7/2)} * gM^2 / (k3 * sqrt(2 * k3 + 2)) \rightarrow E_A \cdot E_B \text{ Kinematic energies}\}$$

$$\text{We calculate } E_{\text{Potential energy}} = gM \cdot \sqrt{(2^{(7/2)} * k3 / (k3 * sqrt(2 * k3 + 2)))}$$

$$\text{And obtain } E_{\text{Kinematic energy}} \neq E_A \text{ or } E_B; E_{\text{Kinematic energy}} = dEk3 - E_{\text{Potential energy}}$$

We obtain from previous algorithm:

```

import cmath
import math
kmin = -10000000
kmax = 10000000
i0 = 0
i1 = 0

```

for  $k3a$  in range( $k_{\min}$ ,  $k_{\max} + 1$ ):

    for  $k3b$  in range( $k_{\min}$ ,  $k_{\max} + 1$ ):

        if  $k3a * k3b != 0$ :

```

            if(4*3***(3/2)*(k3a+1)*(k3b+1))*(2*(k3a*(2*k3b+2)+2*k3b+2))*((9*((4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*k
3a+4*3***(7/2)***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.
sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*c
math.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(2/3)-3*((4*3***(7/2)*k
3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2)***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.
sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*c
math.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.
sqrt(3))***(1/3)+((4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2)***(2/3))/(9*((4*3***(7/2)*k3a+4*3***(7/2 ))*k3
b+4*3***(7/2)*k3a+4*3***(7/2)***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k
3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k
3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3))

```

            k3 =  $(9*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(2/3)-3*((4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2)***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3)+((4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2)***(2/3))/(9*((4*3***(7/2)*k3a+4*3***(7/2 ))*k3
b+4*3***(7/2)*k3a+4*3***(7/2)***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k
3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k
3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3))$

            if (abs(math.floor(abs(k3))-abs(k3)) <= 0.00000001) or (abs(math.ceil(abs(k3))-abs(k3)) <= 0.00000001):

                i0 += 1

                gM = cmath.sqrt(1393.6328858707575005182839547884)

#dE[k3] =  $2^{(7/4)} * abs(gM) * sqrt((k3+1)/(k3 * sqrt(2 * k3 + 2)))$

                dEk3 =  $2^{(7/4)} * gM * cmath.sqrt((k3+1)/(k3 * cmath.sqrt(2 * k3 + 2)))$

                if abs(dEk3.real) <= 4:

                    i1 += 1

                    print("Case ", i1, "/", i0, ":")

                print("k3 = ", k3, " k3a = ", k3a, " k3b = ", k3b)

                rk3 = cmath.sqrt(k3.real\*\*2 + k3.imag\*\*2)

                print("rk3 = ", rk3)

                dErk3 =  $2^{(7/4)} * gM * cmath.sqrt((rk3.real+1)/(rk3.real * cmath.sqrt(2 * rk3.real+2)))$  rdEk3 = cmath.sqrt(dEk3.real\*\*2 + dEk3.imag\*\*2)

---

```

#H = ∫dσ [X²(σ)/2 + (∂X/∂σ)²/2] = m² = E_A.E_B/C⁴ ÷ Potential Energy²/C⁴
#with dE[k3] = 2^(7/4)*abs(gM)*sqrt((k3+1)/(k3*sqrt(2*k3+2)))
#and
#E_A.E_B = dE_A[k3].dE_B[k3]
#dE²[k3] =
#{2^(7/2)*gM²*k3/(k3*sqrt(2*k3+2)) → Potential energy
#+2^(7/2)*gM²/(k3*sqrt(2*k3+2)) → E_A.E_B Kinematic energies}
    E_potential = gM*cmath.sqrt(2***(7/2)*k3/(k3*cmath.sqrt(2*k3+2)))
    E_kinematic = dEk3 - E_potential
    print("dEk3 =",dEk3," GeV")
    print("rdEk3 =",rdEk3)
    print("dErk3 =",dErk3," GeV")
    print("E_potential =",E_potential," GeV")
    print("E_kinematic =",E_kinematic," GeV")
    print()

```

→ ... ....

### 1.11.2. Previous Algorithm Is

```

import cmath
import math
kmin = -100000
kmax = 100000

for k3a in range(kmin, kmax+1):
    for k3b in range(kmin, kmax+1):
        if k3a*k3b != 0:
            if(4*3***(3/2)*(k3a+1)*(k3b+1))*(2*(k3a*(2*k3b+2)+2*k3b+2))*(9*((4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*
k3a+4*3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a+2)*k3b**2*cmath.
sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.
sqrt(2*k3 b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(1/3)) != 0:
                k3=(9*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*cmath.sqrt(2*k3a +2)*k3b**2*cmath.sqrt(2*k-
3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*cmath.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k-
3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.sqrt(3))***(2/3)3*((4*3***(7/2)*k
3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*c
math.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*c
math.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.
sqrt(3))***(1/3)+(4*3***(7/2)*k3a+4*3***(7/2))*k3b+4*3***(7/2)*k3a+4*3***(7/2))***(2/3))/(9*((4*3***(7/2)*k3a+4*3***(7/2))*k
3b+4*3***(7/2)*k3a+4*3***(7/2))***(1/3)*(9*(2*k3a+2)***(1/4)*(2*k3b+2)***(1/4)*cmath.sqrt(27*k3a**2*c
math.sqrt(2*k3a+2)*k3b**2*cmath.sqrt(2*k3b+2)+((-8*k3a**2)-8*k3a)*k3b**2+((-8*k3a**2)-8*k3a)*k3b)+3***(7/2)*k3a*c
math.sqrt(2*k3a+2)*k3b*cmath.sqrt(2*k3b+2)+((-4*cmath.sqrt(3)*k3a)-4*cmath.sqrt(3))*k3b-4*cmath.sqrt(3)*k3a-4*cmath.
sqrt(3))***(1/3))


```

```

if (abs(math.floor(abs(k3))-abs(k3)) <= 0.00000001) or (abs(math.ceil(abs(k3))-abs(k3)) <= 0.00000001):
    print("k3 =",k3, "k3a =",k3a, "k3b =",k3b)
    rk3 = cmath.sqrt(k3.real**2 + k3.imag**2)
    print("rk3 =",rk3)
    gM = cmath.sqrt(1393.6328858707575005182839547884)
    #dE[k3] = 2^(7/4)*abs(gM)*sqrt((k3+1)/(k3*sqrt(2*k3+2)))
    dEk3 = 2***(7/4)*gM*cmath.sqrt((k3+1)/(k3*cmath.sqrt(2*k3+2)))
    dErk3 = 2***(7/4)*gM*cmath.sqrt((rk3.real+1)/(rk3.real*cmath.sqrt(2*rk3.real+2)))
    rdEk3 = cmath.sqrt(dEk3.real**2 + dEk3.imag**2)
    print("dEk3 =",dEk3," GeV")
    print("rdEk3 =",rdEk3)
    print("dErk3 =",dErk3," GeV")
    print()

```

→ k3 = (15.252015994715551+26.988442113219644j) k3a = -99977 k3b = -9167

---

```

rk3 = (30.999999993575265+0j)
dEk3 = (43.289423533179345-12.027879046945008j) GeV
rdEk3 = (44.92932298847736+0j)
dErk3 = (45.10511912443094+0j) GeV

k3 = (22.751358660433908+39.979690844327074j) k3a = -99898 k3b = -96922
rk3 = (46.00000009822514+0j)
dEk3 = (39.20302478717349-10.766641702615907j) GeV
rdEk3 = (40.654615064175026+0j)
dErk3 = (40.76286823600352+0j) GeV

k3 = (15.751953006689266+27.85455037490676j) k3a = -99866 k3b = -11092
rk3 = (32.00000000176821+0j)
dEk3 = (42.945174657934906-11.919051459927925j) GeV
rdEk3 = (44.568506976394715+0j)
dErk3 = (44.737600010875255+0j) GeV

k3 = (32.826138145249125+19.142744186934145j) k3a = -99812 k3b = 31559
rk3 = (38.000000007070796+0j)
dEk3 = (42.3779587280709-5.765780019855431j) GeV
rdEk3 = (42.76839493358904+0j)
dErk3 = (42.804905232767744+0j) GeV

k3 = (38.88617135675854+22.646537862515675j) k3a = -99737 k3b = 86462
rk3 = (44.99999999939494+0j)
dEk3 = (40.59220979108459-5.49627999540387j) GeV
rdEk3 = (40.96262429961367+0j)
dErk3 = (40.99230953863432+0j) GeV

k3 = (21.751420409895772+38.24755822747227j) k3a = -99590 k3b = -74535
rk3 = (44.00000002408086+0j)
dEk3 = (39.64295002946673-10.899444991120085j) GeV
rdEk3 = (41.114004769096006+0j)
dErk3 = (41.2283521272286+0j) GeV

k3 = (36.29030566382351+21.14269886255414j) k3a = -99515 k3b = 57448
rk3 = (42.0000000436177+0j)
dEk3 = (41.311076474648466-5.603445696050985j) GeV
rdEk3 = (41.68937086551974+0j)
dErk3 = (41.72166725896865+0j) GeV

k3 = (21.251453441824104+37.38148909625858j) k3a = -99232 k3b = -65200
rk3 = (43.0000000051595+0j)
dEk3 = (39.872435550273735-10.96898397410855j) GeV
rdEk3 = (41.35371478035538+0j)
dErk3 = (41.471345681252146+0j) GeV
... ...
(k3 = (15.252015994715551+26.988442113219644j) k3a = -99977 k3b = -9167
rk3 = (30.999999993575265+0j)
dEk3 = (43.289423533179345-12.027879046945008j) GeV
rdEk3 = (44.92932298847736+0j)
dErk3 = (45.10511912443094+0j) GeV
E_potential = (43.1025066447868-11.336743959217163j) GeV
E_kinematic = (0.1869168883925454-0.6911350877278455j) GeV
... ....)

```

## 1.12. About Dark Matter and Dark Energy Process

Massive bosons are generated as in the case of Goldstone bosons and in a cosmological context with the Coleman-de Luccia Tun-

neling, as an impossible false vaccum. When  $\Delta\Phi$  is extremely large False vacuum decay is replaced by massive bosons emissions. With equations:

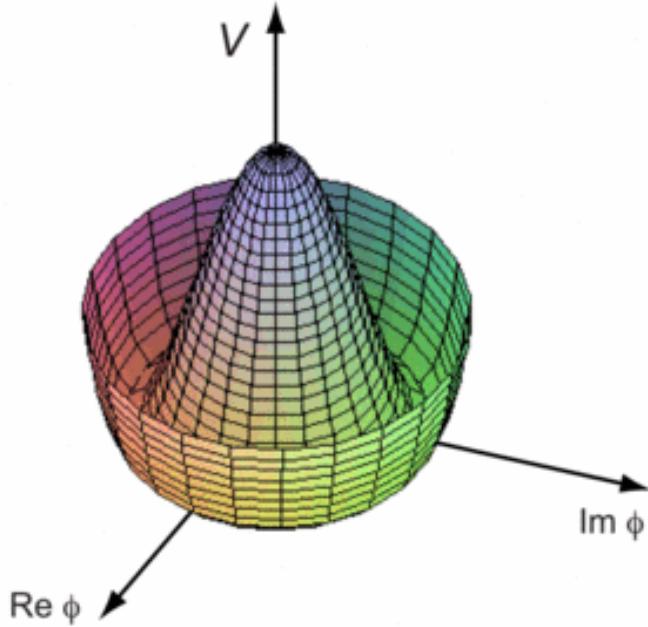
To nucleate, a bubble must overcome an energy barrier of height

$$\Phi_c = 3\gamma/4R^2 - \Delta\Phi, (E. 1)$$

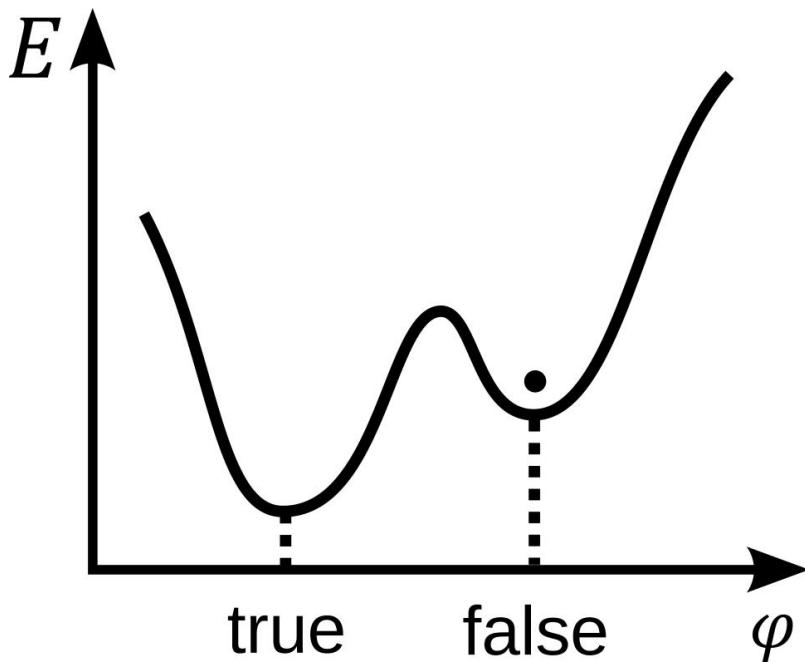
where  $\Delta\Phi$  is the difference in energy between the true and false vacuums,  $\gamma$  is the unknown (possibly extremely large) surface tension of the domain wall, and  $R$  is the radius of the bubble. Rewriting E. 1 gives the critical radius as

$$R_c = \sqrt{3\gamma/(4\Delta\Phi)}. (E. 2)$$

A bubble smaller than the critical size can overcome the potential barrier via quantum tunnelling of instantons to lower energy states. When the energy at the MAD is smaller due to conversions in massive bosons, we have the value  $R$  equivalent to becoming smaller and a Tunneling effect can occur (with particles sent outside black hole's core)



**Figure 15:** Goldstone Boson



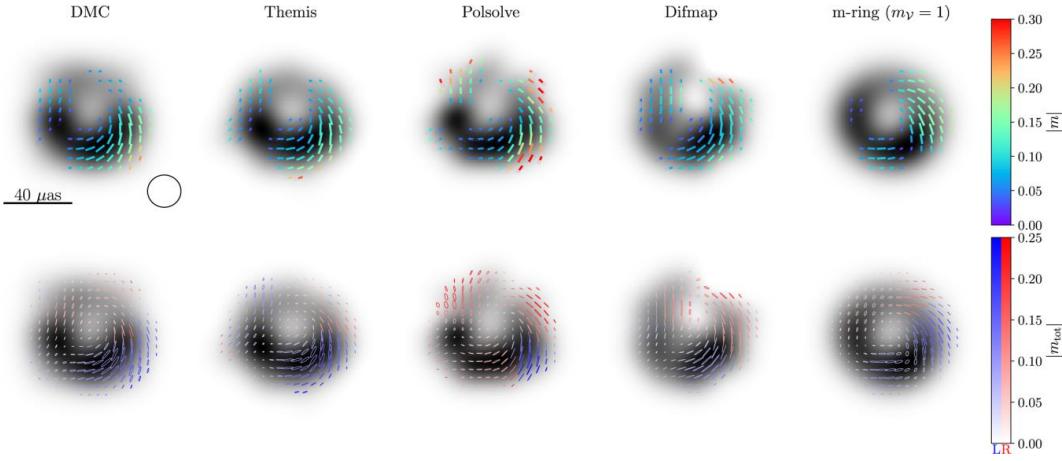
**Figure 16:** A scalar field  $\phi$  (which represents physical position) in a false vacuum. The energy  $E$  is higher in the false vacuum than that in the true vacuum or ground state, but there is a barrier preventing the field from classically rolling down to the true vacuum. Therefore, the transition to the true vacuum must be stimulated by the creation of high-energy particles or through quantum-mechanical tunneling [10,17-22].

## 2. EHT Results

It is found that most simulations naturally produce a low level of circular polarization consistent with our upper limit and that Faraday conversion is likely the dominant production mechanism for circular polarization at 230 GHz in M87\*. All methods find a moderate level of resolved circular polarization across the image ( $\langle |v| \rangle < 3.7\%$ ), which is consistent with the low fraction of circular polarization measured by the Millimeter/Submillimeter Observatory of the Atacama (ALMA) ( $|v_{int}| < 1\%$ ) over the entire image. This means that there is some amount of circular polarization present in the image, but it is not very intense. But tentative detection of a low value of the Stokes intensity  $v$  is carried out with a signal-to-noise ratio (SNR) of about 5. This suggests that there is an indication of the presence of some linear polarization in the data, but this is still weak and requires further analysis to confirm. Despite this broad agreement, the methods show substantial variation in the morphology of the circularly polarized emission, indicating that our conclusions are strongly dependent on the imaging assumptions because of the limited baseline coverage, uncertain telescope gain calibration, and weakly polarized signal. Therefore the EHT results confirm an effective and continuous MAD process., (National Radio Astronomy Observatory) [23].

A supermassive black hole's strong magnetic fields are revealed in a new light Closure phases observed on the ALMA-SMT-PV triangle during M87\* observations on 2017 April 5–11 in low band (left column) and in high band (right column). Top: closure phases of scan-averaged visibilities for all epochs, RR\* in red, LL\* in blue. Bottom: difference of closure phases between RR\* and LL\*. The zero level of the closure difference (i.e., no detected) is marked with a black dashed line. A light-green band shows the RR\* – LL\* difference, inferred by band, under the constant difference assumption [4]. For this antenna triangle, the average offset in closure phases between RR\* and LL\* (combining all epochs and assuming a constant residual value) is  $6.7 \pm 1.3$  deg in the low band and  $7.9 \pm 1.6$  deg in the high band, indicated with green bands in the bottom panels. The offset is consistent despite each band being calibrated independently. Moreover, the measured offset is difficult to explain with the conservative systematic nonclosing error budget discussed in Section 8.4 of Paper III, and hence it implies a tentative detection of a weak Stokes  $v_{\text{medium}}$  at the level of  $S/N \sim 5$ .

While this measurement implies the presence of a fractional CP reaching  $\sim 3\%$  somewhere in the visibility domain, the measurement cannot be directly translated into a quantitative image domain constraint. The ALMA-SMT-PV triangle shown is the one that produces closure phase differences with the most clear deviation from zero. In Appendix B, we show the results for all other triangles including ALMA. None of these other triangles show an unambiguous detection of a nonzero closure phase difference like that seen on the ALMA-SMT-PV triangle, suggesting that SMT-PV is the baseline most sensitive to the CP signatures in M87\*. Even though the RR\* and LL\* closure phases are robust against antenna gains, they may be affected by instrumental polarimetric leakage (antenna D-terms, the D matrix term in Equation (3)). However, the effect of D-term uncertainties in the parallel-hand visibilities is much smaller than in the cross-hands (e.g., Smirnov 2011), which implies that Stokes is much less affected by instrumental polarization than Stokes Q and  $\mu$ . To verify a negligible impact of the polarimetric leakage on the closure phase signal, we have compared the closure phase values between the data with and without D-term calibration. For all triangles related to ALMA, the effect of the D-terms on the RR\* – LL\* closure differences is always less than the standard deviation of the thermal noise on the closure phase difference. For the triangle shown in previous Figure, the maximum effect of the D-terms is only  $0.42\sigma$ . Hence, we can conclude that the closure phase differences indicating the presence of circular polarization on EHT baselines, presented in previous Figure, are robust against both antenna gains and polarimetric leakage. In Appendix C, we discuss evidence for polarization in "closure trace" products, quantities that are insensitive to all station-based systematic factors, including D-terms.



**Figure 17:** Reconstructions of 2017 EHT M87\* data from April 11, low band. The top row shows total intensity images from all reconstruction methods in gray scale and fractional linear polarization in colored ticks as in Paper VII. The second row shows the same grayscale total intensity image overlaid with colored ellipses indicating the total polarization fraction  $|m_{\text{tot}}| = \sqrt{(Q^2 + \mu^2 + v^2)/x}$ . The size of each ellipse indicates the total polarized brightness; the orientation of each ellipse indicates the linear EVPA, and axis ratio indicates the relative fraction of circular polarization [4].

Circular polarization imaging results from 2017 EHT observations of M87\* on April 5 (top two rows) and April 6 (bottom two rows). Images of circular polarization on these consecutive days are expected to be nearly identical, as is seen in total intensity and linear polarization. The top/bottom row in each pair shows results from imaging the high/low-band data. In each panel, total intensity is indicated in the colored linear-scale contours, and the Stokes brightness is indicated in the diverging color map, with red/blue indicating a positive/negative sign. The color bar ranges are fixed in both plots (and in next Figure). For posterior exploration methods (DMC, Themis, m-ring fitting), the posterior-average image is shown. All images are blurred with the same 20  $\mu\text{as}$  FWHM Gaussian, shown with the black inset circle in the upper left panels [4]. The same as previously, but for 2017 EHT observations of M87\* on April 10 (top two rows) and April 11 (bottom two rows) [4].

Circular polarization properties of passing Paper VIII one-zone models. Left: distribution of the Faraday conversion optical depth  $\tau_F Q$  in passing models. In all passing models  $\tau_F Q > 1$ , indicating that most circular polarization is likely produced by Faraday conversion. Middle: distribution of the ratio of the Faraday rotation to Faraday conversion optical depths. In all cases,  $\tau_F V > \tau_F Q$ , indicating that with a constant field orientation in the emission region, circular polarization will dominate over linear polarization in these models. Right: the average fractional circular polarization between 5rg and 10rg in one-zone models with a rotating magnetic field direction along the line of sight, as a function of the angular rotation frequency  $\omega$ . We show three different models: a model with low Faraday conversion depth (blue), a model with median conversion depth (orange), and a model with high conversion depth (green). Dashed lines show corresponding results for one-zone models with no intrinsic emission of circular polarization,  $j_v = 0$  [4].

A random selection of representative snapshots from our GRMHD image library. The color scales for each snapshot are normalized individually. The first three rows are presented at native resolution in symmetric logarithmic scale with three decades in dynamic range shown to better visualize faint features. The bottom three rows plot Stokes  $x$  in contours and Stokes  $v$  in color after blurring with a 20  $\mu\text{as}$  FWHM Gaussian, both in linear scale. Models exhibit a wide variety of morphologies and almost always show sign reversals, at both perfect resolution and EHT resolution [4]. Example GRMHD snapshot ( $\text{MAD } a^* = -0.94$   $R_{\text{low}} = 10$   $R_{\text{high}} = 160$ ) plotted with both magnetic field configurations, aligned (left) and reversed (right). The top panels show the images blurred to EHT resolution, and the bottom panels show the images at their native resolution. As shown in the left panels, this snapshot fails simultaneous polarimetric constraints with the aligned-field configuration, overproducing  $v_{\text{net}}$ . However, as shown in the right panels, flipping the magnetic field polarity produces some oppositely signed regions that reduce  $\Box v_{\text{net}} \Box$ . Flipping the field has no effect on the total intensity image [4].

This illustrates that it is not easy to predict which regions of a given image change upon a reversal of the magnetic field direction. We expect that regions dominated by intrinsic synchrotron emission should trivially flip sign, while regions dominated by Faraday conversion may remain unchanged unless Faraday rotation is significant along those geodesics. We further explore the effect of flipping the magnetic field polarity on linear polarization in Appendix I. While there are noticeable differences in the distribution of the  $\angle \beta_2$  parameter. Palumbo et al across all GRMHD models, the effect is less dramatic for linear polarization metrics than it is for

circular. Imaging results from the three synthetic data sets in Table 4. The first row shows the total intensity in gray scale and the fractional linear polarization in the colored ticks. The left column is the ground-truth simulation image. From left to right, the next columns show the posterior-average images from DMC and Themis, the final CLEAN images from polsolve and DIFMAP, and the posterior average of the m-ring model fits. All images are blurred with the same 20  $\mu$ as FWHM circular Gaussian beam. The second row shows the total intensity image with eight contour levels on a linear scale and the Stokes v structure in a diverging color map. The first and second rows show the results for model 01 (low resolved circular polarization), the third and fourth rows show the results for model 02 (moderate resolved circular polarization), and the fifth and sixth rows show the results for model 03 (high resolved circular polarization). Note that the color bar for v has different maximum values in the second, fourth, and sixth rows as the GRMHD simulation images become more polarized [4].

Examples of three m-ring models in Stokes x and p (top panels) and Stokes x and v (bottom panels) [4]. Throughout the panels, the Stokes x structure (heat map) is kept constant with  $F = 0.5$  Jy,  $d = 40$   $\mu$ as,  $\alpha = 10$   $\mu$ as, and  $\beta_{x,1} = 0.2 - 0.1i$ . The top middle panel shows a linear polarization structure with  $m_{\text{net}} = \beta_{p,0} = 0.1$ ,  $\beta_{p,-1} = 0.1 + 0.2i$ , and  $\beta_{p,1} = -0.1 + 0.1i$ . In the top left and right panels, nonzero  $\beta_{p,2}$  components have been added with opposite sign. The bottom left panel shows a dipolar circular polarization structure (contours) oriented toward the north ( $\beta_{v,0} = 0.14$ ). The net circular polarization is zero, so that the north and south half of the ring are identical with opposite sign in Stokes  $\beta_v$ . In the bottom middle panel, we have rotated the circular polarization structure by  $-45^\circ$  and introduced a nonzero net circular polarization ( $v_{\text{net}} \equiv \beta_{v,0} = 0.05$ ), so that the symmetry is broken. Finally, in the bottom right panel we have added a nonzero  $\beta_{v,2}$  component, increasing the complexity of the azimuthal structure in Stokes v. The model shown in the middle panels is used for our geometric tests [32]. Test of plasma content, where we ray-trace a single snapshot of the MAD  $a = + 0.5$  Rhigh = 80 Rlow = 10 aligned-field model with an increasing positron-to-electron ratio, denoted as f in the upper left corner of each panel. The Stokes v structure clearly evolves as f increases, but we do not observe a clear discriminant of plasma content [4].

In next figure, we spot-check our sensitivity to our assumption of thermal electrons by ray-tracing a GRMHD snapshot with three different assumptions for the electron distribution function. A new plasma density scale is found for each image to match the total flux of the image with thermal electrons, 0.7 Jy. This snapshot corresponds to the MAD  $a = + 0.5$  Rhigh = 80 Rlow = 10 aligned-field model. In the top row, we plot images blurred to EHT resolution, while in the bottom row we plot perfect-resolution images of Stokes in symmetric logarithmic scale. Compared to the leftmost image assuming thermal electrons, we find very little changes in the variable kappa model shown in the middle panel. This is broadly consistent with our findings in Event Horizon Telescope Collaboration et al. (2022d) for Sgr A\* in total intensity. Thus, at least for this snapshot, exchanging a thermal distribution for a physically motivated nonthermal electron distribution has very little effect on Stokes . However, we report dramatic differences when switching to a constant kappa model with a value of  $\kappa = 5$ . As found in many other studies, nonthermal electrons make the image noticeably larger and more diffuse (e.g., Özel 2000; Mao et al. 2017; Fromm et al. 2022; Ricarte et al. 2023). Intriguingly, although the plasma density is decreased only by a factor of 4 compared to the thermal model, the Stokes v signal almost entirely vanishes. This may be due to the fact that Faraday conversion is caused by the coldest relativistic electrons, which occur at a smaller fraction in  $\kappa$  models by definition. A single GRMHD snapshot (MAD  $a = + 0.5$  Rhigh = 80 Rlow = 10 aligned field) ray-traced with three different electron distribution functions. The physically motivated variable kappa model produces both a Stokes x and Stokes v image very similar to the thermal model. However, a model with fixed  $\kappa = 5$  produces a much more diffuse Stokes x and extremely little Stokes v [24-26].

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